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**FLOW AND THERMAL FIELDS IN A PENDANT DROPLET  
MOVING ON LYOPHOBIC SURFACE****Basant Singh Sikarwar**Department of Mechanical Engineering  
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samkhan@iitk.ac.in**ABSTRACT**

Clusters of liquid drops growing and moving on physically or chemically textured lyophobic surfaces are encountered in drop-wise mode of vapor condensation. As opposed to film-wise condensation, drops permit a large heat transfer coefficient and are hence attractive. However, the temporal sustainability of drop formation on a surface is a challenging task, primarily because the sliding drops eventually leach away the lyophobicity promoter layer. Assuming that there is no chemical reaction between the promoter and the condensing liquid, the wall shear stress (viscous resistance) is the prime parameter for controlling physical leaching. The dynamic shape of individual droplets, as they form and roll/slide on such surfaces, determines the effective shear interaction at the wall. Given a shear stress distribution of an individual droplet, the net effect of droplet ensemble can be determined using the time averaged population density during condensation.

In this paper, we solve the Navier-Stokes and the energy equation in three-dimensions on an unstructured tetrahedral grid representing the computational domain corresponding to an isolated pendant droplet sliding on a lyophobic substrate. We correlate the droplet Reynolds number ( $Re = 10-500$ , based on droplet hydraulic diameter), contact angle and shape of droplet with wall shear stress and heat transfer coefficient. The simulations presented here are for Prandtl Number ( $Pr = 5.8$ ). We see that, both Poiseuille number ( $Po$ ) and Nusselt number ( $Nu$ ), increase with increasing the droplet Reynolds number. The maximum shear stress as well as heat transfer occurs at the droplet corners. For a given droplet volume, increasing contact angle decreases the transport coefficients.

**INTRODUCTION**

The sliding of liquid drops underneath a lyophobic surface has been a subject of extensive research in many industrial and engineering applications such as drop-wise condensation heat transfer, microfluidics, lab-on-chip device, ink jet printing systems, spraying of insecticide on crops and several biochemical processes. It is known that the dynamic steady state of condensing vapors on a cold substrate involves a large population or ensemble of droplets, representing various temporal generations [1-4]. The droplets increase in size by combination of direct condensation and coalescence with neighboring droplets [5-6]. As droplets grow, the body forces eventually exceed the droplet retention force due to surface tension which leads to sliding of drops and eventual fall off. This exposes virgin substrate portions where another temporal generation of droplets begins to grow; the cycle is repeated as shown in Figure 1.

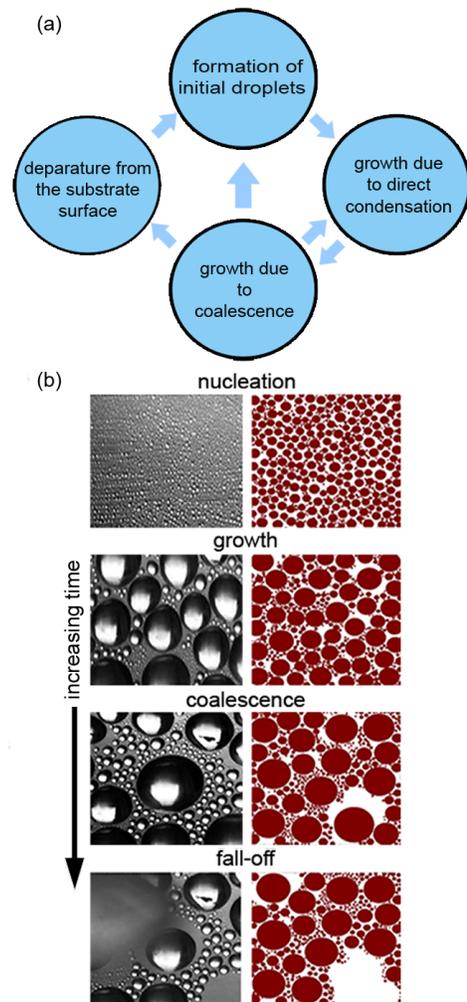
The long term sustainability of dropwise condensation depends on the shear interaction of sliding droplets with the promoter layer creating lyophobicity. The phenomenon of removal of promoter layers or surface damage due to sliding of drop is called surface leaching. This phenomenon is primarily affected by viscous forces at the contact surface, chemical reactions between the condensing liquid and the lyophobic promoter; the heat transfer rate and temperature fluctuations will also affect these interactions. Open literature on surface leaching due to droplet motion is limited. Most of the existing works [7-13] have considered static critical state of sessile drop on inclined surface and focused on the contact angle hysteresis, drop shape, and drop retention with tiltable surface of various combinations

of the hydrophobic surface and the liquid. Elsherbine and Jacobi [12-13] performed experiments on an isolated sessile droplet and reported that the drop is deformed at the static critical state of an inclined plane. They investigated the geometric parameters necessary to describe the shape of the sessile drop and retention forces at this state.

Though a large volume of work exists on the drop shape, its spreading and stability on a tilted plane, very few researchers have reported the sliding behavior of the drop on inclined surface [14-26]. Kim et al. [14] performed experiments for measuring the steady sliding velocity of different liquid drops on an inclined surface and reported a scaling law to determine the sliding velocity of a liquid droplet of known wetting characteristics. Huang et al. [15] used a numerical technique, i.e. the front tracking method, to determine the motion of two-dimensional drops and bubbles on a partially wetting surface exposed to shear flow. Gao and McCarthy [16] postulated two mechanisms for drop moving down the plane. Droplets can move by sliding where the particles near the solid-liquid interface exchange their position with those at the gas-liquid interface while the bulk of the fluid remains unaffected. The particle movement along the gas- liquid and solid-liquid interfaces is similar to the motion of a tread of a chain-driven tank. On the other hand, there could be rolling motion where the entire fluid mass undergoes a circulatory movement. Suzuki et al. [17] studied the sliding behavior of water droplets on various chemically textured surfaces at a fixed inclination of 35° and reported the sliding displacement of the advancing edge of the droplet. Sakai et al. [18] studied the rolling versus sliding behavior of droplet on various chemically textured surfaces. Annapragada et al. [19] have performed experiments to characterize the velocity dependence of advancing and receding angles as a function of the Capillary number. In their theoretical analysis, Grand et al. [20] scaled the viscous force as  $\mu UV^{1/3}$  and reported that the drop sliding velocity along an inclined plane is a linear function of the Bond number. Yoshida et al. [21] did not consider the viscous force in their study of sliding behavior of water droplets on a flat polymer surface. The authors reported that the sliding motion changes from constant velocity to one of constant acceleration with an increase in the contact angle. Daniel et al. [22] reported the maximum velocity of the condensing sessile drop on a chemically textured surface. Sakai and Hashimoto [23] have experimentally determined the velocity vector distribution inside a sliding sessile drop using PIV. The authors reported that the velocity gradient near the liquid-solid interface is higher than locations elsewhere inside a drop. This analysis was further used to recognize the slipping and rolling components of the sliding velocity and the acceleration of the water droplet [24]. Das and Das [25] used smooth particle hydrodynamics (SPH) to numerically simulate the movement of drops down an inclined plane. The study captured the internal circulation inside a sliding sessile drop. It was shown that the frictional resistance by viscosity at the interface of solid and liquid cannot be neglected in estimating the sliding

behavior and related effects for a droplet moving on an incline substrate.

To the best of the knowledge of the authors there is no literature available that correlates droplet shape and flow parameters with wall shear stress (friction coefficient) and heat transfer coefficient (Nusselt Number) of an isolated droplet sliding underneath a lyophobic surface. We have therefore aimed at providing a correlation between the droplet shape, contact angle, volume, sliding velocity and the ensuing friction factor as well as the heat transfer coefficient. Section 2 of the paper describes the mathematical formulation of the problem and defines of the non-dimensional numbers of interest. Sections 3 and 4 describe the procedures of calculation of wall shear stress and wall heat transfer coefficient and discuss the implications thereof. Finally, conclusions are reported in Section 5.



**Figure 1: Complete cycle of dropwise condensation underneath chemically textured inclined surface [5]. (a) Cycle of drop formation to sliding motion and finally a gravitational falloff. (b) Experimentally observed cycle and cycle captured by computer simulation.**

## NOMENCLATURE

|               |   |
|---------------|---|
| $A_{yz max}$  | maximum cross-sectional area of the droplet in the YZ plane (m <sup>2</sup> ) |
| $C_p$         | specific heat of the liquid (J/kg-K)  |
| $D_{hyd}$     | hydraulic the diameter of the droplet (m)                                     |
| $d$           | diameter of the droplet (m)   |
| $d_b$         | base diameter of the droplet (m)  |
| $H$           | maximum height of the droplet (m)   |
| $h$           | heat transfer coefficient (W/m <sup>2</sup> -K)                               |
| $k$           | thermal conductivity (W/m-K)  |
| $\bar{n}$     | unit normal vector of the surface (-)   |
| $P$           | wetted perimeter, length of the contact line (m)                              |
| $p$           | pressure (Pa)   |
| $q$           | heat flux (W/m <sup>2</sup> )   |
| $t$           | time (s)  |
| $\bar{t}$     | unit tangent vector (-)   |
| $T$           | temperature (°C)  |
| $\Delta T$    | temperature difference between wall and the drop interface (°C)               |
| $u$           | velocity (m/s)  |
| $U_{wall}$    | sliding velocity of the wall (m/s)  |
| $V$           | volume of drop (m <sup>3</sup> )  |
| $\rho$        | density (kg/m <sup>3</sup> )  |
| $\mu$         | dynamic viscosity (Pa-s)  |
| $\sigma$      | surface tension (N/m)   |
| $\phi$        | viscous dissipation function (1/s <sup>2</sup> )                              |
| $\tau$        | shear stress (N/m <sup>2</sup> )  |
| $\tau_{wall}$ | wall shear stress (N/m <sup>2</sup> )   |
| $\theta$      | contact angle (°)   |
| $\theta_a$    | advancing angle of the droplet (°)  |
| $\theta_r$    | receding angle of the droplet (°)   |

## Non-dimensional parameters

|       |   |
|-------|---|
| Bo    | Bond number ( $\rho g d_b^2 / \sigma$ )                     |
| Ca    | Capillary number ( $\mu U_{wall} / \sigma$ )                |
| $C_f$ | Coefficient of friction ( $\tau_{wall} / \rho U_{wall}^2$ ) |
| Nu    | Nusselt number ( $h d_b / k$ )                              |
| Po    | Poiseuille number ( $C_f \cdot Re$ )                        |
| Pr    | Prandtl number ( $\mu C_p / k$ )                            |
| Re    | Reynolds number ( $\rho U_{wall} D_h / \mu$ )               |

## Subscripts

|        |  |
|--------|--|
| $a$    | advancing angle                                      |
| $b$    | base of the droplet                                  |
| $f$    | friction   |
| $free$ | free surface of the droplet                          |
| $hyd$  | hydraulic  |
| $i$    | free indices   |
| $j$    | repeated indices                                     |
| $max$  | maximum  |
| $p$    | pressure   |
| $r$    | component in radial direction; spherical coordinates |
| $wall$ | wall   |

|           |  |
|-----------|--|
| $x, y, z$ | component in the $x, y,$ or $z$ direction respectively     |
| $xy$      | $xy$ plane   |
| $yz$      | $yz$ plane   |
| $zy$      | $zy$ plane   |
| $\theta$  | component in the $\theta$ direction, spherical coordinates |
| $\phi$    | component in the $\phi$ direction, spherical coordinates   |

## MATHEMATICAL DESCRIPTION

The schematic diagram of the three-dimensional deformed drop with an advancing angle 105° and a receding angle 55° as well as symmetric drops of various contact angles (90, 105 and 120°) are shown in Figure 2. The liquid droplet is treated as fixed relative to which the wall (substrate) is moving at a constant speed. The volume of the droplet for all computations is fixed and is equal to 134  $\mu$ l. The shape of drops for various contact angles is taken to be a part of sphere while the shape of the deformed droplet is determined by a procedure described by Sikarwar et al. [6]<sup>1</sup>.

The hydraulic diameter of the droplet is calculated with respect to the maximum cross section of drop over the YZ plane ( $A_{yz|max}$ ) and the wetted perimeter,  $P$ , of the droplet base area on the wall (substrate), as given below (refer Fig. 3):

$$D_{hyd} = (4 \cdot A_{yz|max}) / P \quad (1)$$

Wall shear stress is determined by solving the three dimensional Navier-Stokes equation; the boundary conditions are no slip at the wall and free surface (zero shear) elsewhere on the droplet. The wall heat transfer coefficient is obtained by solving the three dimension energy equation for a pair of constant temperature boundaries at the wall and the free surface respectively, as given by Eqs. (2-5). Boundary condition at the free surface is in spherical coordinates as given by Eq. (5). They need to be transformed from spherical to Cartesian coordinates during the numerical implementation. For a deformed drop, a local coordinate system is used for boundary conditions. The flow field and heat transfer rates have been obtained for Reynolds numbers in the range 10-500 at Pr = 5.8.

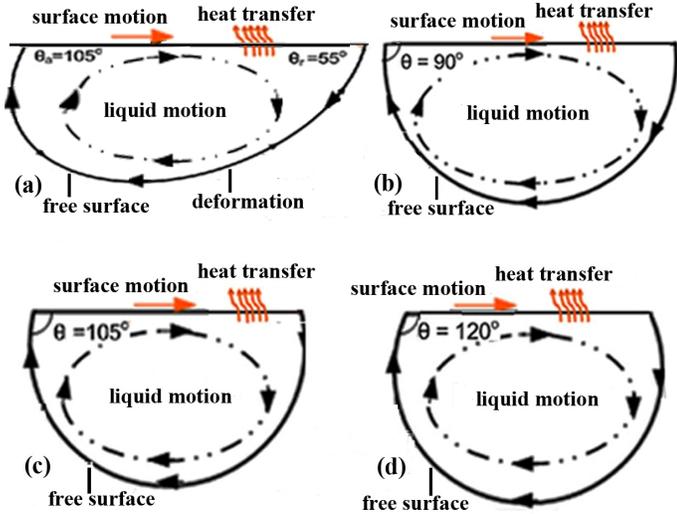
The governing equations for an incompressible liquid with proper boundary conditions are summarized as follows:

$$\rho \left( \frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} \right) = - \frac{\partial p}{\partial x_i} + \mu \frac{\partial^2 u_i}{\partial x_j^2} \quad (2)$$

$$\rho \cdot C_p \left( \frac{\partial T}{\partial t} + u_j \frac{\partial T}{\partial x_j} \right) = k \frac{\partial^2 T}{\partial x_j^2} + \mu \cdot \phi \quad (3)^2$$

<sup>1</sup> The shape of liquid-vapor interface is obtained by solving the Young-Laplace equation that enforces a balance between pressure force, gravity and surface tension. Static equilibrium condition leads to the rate of change of curvature at each location of the droplet, which is solved by the Runge-Kutta method. The details are given in [6].

<sup>2</sup> The contribution of viscous dissipation was found to be insignificant.



**Figure 2: Schematic diagram of (a) a deformed drop (b) a symmetric drop with contact angle  $90^\circ$ , (c) a symmetric drop of contact angle  $105^\circ$ , and (d) a symmetric drop of contact angle  $120^\circ$ .**

Boundary condition at the wall and the free surface:

$$u_x = U_{wall}; u_y = 0; u_z = 0; T = T_{wall} \quad (4)$$

$$u_r = 0; \tau_{r\theta} = 0; \tau_{r\phi} = 0; T = T_{free} \quad (5)$$

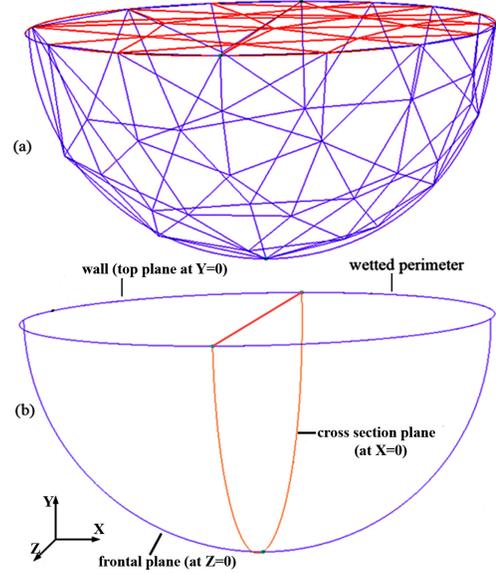
Fluid flow and heat transfer rates inside the drop have been obtained by numerically solving the unsteady Navier-Stokes and energy equations in three dimensions. The drop deformation arising from fluid motion is neglected. From the flow and temperature distributions, the wall shear stress and heat transfer coefficient are calculated from Eq. (6) followed by Eqs. (7-8).

$$\left. \begin{aligned} \tau_{xy} &= \mu \left[ \left( \frac{\partial u_x}{\partial y} \right) + \left( \frac{\partial u_y}{\partial x} \right) \right]_{wall} \\ \tau_{zy} &= \mu \left[ \left( \frac{\partial u_z}{\partial y} \right) + \left( \frac{\partial u_y}{\partial z} \right) \right]_{wall} \\ \tau_{wall} &= \sqrt{\tau_{xy}^2 + \tau_{zy}^2} \end{aligned} \right\} \quad (6)$$

$$q = -k \left[ \frac{\partial T}{\partial n} \right] = -k \left[ \frac{\partial T}{\partial y} \right]_{wall} \quad (7)$$

$$h = q / \Delta T \quad (8)$$

Here,  $\Delta T$  is the temperature difference between the wall and the surface of the droplet.



**Figure 3: Computational domain within the drop. (a) Triangular base of the tetrahedral element is shown on the surface. (b) Various planes of the drop of contact angle  $90^\circ$ .**

The Reynolds number is defined on the basis of the hydraulic diameter of the drop and Prandtl number is defined at an average temperature (mean temperature of the two boundary conditions) of the drop.

$$\text{Reynolds number (Re)} = (\rho \cdot U_{wall} \cdot D_{hyd}) / \mu \quad (9)$$

$$\text{Prandtl Number (Pr)} = (\mu \cdot C_p) / k \quad (10)$$

$$\text{Nusselt Number (Nu)} = (h \cdot D_{hyd}) / k \quad (11)$$

## NUMERICAL METHODOLOGY

The computational approach adopted in the present study is based on finite volume discretization (FVM) of the three dimensional unsteady Navier-Stokes and energy equations over an unstructured mesh. Between vertex-centered and cell-centered placement of variables, the pressure correction procedure is cell centered, collocated with the fluid velocities [26]. The unstructured mesh is filled with tetrahedral elements of nearly equal volumes. Pressure-velocity coupling is treated using a smoothing pressure correction method that results in a SIMPLE-like algorithm. Convective terms are discretized by a second order upwind scheme. Geometry invariant features of the tetrahedral element are used so that the calculation of gradients at cell faces is simplified using nodal quantities of a particular variable. Nodal quantities, in turn, are calculated as a weighted average of the surrounding cell-centered values [27]. The diffusion terms are discretized using a 2<sup>nd</sup> order central-difference scheme.

Free surface boundary is discretized in spherical coordinates and transformed to Cartesian coordinates. The discretized free

surface boundary condition is described in the previous work of the authors [6]. The discretized system of algebraic equations is solved by the Stabilized Bi-Conjugate Gradient method (biCGStab) with a diagonal pre-conditioner. The overall solution algorithm used for the present study is quite similar to that proposed by Date [28]. Points of difference are related to the use of certain invariant properties of the tetrahedral element, powerful linear equations solver as well as a parallel implementation of the computer program. Iterations within the code are run till a convergence in terms of the absolute residual of order  $\sim 10^{-7}$  is reached.

The computer code has been validated against many benchmark problems, such as, a three-dimensional lid driven cavity at  $Re = 400$  [29], as shown in Figure 4, flow through pipe and experimental results of steady flow through the human carotid bifurcation available [30]. Close agreements lend the desired validation of the code. The number of cells within the drop required for grid independence at the highest Reynolds number was close to 700,000.

## RESULTS AND DISCUSSION

To give a complete picture of the flow patterns inside a sliding drop, computed predictions are displayed in the form of velocity profiles, contours of velocity magnitude, velocity vectors, streamline plots, wall shear stress, dimensionless temperature, wall heat transfer coefficient as well as wall pressure distribution. Reynolds numbers considered are  $Re = 10, 50, 100,$  and  $500$  at a Prandtl number of  $5.8$ . A typical computational domain with triangular faces on the boundary, tetrahedral elements inside the droplet volume and the corresponding Cartesian coordinate system is shown in Figure 3(a) for a contact angle of  $90^\circ$ . Similar grids are generated for other geometries – symmetric and deformed. Flow parameters are displayed on the X-Y plane (frontal plane) where  $Z=0$ , X-Z plane where  $Y=0$  and Z-Y plane (cross section plane) where  $X=0$  as shown in Figure 3(b). The fluid flow patterns inside the drop of contact angle  $90^\circ, 105^\circ,$  and  $120^\circ$  respectively are shown in Figures 5-12. The velocity vectors and the velocity profile at the center of the frontal plane (corresponding to  $A_{xylmax}$ , at  $X=0$ ) have been shown in Figures 5-7. The results show that the  $u$  velocity variation is nearly linear with respect to height ( $y$ ) of the drop at  $X=0$ . These results are in agreement with the PIV studies reported in [18] and [24]. With increasing  $Re$ , the location inside the drop where the  $x$ -component velocity changes its sign shifts towards the base of the drop. In this plane, the magnitude of velocity at the free surface nearly matches the imposed wall velocity though in the opposite direction. Qualitatively comparing drops of contact angles  $90^\circ, 105^\circ,$  and  $120^\circ$  respectively, we find that there is no major difference in the distributions of velocity components and therefore the overall flow pattern. Deformed drops also show similar qualitative flow distribution at various Reynolds numbers. The point of zero velocity was seen to move closer to the solid wall at Reynolds numbers of  $1000$  and higher. On the Y-Z plane, multiple cells of circulations were

observed creating a low pressure zone across the drop (Figures 8-9). The velocity vectors in Figures 5-7 agree well with published experimental data [25] and the smooth particle hydrodynamics estimations in [26].

The derived flow parameters (wall pressure and wall shear stress) for symmetric drops at various contact angles are shown in Figures 8-13. The pressure distributions at the wall surface are shown in Figures 8-10. The pressure distributions at the wall are seen to be qualitatively similar in these cases. It is seen that the wall pressure at the center of the base is smaller (negative) than that towards the sides. Figures 8-10 also show that wall pressure variation is heightened for increasing values of Reynolds number. The wall shear stress distribution, determined by using Eq. (6), for Reynolds number  $10$  to  $500$  are shown in Figures 11-13. It is understandable that the region close to the contact line is a high shear zone [31, 32]. This is clearly seen in Figures 11-13, as we move away from the contact line and come in the inner zone of the base of the drop, the shear stress reduces. It can also be clearly observed that average shear stress is a strong function of the Reynolds number. It is also dependent on the contact angle. This is quantitatively depicted in Fig. 13 for the average wall shear stress which highlights increase in the Poiseuille number with increase in Reynolds number. The average wall shear stress distribution is high for a deformed drop in comparison to symmetric drop of contact angles  $90^\circ, 105^\circ$  and  $120^\circ$  respectively, as shown in Figure 13.

The non-dimensional temperature  $= (T - T_{wall}) / (T - T_{free})$

contours inside the drop on selected frontal planes are shown in Figures 15-17. Near the wall and the free surface, the normal velocity component is zero and diffusion is the dominant mode of heat transfer. At low  $Re$ , on the line of symmetry on the XY plane, temperature decreases monotonically from the free surface to the wall. In contrast, we see a shift in this monotonic trend at higher Reynolds numbers ( $> 100$ ). Owing to strong circulation and three dimensionality in the flow in the cross-sectional plane  $X=0$  (YZ), there occurs a temperature inversion at the core of the drop, as one moves from the substrate to the free surface (Figure 18(a)). The related temperature distribution is shown in Figure 18(b). At high  $Re$ , the flow was seen to be unsteady as well.

Figures 19-21 show the local heat transfer coefficient at the wall for various Reynolds numbers in terms of the Nusselt number. The heat transfer rate increases as Reynolds number increases due to stronger mixing. The heat transfer coefficient at the wall is approximately uniformly distributed at the Reynolds numbers considered, except very near the drop periphery. For each contact angle, Figure 22 shows that the Nusselt number is a nearly a linear function of Reynolds number; slight change of slope, i.e. decrease of  $Nu$  is observed around  $Re \sim 50-100$ , which, as stated above, is attributed to the temperature inversion phenomena leading to reduced thermal transport. In addition, Nusselt number is large for a contact angle of  $90^\circ$  and decreases as the contact angle increases.

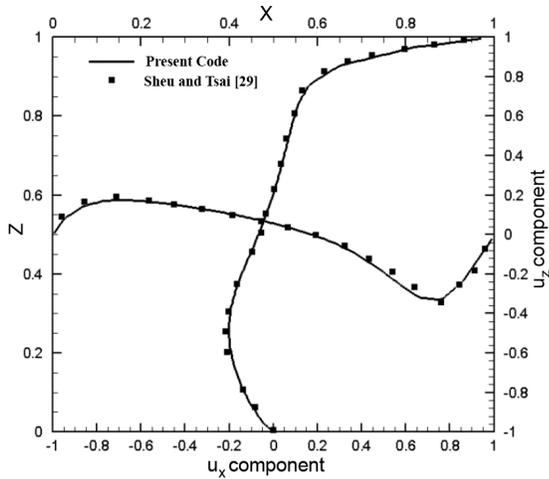


Figure 4: 3D-Lid driven velocity component ( $u_x$ ) variation with respect to the height of lid ( $Z$ ) and velocity component ( $u_z$ ) variation with respect to width of lid ( $X$ ) at the plane of symmetry  $Y=0$ , and compared these with the well know data available in literature[29] at  $Re = 400$ .

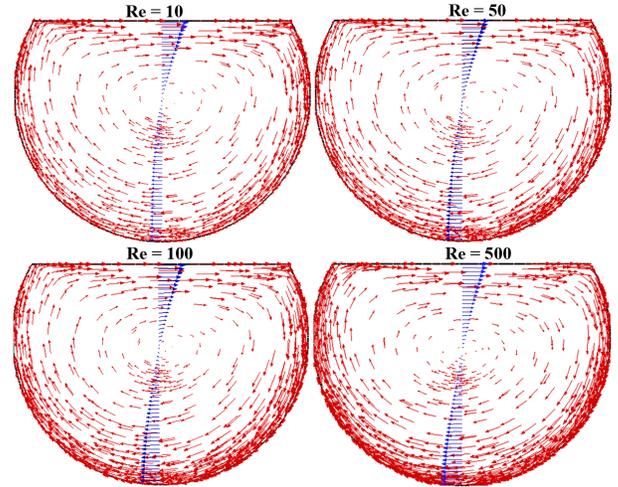


Figure 7:  $u_x$  and  $u_y$  components define the velocity vectors;  $u_x$  profile is shown with respect to the vertical coordinate at  $X=0$  for a drop whose contact angle is  $120^\circ$  and  $Pr = 5.8$ .

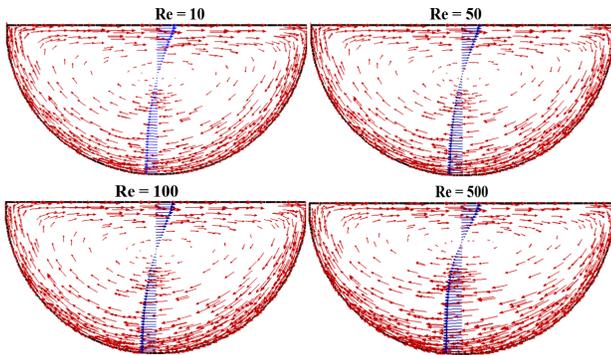


Figure 5:  $u_x$  and  $u_y$  components define the velocity vectors (red color);  $u_x$  velocity profile is also shown with respect to the vertical coordinate at  $X=0$  in the frontal plane ( $Z=0$ ) of the drop whose contact angle is  $90^\circ$  and  $Pr = 5.8$ .

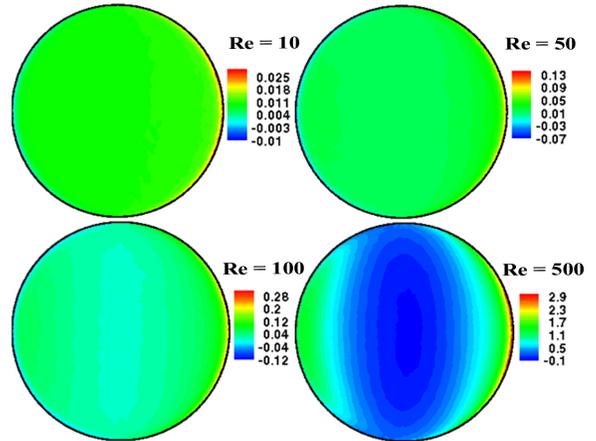


Figure 8: Wall pressure distribution for a drop of contact angle  $90^\circ$  at various  $Re$  and  $Pr = 5.8$ .

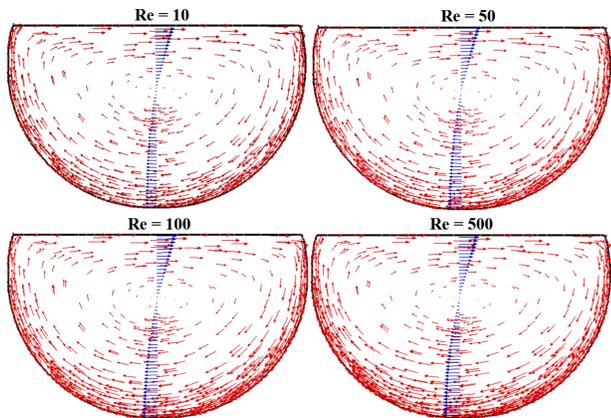


Figure 6:  $u_x$  and  $u_y$  components define the velocity vectors (red color);  $u_x$  velocity profile is shown with respect to the vertical coordinate at  $X=0$  in the frontal plane ( $Z=0$ ) of the drop whose contact angle is  $105^\circ$  and  $Pr = 5.8$ .

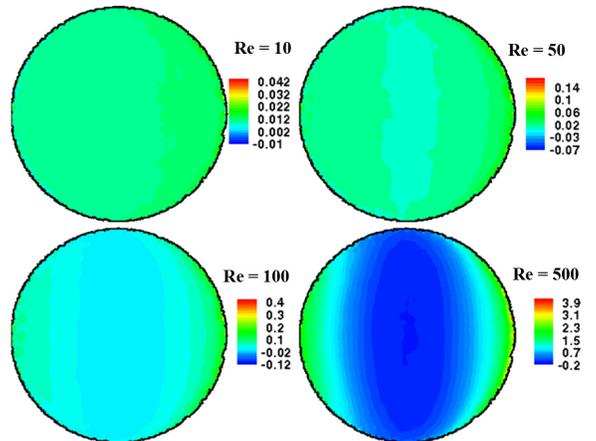


Figure 9: Wall pressure distribution for a drop of contact angle  $105^\circ$  at various  $Re$  and  $Pr = 5.8$ .

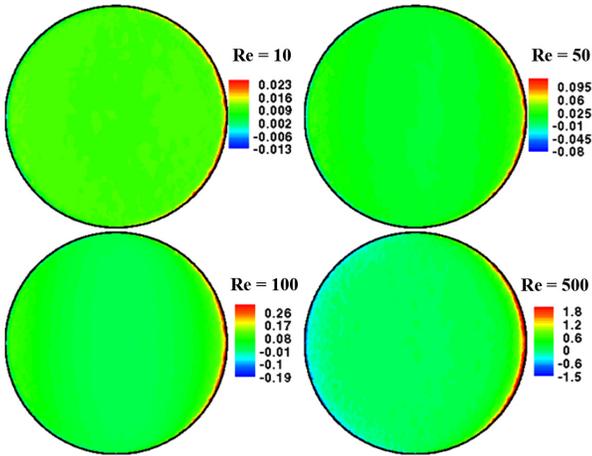


Figure 10: Wall pressure distribution for a drop of contact angle 120° at various Re and Pr = 5.8.

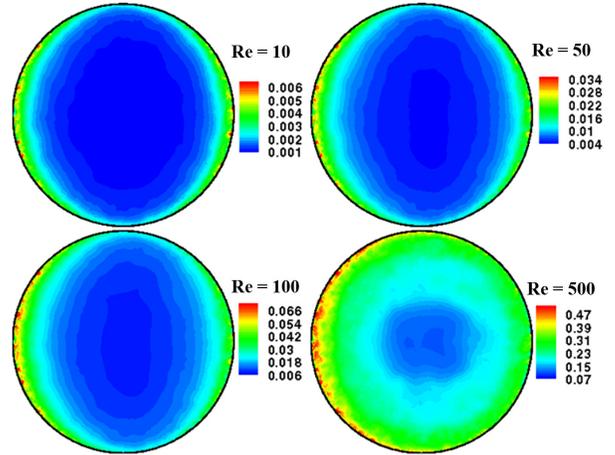


Figure 13: Wall shear stress distribution for a drop of contact angle 120° at various Re and Pr = 5.8.

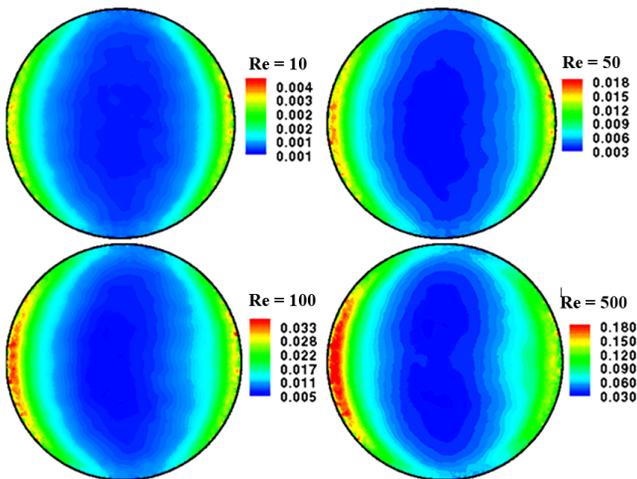


Figure 11: Wall shear stress distribution for a drop of contact angle 90° at various Re and Pr = 5.8.

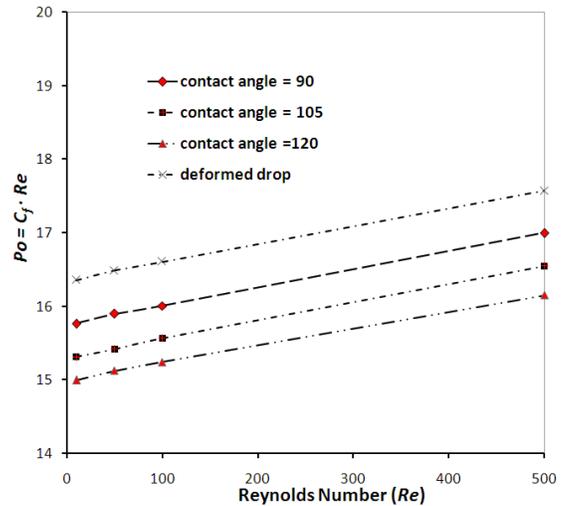


Figure 14: Poiseuille number ( $Po = C_f \times Re$ ) versus Re at Pr = 5.8 for various contact angles and deformed drop sliding underneath an inclined surface.

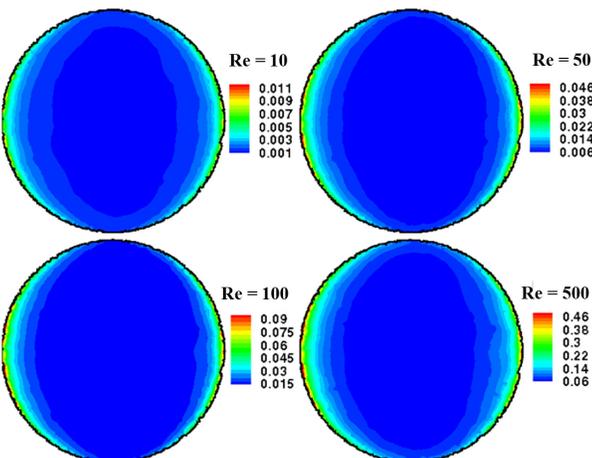


Figure 12: Wall shear stress distribution for a drop of contact angle 105° at various Re and Pr = 5.8.

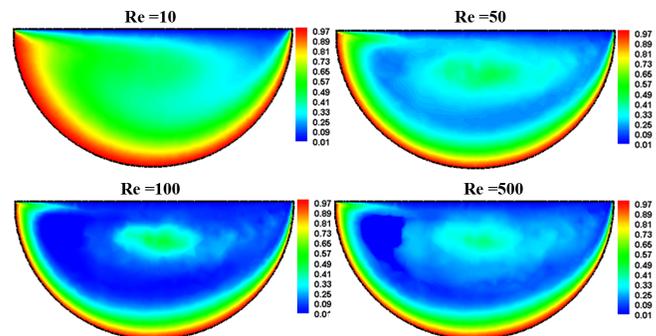


Figure 15: Non-dimensional temperature contours in the frontal plane ( $Z=0$ ) of the drop of contact angle 105° for various Re and Pr = 5.8. The highest temperature is at the free surface ( $= 1$ ) and the lowest temperature at the wall ( $= 0$ ).

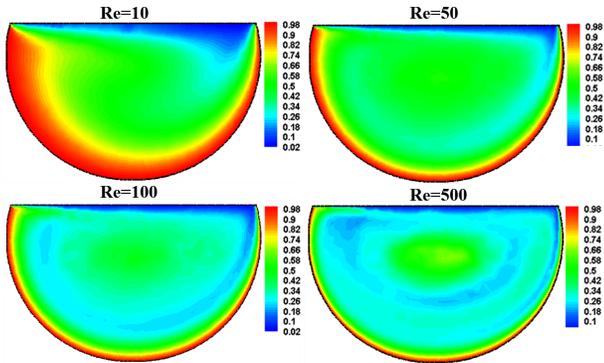


Figure 16: Non-dimensional temperature contours in the frontal plane ( $Z=0$ ) of the drop of contact angle  $105^\circ$  for various  $Re$  and  $Pr = 5.8$ . The highest temperature is at the free surface ( $= 1$ ) and the lowest temperature at the wall ( $= 0$ ).

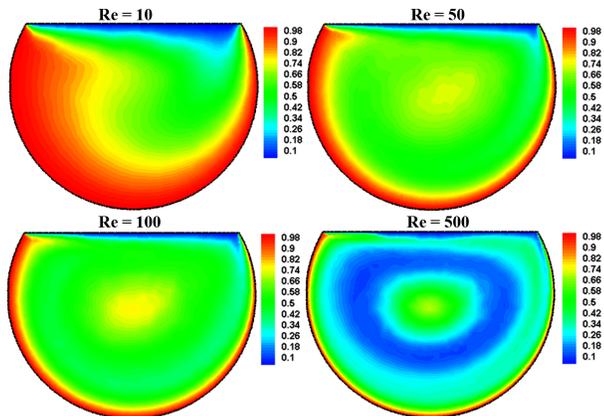


Figure 17: Non-dimensional temperature contours in the frontal plane ( $Z=0$ ) of the drop of contact angle  $120^\circ$  for various  $Re$  and  $Pr = 5.8$ . The highest temperature is at the free surface ( $= 1$ ) and the lowest temperature at the wall ( $= 0$ ).

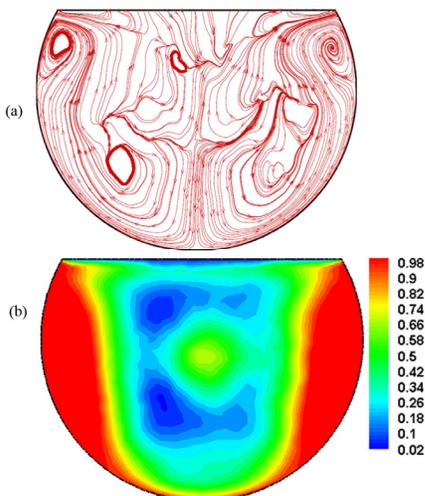


Figure 18: (a) Streamlines and (b) temperature distribution at the  $X=0$  plane for a drop of contact angle  $120^\circ$  at a  $Pr = 5.8$  and  $Re = 500$ .

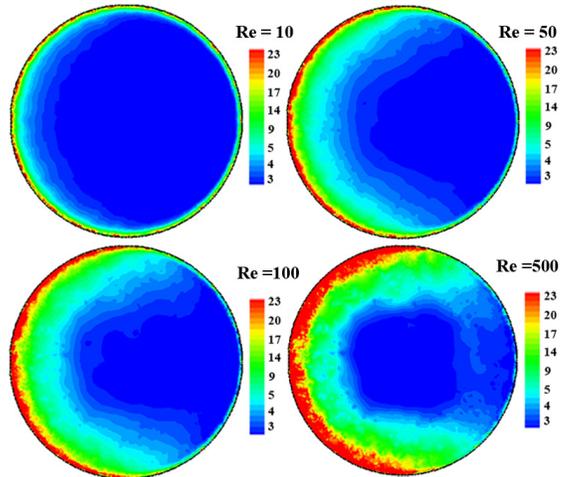


Figure 19: Nusselt number variation for a drop of contact angle  $90^\circ$  at various  $Re$  and  $Pr = 5.8$ .

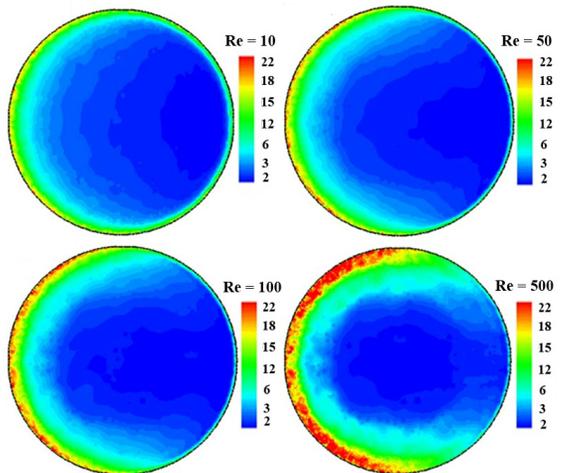


Figure 20: Nusselt number variation for a drop of contact angle  $105^\circ$  at various  $Re$  and  $Pr = 5.8$ .

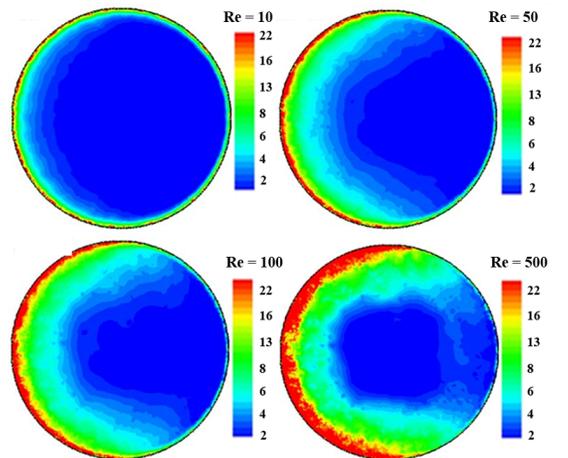
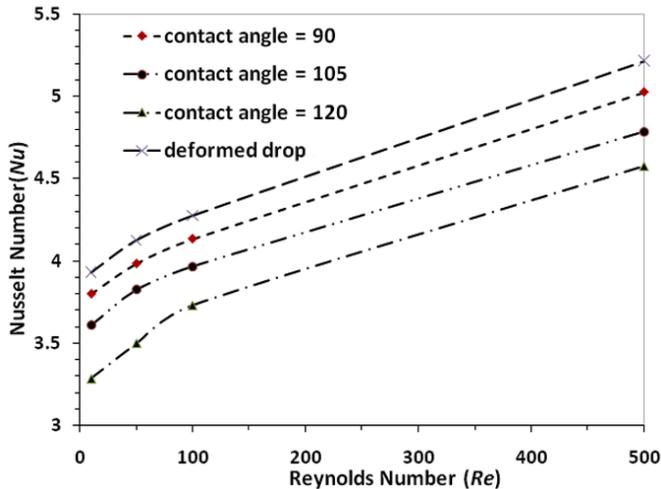


Figure 21: Nusselt number variation for a drop of contact angle  $120^\circ$  at various  $Re$  and  $Pr = 5.8$ .



**Figure 22: Nusselt number (Nu) versus Reynolds number (Re) at Prandtl number (Pr) = 5.8 for various contact angles and a deformed drop sliding underneath an inclined surface.**

## CONCLUSIONS

The present three dimensional numerical investigation reports fluid flow and temperature distribution inside a pendant liquid drop sliding on an inclined surface at a Prandtl number of 5.8 and various Reynolds numbers. The shape of the drop is defined by its contact angle. An attempt has been made to correlate the effective average shear stress, i.e. Poiseuille number and the net heat transfer, i.e. Nusselt number, at the droplet base, with respect to the drop Reynolds number and its shape. Such information is vital for estimating leaching rates of droplets growing and sliding on a substrate during dropwise condensation. Estimation of the leaching rates is important in many engineering applications, for example (a) estimation of life cycle of a heat exchanger textured by promoter layers and (b) estimation of substrate life on which heavy liquid metals are being deposited under closed vacuum conditions. If the ensemble droplet population under dynamic dropwise condensation process is independently known either by experiments or by simulation, the relations proposed in this work for single drops can be used to find the effective shear stress and heat transfer coefficient on the entire physically/chemically textured condensing surface.

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