

LET US INTRODUCE A 0-1 VARIABLE  $y_{ij}$

$$y_{ij} = \begin{cases} 0 & \text{if } j \text{ precedes } i \\ 1 & \text{if } i \text{ precedes } j \end{cases}$$

THEN THE EARLIER TWO CONSTRAINTS CAN BE WRITTEN AS ( $M$  IS A LARGE POSITIVE NUMBER)

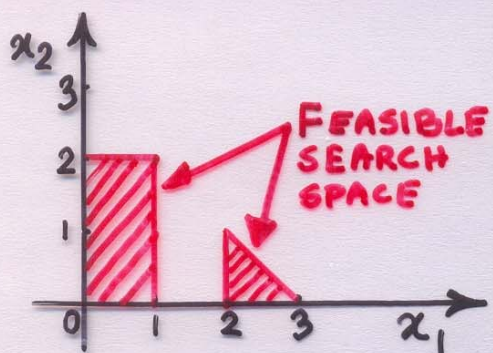
$$M y_{ij} + (x_i - x_j) \geq a_j \quad \dots \dots \dots \textcircled{1}$$

$$M(1 - y_{ij}) + (x_j - x_i) \geq a_i \quad \dots \dots \dots \textcircled{2}$$

NOTE: IN THE EVENT  $i$  precedes  $j$  (i.e.  $y_{ij} = 1$ ) CONSTRAINT  $\textcircled{2}$  BECOMES ACTIVE AND  $\textcircled{1}$  REDUNDANT. THIS IS WHAT WE SET OUT TO DO; THAT IS, IF IT IS BENEFICIAL TO DO  $i$  BEFORE  $j$  THEN STARTING TIME OF  $j$  MUST BE AT LEAST  $a_i$  UNITS AFTER THE START OF PROJECT  $i$ .

ALSO NOTE IF  $y_{ij}$  IS USED IN THE FORMULATION THERE IS NO NEED TO USE  $y_{ji}$ .

CONSIDER A PROBLEM WHOSE FEASIBLE SEARCH SPACE IS GIVEN AS FOLLOWS:



THE QUESTION IS HOW DOES ONE REPRESENT THIS NON-CONVEX SEARCH SPACE THROUGH LINEAR CONSTRAINTS

THIS IMPLIES

$$\begin{matrix} x_1 \leq 1 & \text{OR} & x_1 \geq 2 \\ x_2 \leq 2 & & x_1 + x_2 \leq 3 \end{matrix}$$

DEFINE  $y = \begin{cases} 1 & \text{if LEFT AREA IS USED} \\ 0 & \text{if RIGHT AR. IS USED.} \end{cases}$

$$\begin{aligned} x_1 + M y &\geq 2 \\ x_1 + x_2 - M y &\leq 3 \\ x_1 - M(1 - y) &\leq 1 \\ x_2 - M(1 - y) &\leq 2 \end{aligned}$$