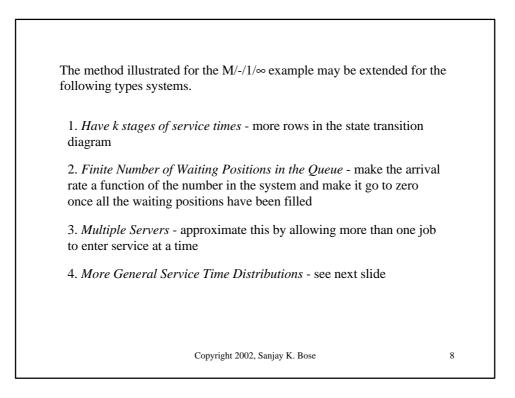
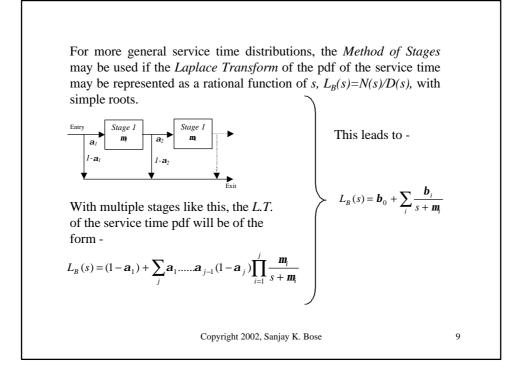
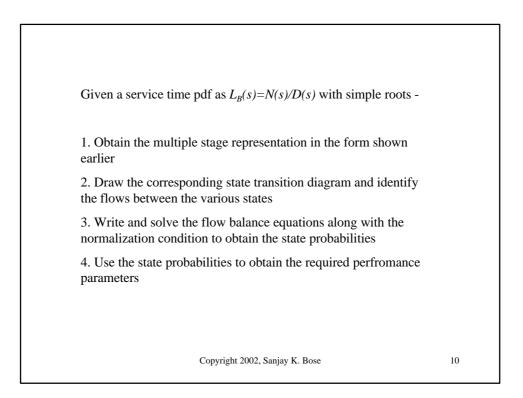
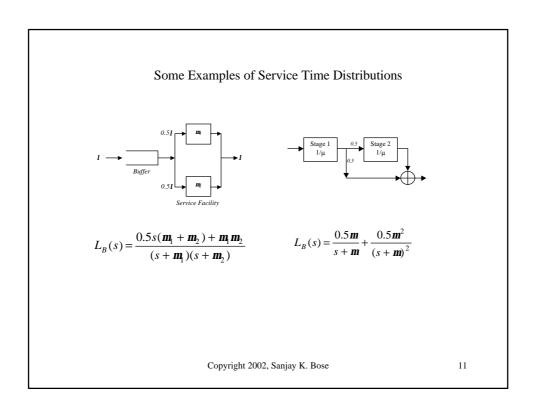


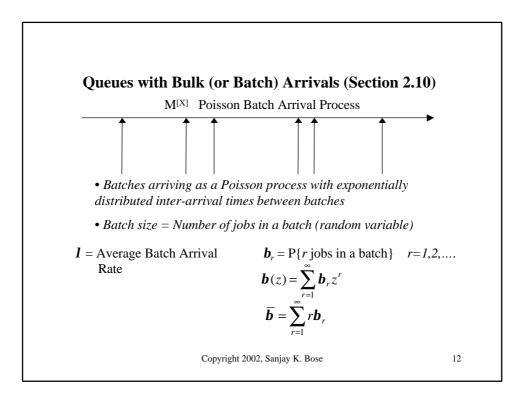
 $I p_{00} = m_2 p_{12}$ $(\boldsymbol{l} + \boldsymbol{m}_1) p_{11} = \boldsymbol{l} p_{00} + \boldsymbol{m}_2 p_{22}$ Balance Equations for $(\mathbf{l} + \mathbf{m}_2) p_{12} = \mathbf{m}_1 p_{11}$ (2.38) the System $(\mathbf{l} + \mathbf{m}_1) p_{21} = \mathbf{l} p_{11} + \mathbf{m}_2 p_{32}$ $(\mathbf{l} + \mathbf{m}_2)p_{22} = \mathbf{l}p_{12} + \mathbf{m}_1p_{21}$ etc..... These Balance Equations may be solved along with the appropriate Normalization Condition to obtain the state probabilities of the system. Once these are known, performance parameters of the queue may be appropriately evaluated. Copyright 2002, Sanjay K. Bose 7

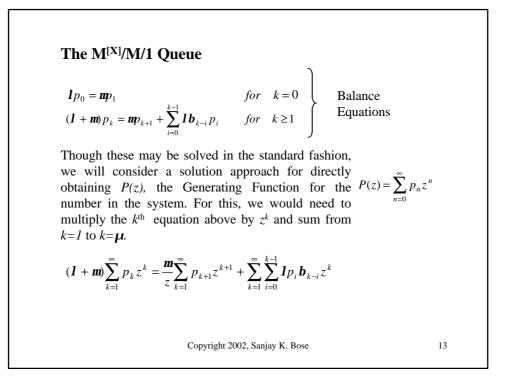












Simplifying, we get $(l + m)[P(z) - p_0] = \frac{m}{z}[P(z) - p_0 - p_1 z] + lP(z)b(z)$ $P(z) = \frac{mp_0(1 - z)}{m(1 - z) - lz[1 - b(z)]}$ Define $r = \frac{l\overline{b}}{m}$ as the offered traffic Note that, P(1)=1 is effectively the same as the Normalization Condition. Using this, we get $p_0 = 1 - r$ $P(z) = \frac{m(1-r)(1-z)}{m(1-z) - Iz[1-b(z)]}$ (2.42)Therefore We can invert P(z) or expand it as a power series in z^i i=0,1,... to get the state probability distribution. The mean number N in the system may be directly calculated from P(z) as - $N = \frac{dP(z)}{dz}\Big|_{z=0} = \frac{\mathbf{r}(\overline{\mathbf{b}} + \overline{\mathbf{b}^2})}{2(1-\mathbf{r})}$ (2.43)Copyright 2002, Sanjay K. Bose

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