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# Airborne Altimetric LiDAR Simulator: An Education Tool

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**Bharat Lohani, PhD**

[R K Mishra, Parameshwar Reddy, Rajneesh Singh, Nishant Agrawal and Nitish Agrawal](#)

Department of Civil Engineering  
IIT Kanpur Kanpur INDIA



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*Are data available?*

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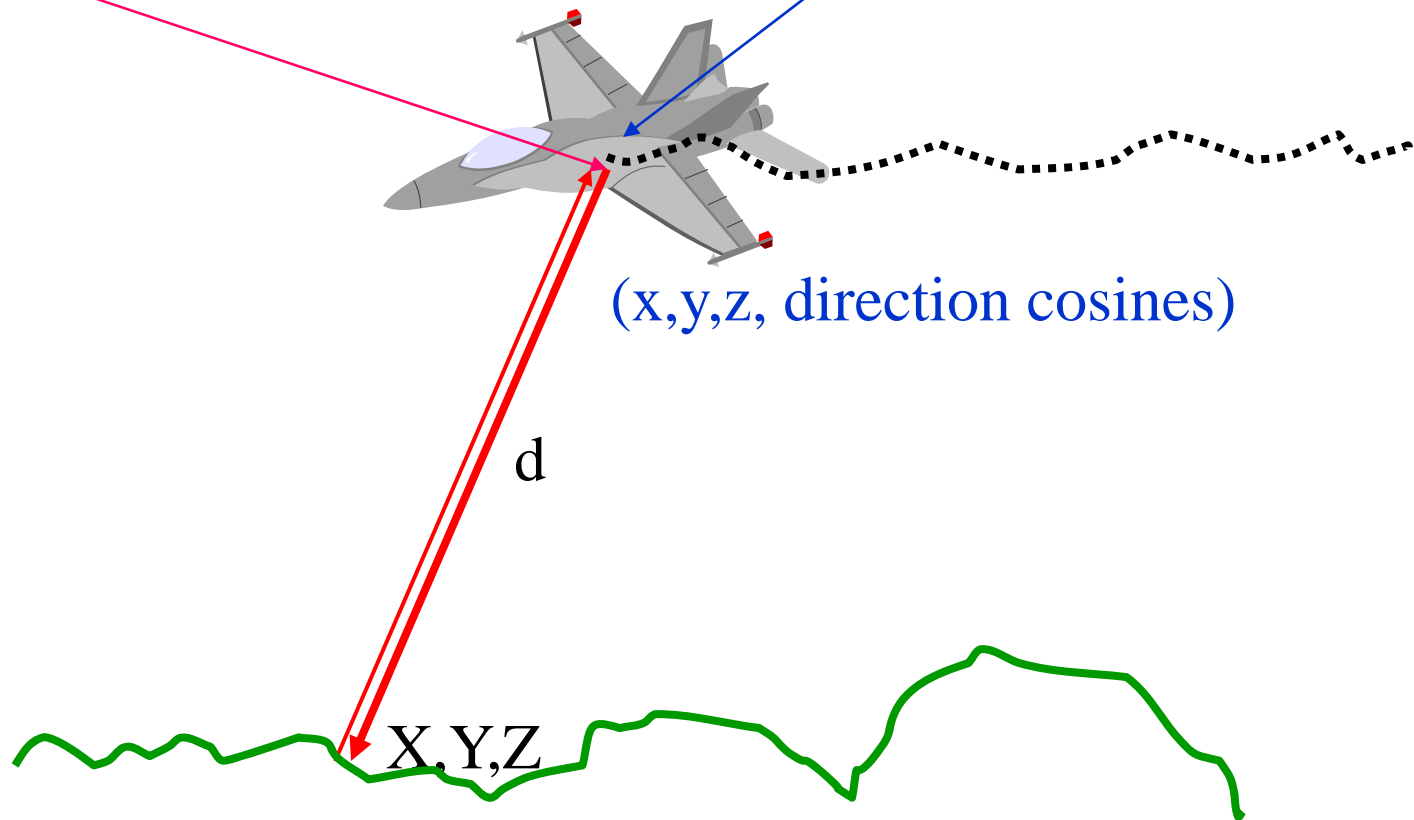
# Outline

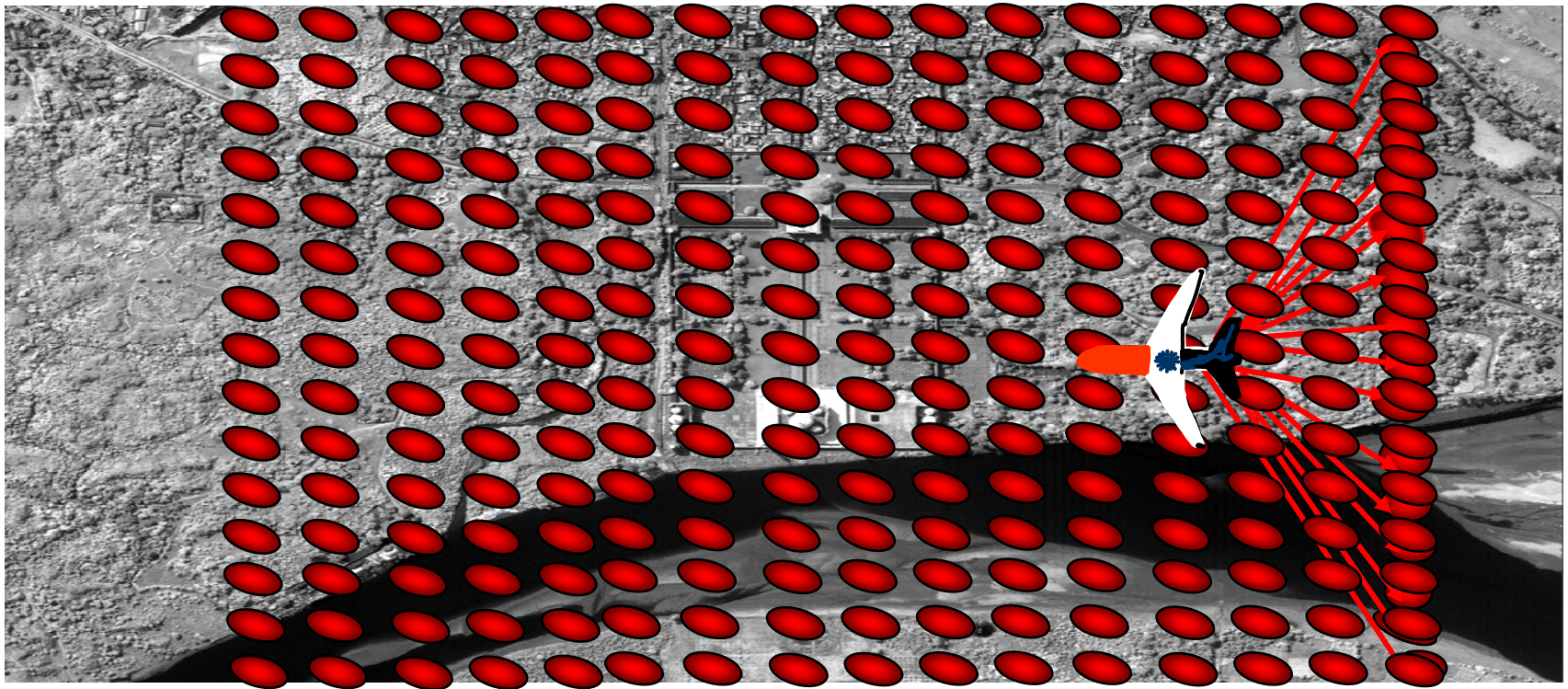
- What is Airborne Altimetric LiDAR Simulator?
  - What should an ideal simulator do?
  - Development of simulator
  - Simulated data and results
  - Applications of simulator
-

# Principle of LiDAR

Laser transmitter

INS, GPS, Scanner





Credit space Imaging for background image

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# What is an airborne altimetric simulator?

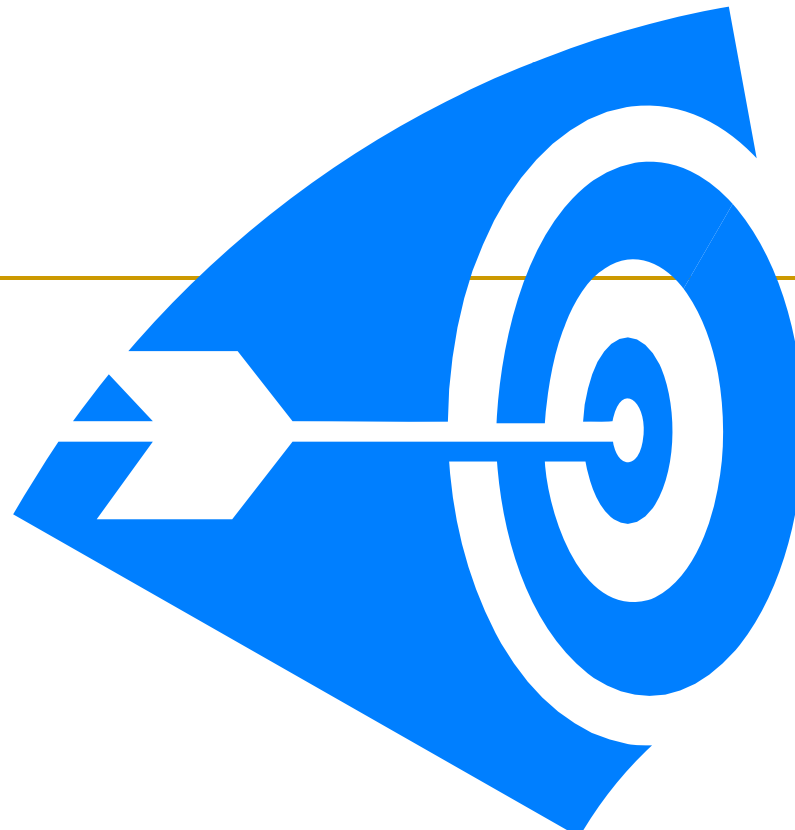
- **Definition:**

- A computer based system which generates LiDAR data similar to an actual sensor for user specified sensor and trajectory over a given terrain.
  - Based on mathematical models, algorithms and programming language.
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# Design consideration for simulator

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# Should be . . .

- User friendly
- Wider distribution
- Help or tutorial





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# Can simulate . . .

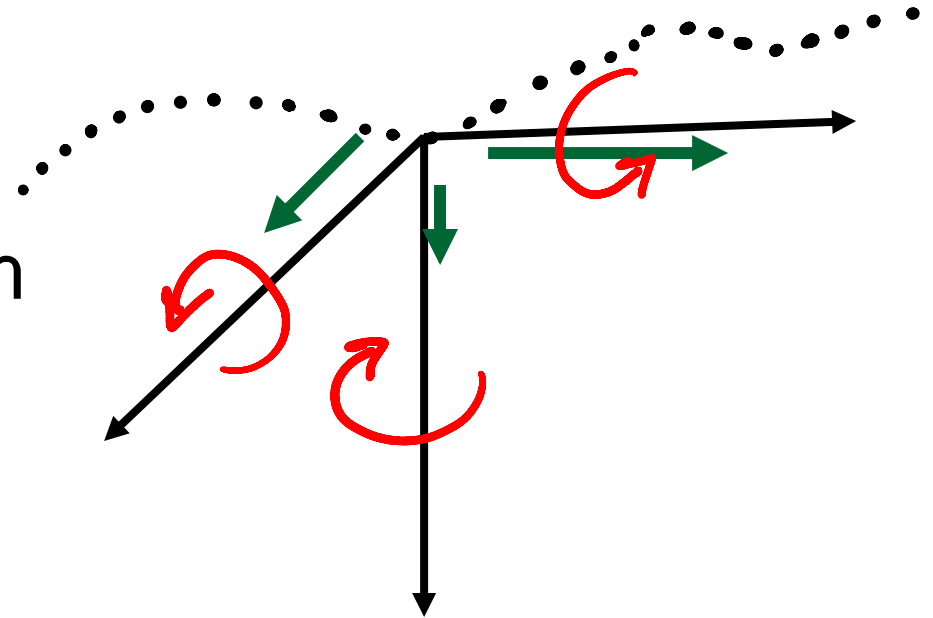
- Generic sensor
- Specific sensors
  - ALTM
  - ALS
  - And others...



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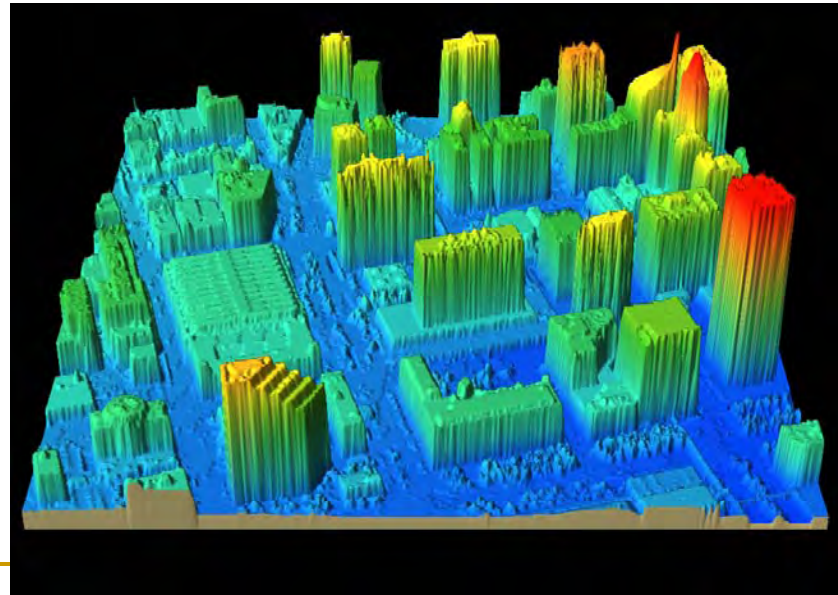
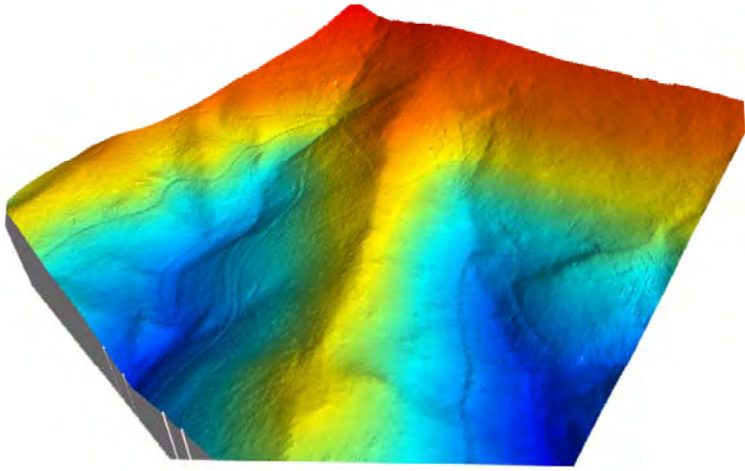
# Should simulate trajectory as in a normal flight

- 6 degrees of freedom



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# Should simulate earthlike surfaces



Source: Optech Inc.

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Also...

- Possibility of error introduction
  - Output data in common formats
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# Development of simulator

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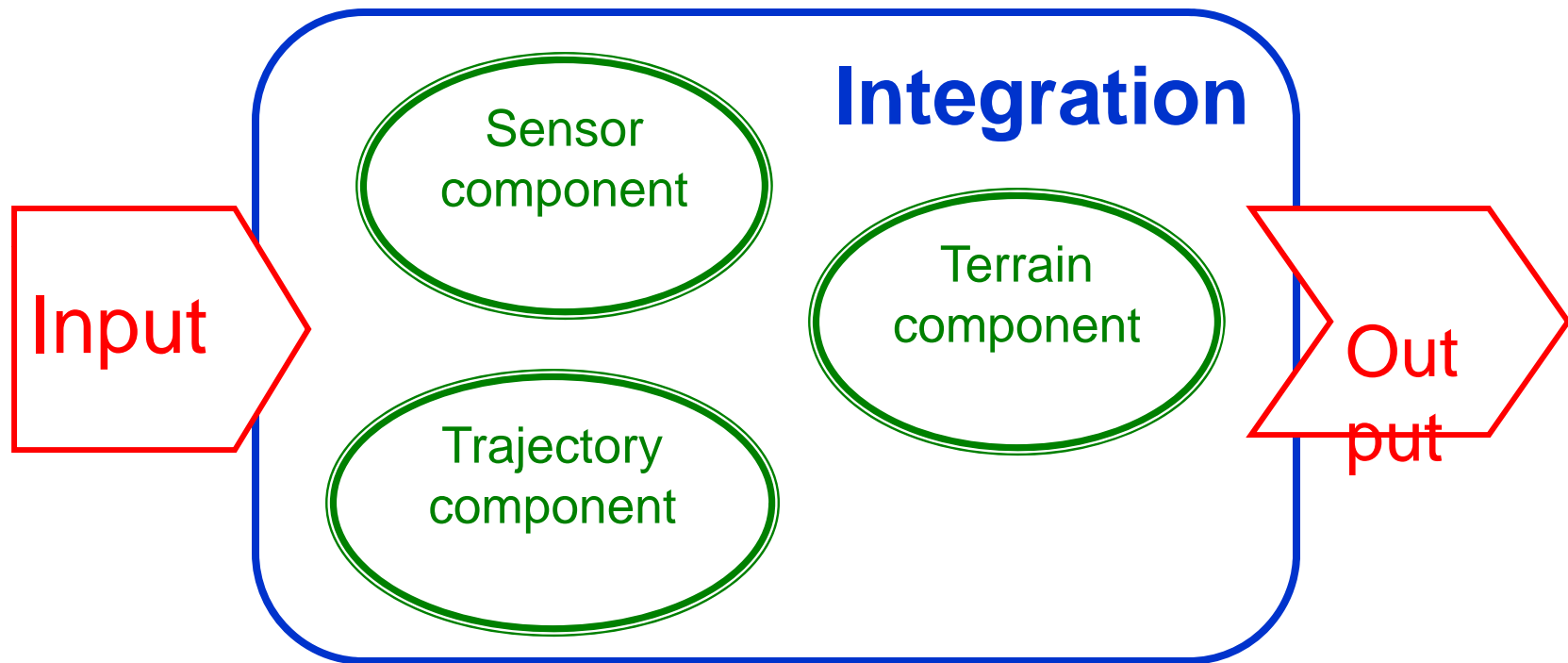
# Programming language

- JAVA

- GUI
  - Graphical and numerical programming
  - Platform independent
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# System components



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# Trajectory component

- Location
- Attitude





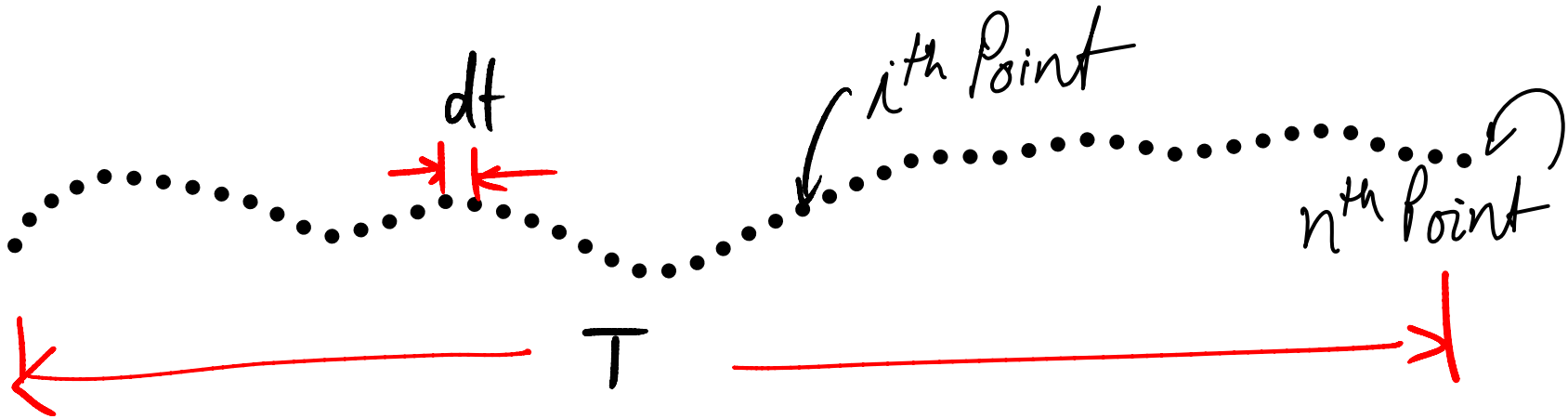
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# Location

- Location: coordinates of laser head at each firing of pulse
  - Location depends on Instantaneous accelerations
  - Instantaneous **accelerations should be simulated** as in a normal flight: pseudo-random simulation
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# Acceleration simulation

$$a_X^i = \sum_{j=1}^J A_j \sin\left(B_j \left(\frac{2\pi}{T} (id_t)\right)\right) + \sum_{k=1}^K C_k \cos\left(D_k \left(\frac{2\pi}{T} (id_t)\right)\right) + m(id_t)$$



$$dt = \frac{1}{F}$$

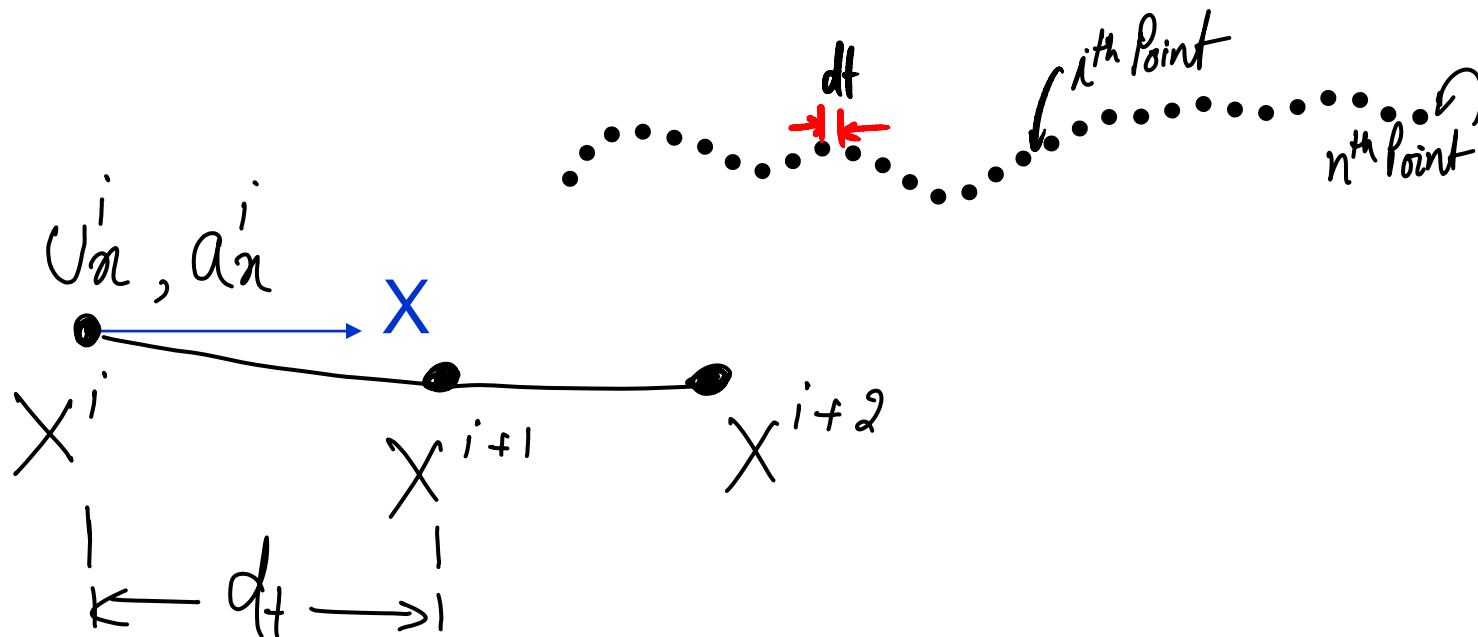
F = Firing frequency

J, K, A, B, C, D and m governing parameters

$$T = n \cdot dt$$

# Location simulation

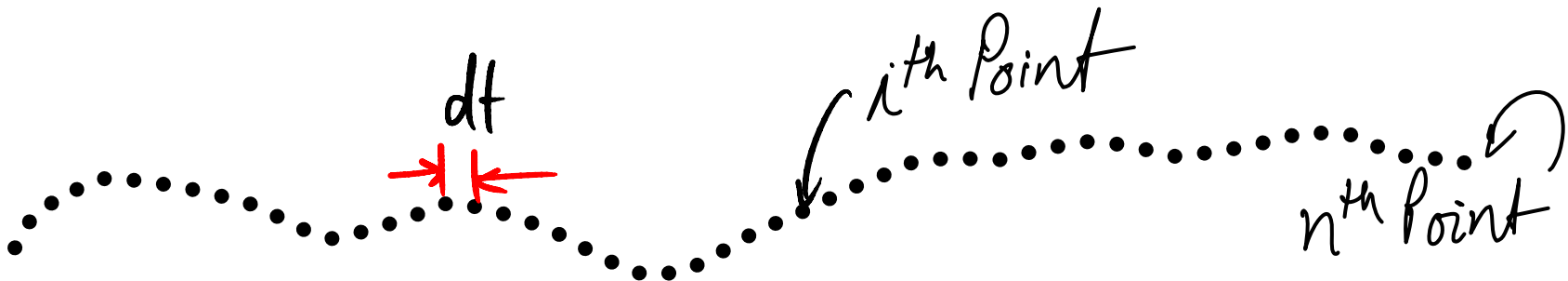
$$X^{i+1} = X^i + u_x^i d_t + \frac{1}{2} a_x^i d_t^2$$



$u_x$  = Velocity in direction flight i.e. X axis

# Attitude (Roll, Pitch, Yaw) simulation

$$R^i = \sum_{j=1}^J A_j \sin\left(B_j \left(\frac{2\pi}{T}(id_t)\right)\right) + \sum_{k=1}^K C_k \cos\left(D_k \left(\frac{2\pi}{T}(id_t)\right)\right) + m(id_t)$$



# Sensor component

## ■ Replicate sensor function

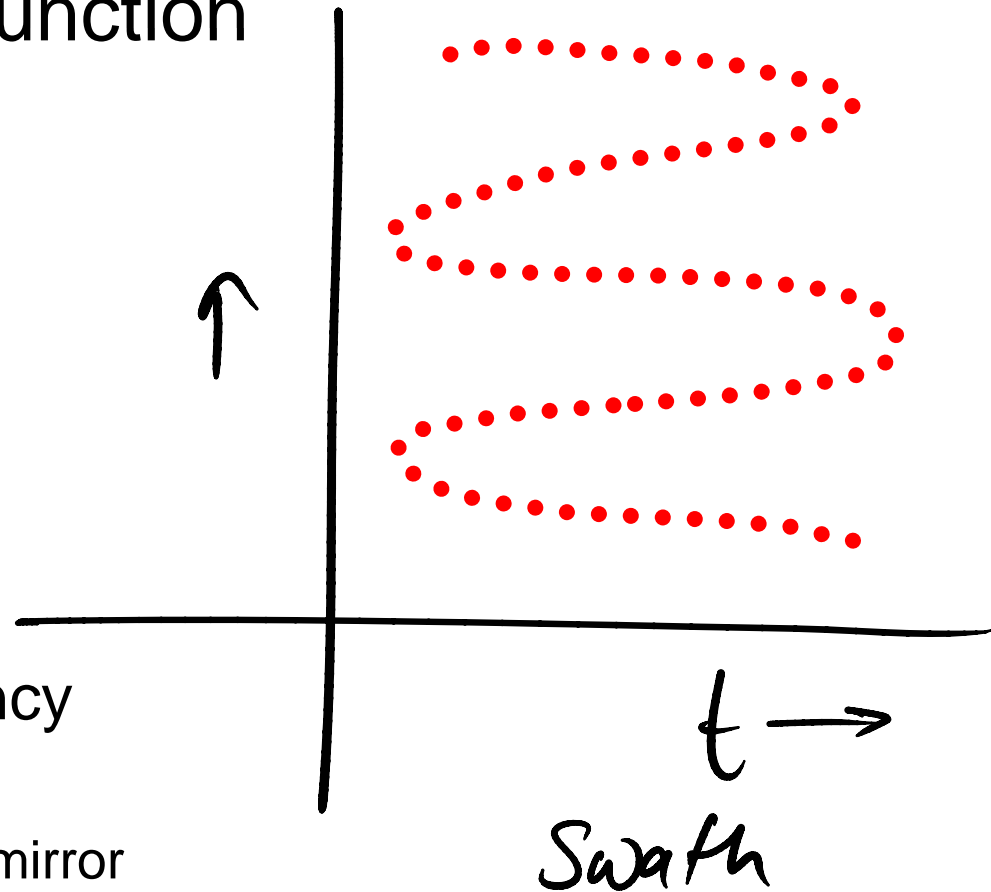
$$\theta = \frac{\frac{S}{2} \sin\left(t \sqrt{\frac{k}{R}}\right)}{\sin\left(\frac{1}{4f} \sqrt{\frac{k}{R}}\right)}$$

$S$  is full scan angle

$f$  is the scanning frequency

$k$  is driving acceleration

$R$  is radius of the scanning mirror



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# Terrain component

- Modeling surfaces: earthlike
  - Vector approach

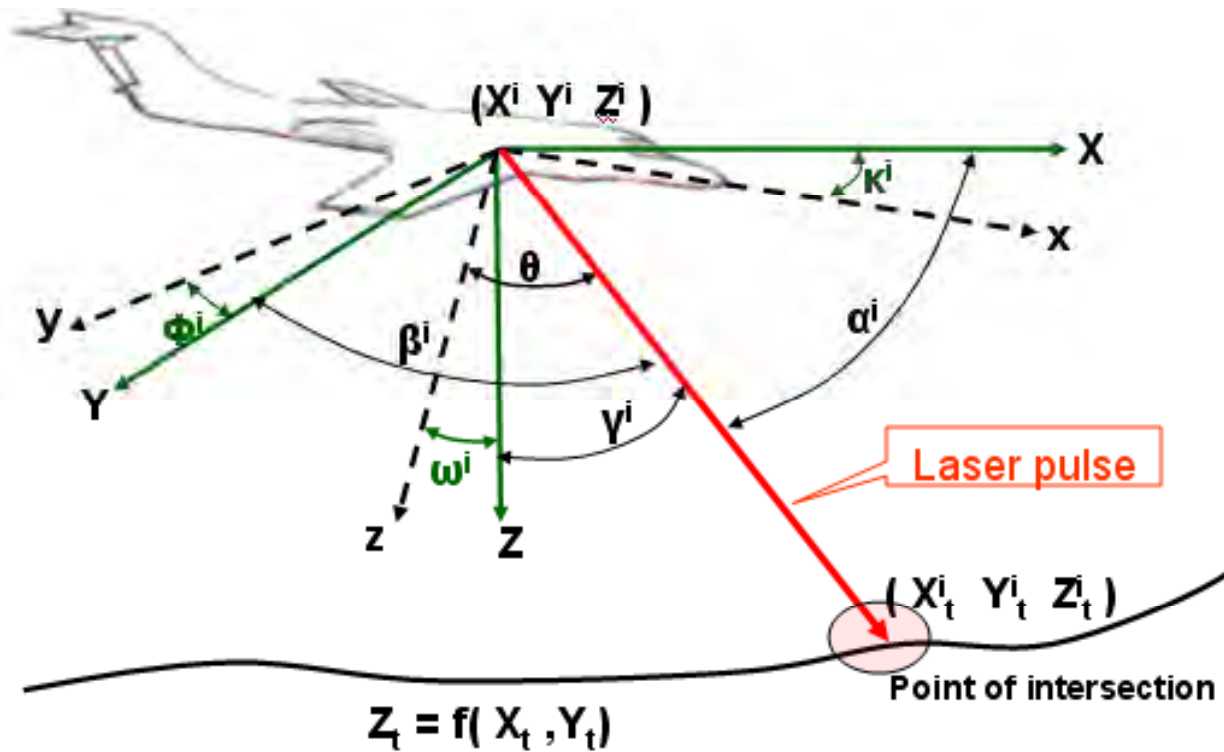
$$Z = AX + BY + C$$

$$Z = A[\sin(X / B) - \sin(XY / C)] + D$$

$$Z = A[\sin(X / Y) - \sin(XY / B)] + C$$

- Raster approach
-

# Integration of components



Laser vector  $\frac{X - X^i}{a^i} = \frac{Y - Y^i}{b^i} = \frac{Z - Z^i}{c^i}$

Solving the intersection

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# Error introduction in simulated data

$$X_T^i = X_t^i + N(\mu_X, \sigma_X^2)$$

  
Known from field

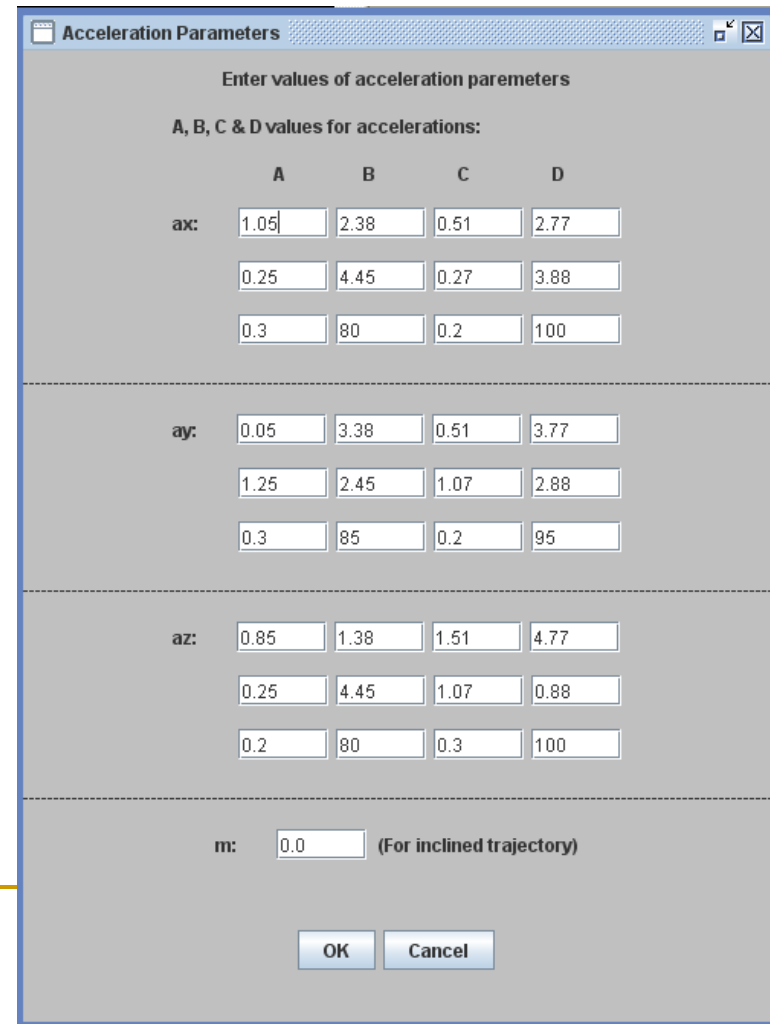
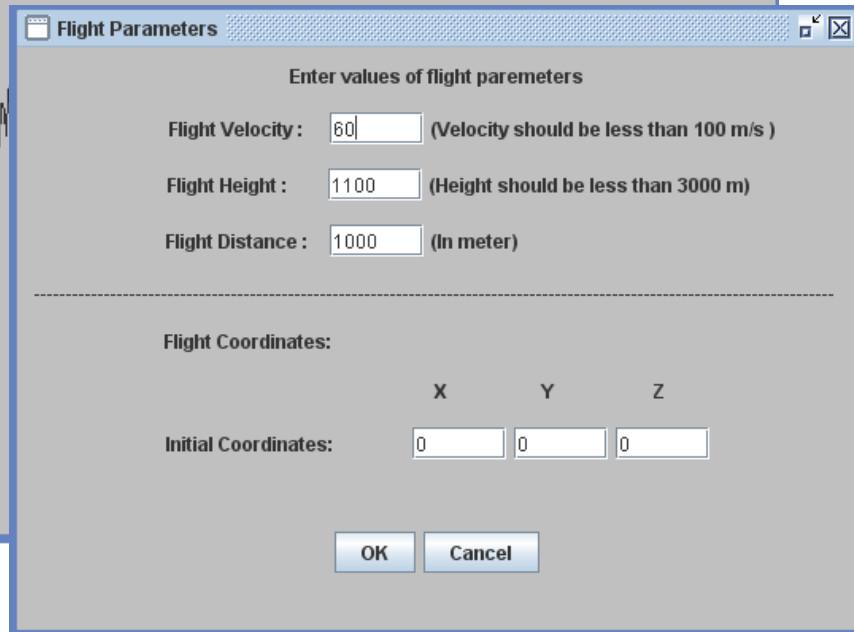
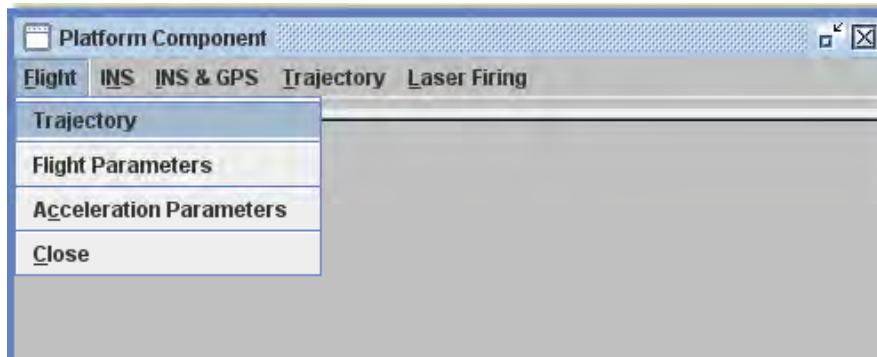




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# Software development

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## Sensor component.

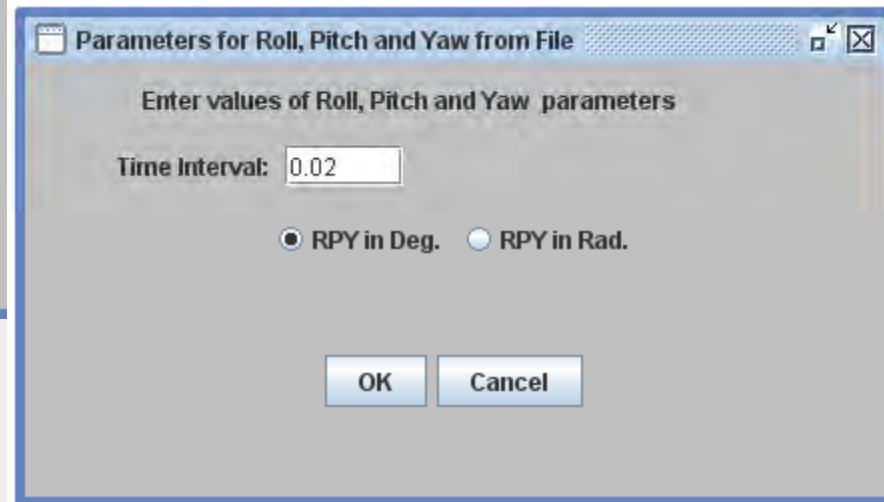
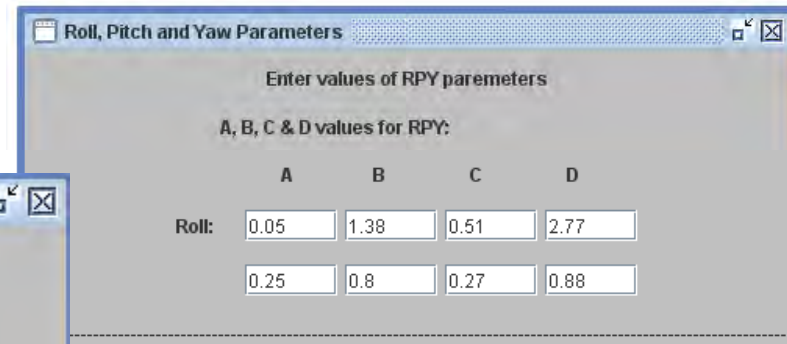
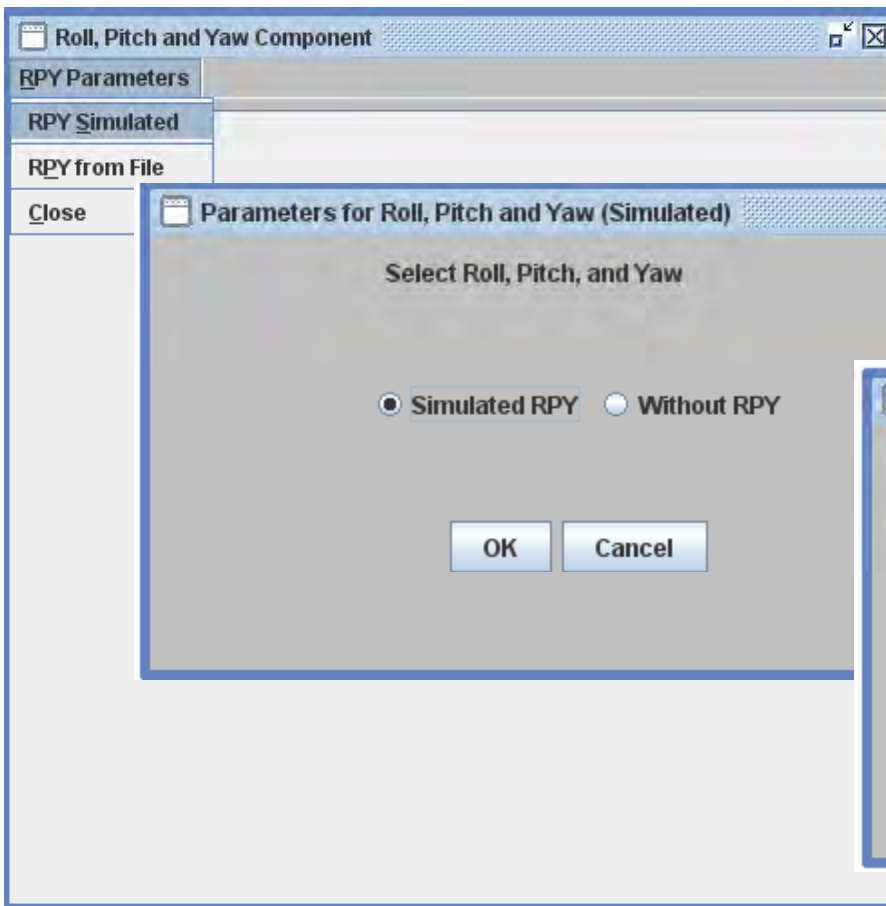


The 'Sensor Component' dialog box is open, titled 'Sensor Component'. It contains the text 'Enter values of sensor parameters' and four input fields with their respective units and constraints:

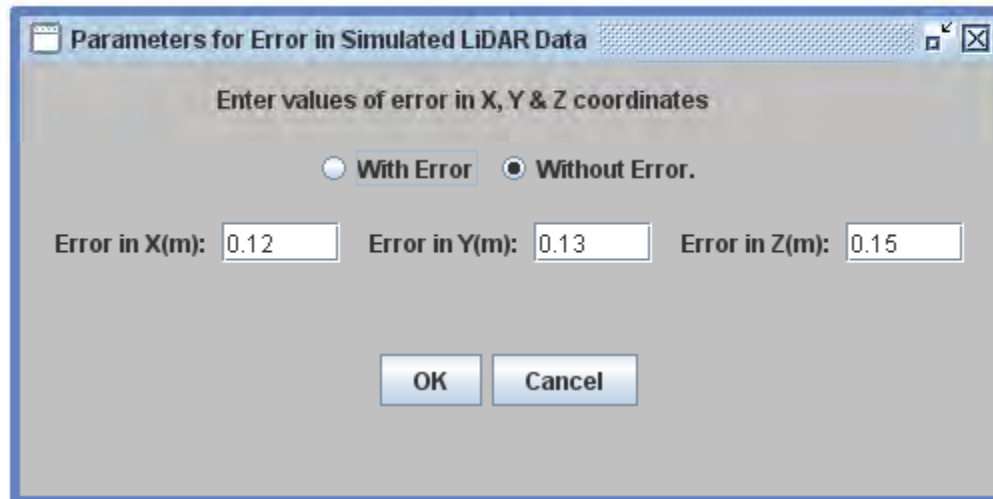
- Radius of Mirror :  (Radius should be less than 0.05 m)
- Firing Frequency :  (Laser firing frequency should be less than 83 khz)
- Scan Frequency :  (Laser scan frequency should be less than 70 hz)
- Scan Angle :  (Laser scan angle should be less than 50 degree)

At the bottom of the dialog are 'OK' and 'Cancel' buttons.

# Simulation of Roll, Pitch and Yaw.



# Error Simulation.



# Surface component.



**Surface Component**

Surface

Create Surface

Close

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**Mathematical Surfaces**

Surface Type: Simple Surface

Simple Surfaces:  $Ax+By+Cz+D=0$  Complex Surfaces:  $Z=A[\sin(X/B)-\sin(XY/C)]-D$

Enter values of A, B and C for the surfaces. D is equal to the height of aeroplane.

A: 0 B: 0 C: 1

OK Cancel

**Mathematical Surfaces**

Surface Type: Complex Surface

Simple Surfaces:  $Ax+By+Cz+D=0$  Complex Surfaces:  $Z=A[\sin(X/B)-\sin(XY/C)]-D$

Enter values of A, B and C for the surfaces. D is equal to the height of aeroplane.

A: 1 B: 1.0 C: 90

OK Cancel

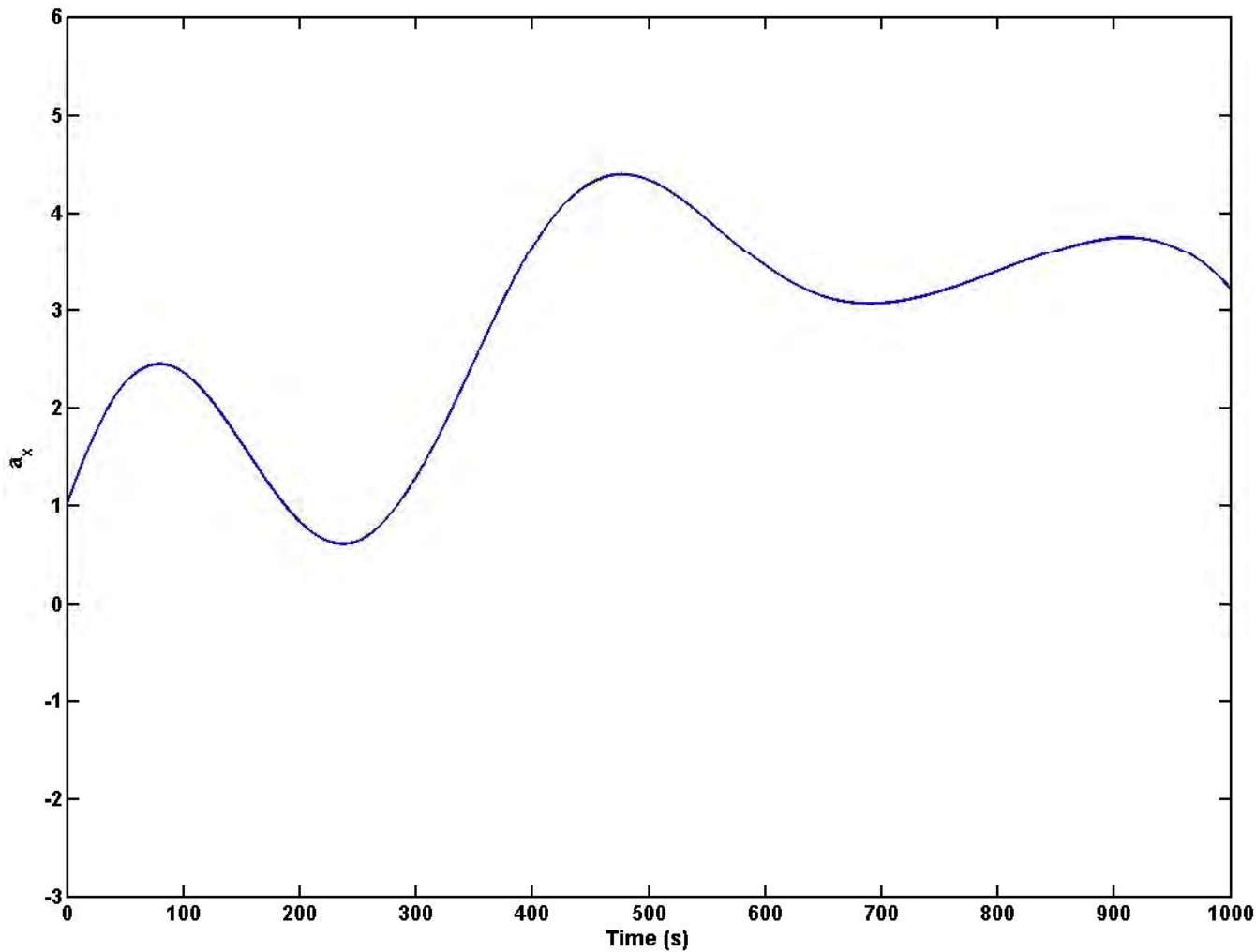
- $Z=A[\sin(X/B)-\sin(XY/C)]-D$
- $Z=A[\cos(X/B)-\sin(XY/C)]-D$
- $Z=A[\sin(X/B)-\cos(XY/C)]-D$
- $Z=A[\cos(X/B)-\cos(XY/C)]-D$
- $Z=A[\sin(X/B)^*\cos(X/B)-\sin(XY/C)]-D$
- $Z=A[\sin(X/B)^*\sin(X/B)-\sin(XY/C)^*\sin(XY/C)]-D$
- $Z=A[\cos(X/B)^*\cos(X/B)-\cos(XY/C)^*\cos(XY/C)]-D$
- $Z=A[\sin(X)-\sin(Y)]-D$

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# Simulated data and results

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$$a_X^i = \sum_{j=1}^J A_j \sin\left(B_j \left(\frac{2\Pi}{T} (id_t)\right)\right) + \sum_{k=1}^K C_k \cos\left(D_k \left(\frac{2\Pi}{T} (id_t)\right)\right) + m(id_t)$$

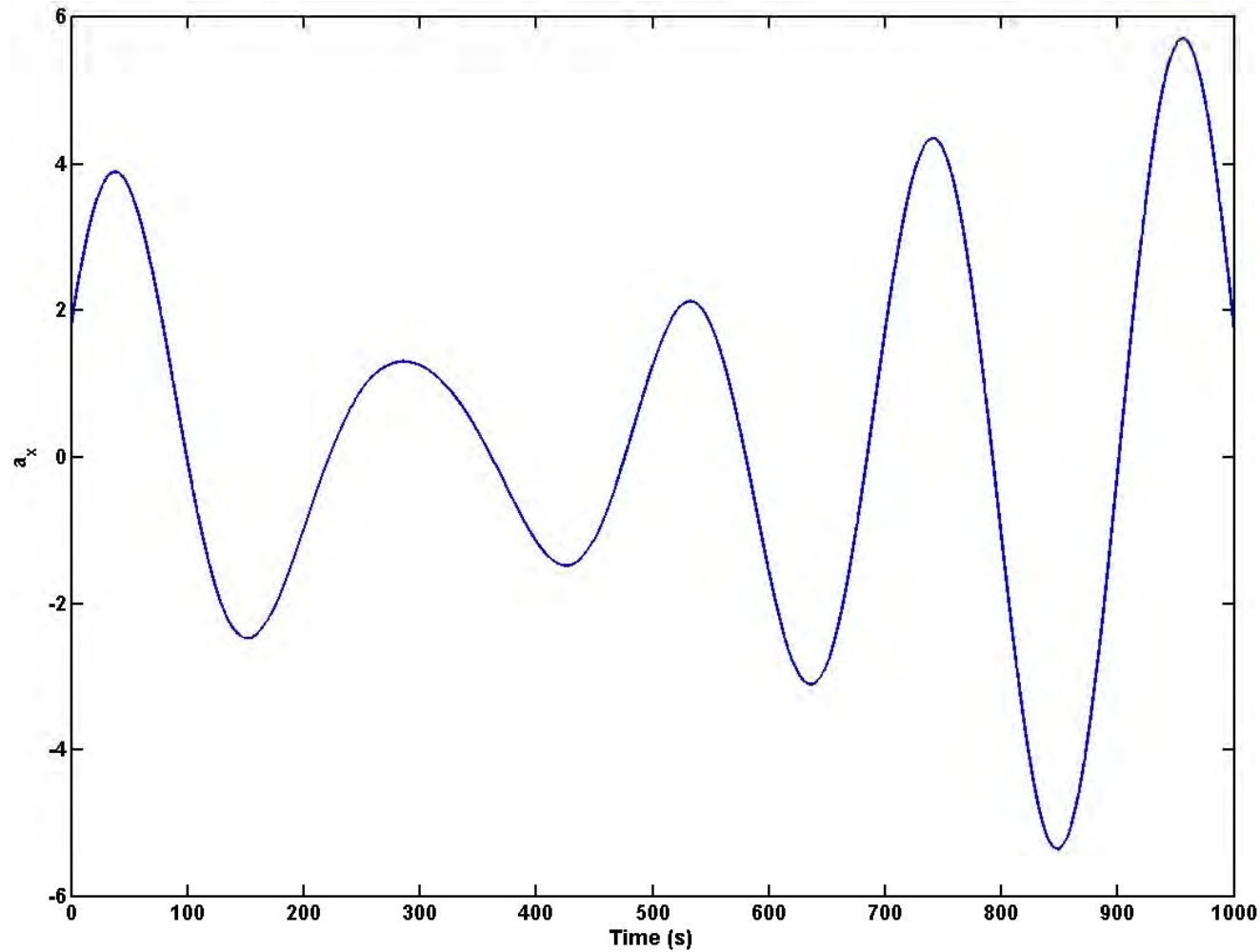


j=2, k=2

$A_1$	3.54
$A_2$	1.65
$B_1$	0.38
$B_2$	2.45
$C_1$	0.51
$C_2$	3.77
$D_1$	2.77
$D_2$	0.88
m	0.0
dt	0.001
T	1000



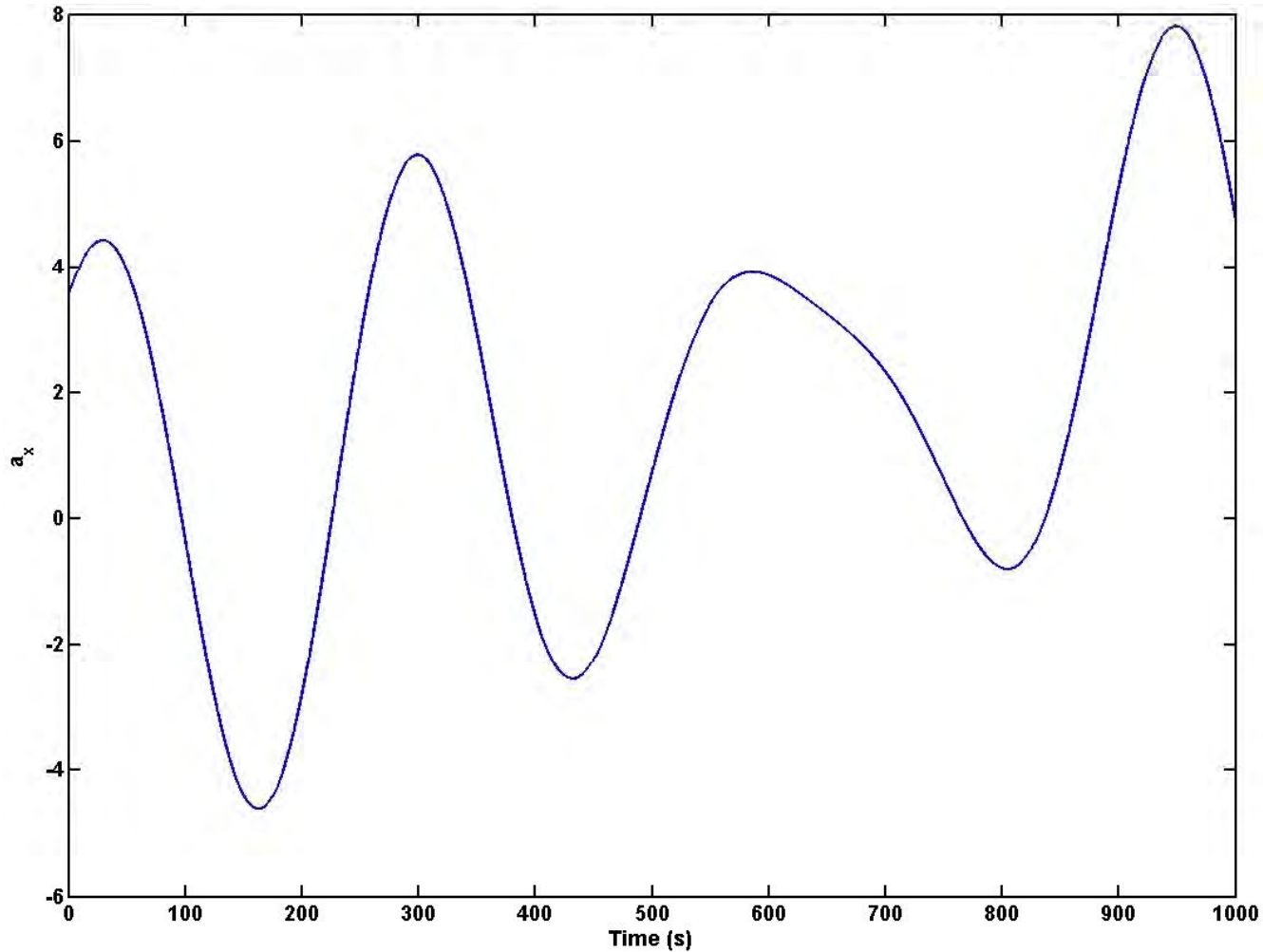
$$a_x^i = \sum_{j=1}^J A_j \sin\left(B_j \left(\frac{2\Pi}{T} (id_t)\right)\right) + \sum_{k=1}^K C_k \cos\left(D_k \left(\frac{2\Pi}{T} (id_t)\right)\right) + m(id_t)$$



j=2, k=2

$A_1$	0.68
$A_2$	3.25
$B_1$	3.38
$B_2$	4.45
$C_1$	0.89
$C_2$	2.54
$D_1$	5.23
$D_2$	1.34
m	0.0
dt	0.001
T	1000

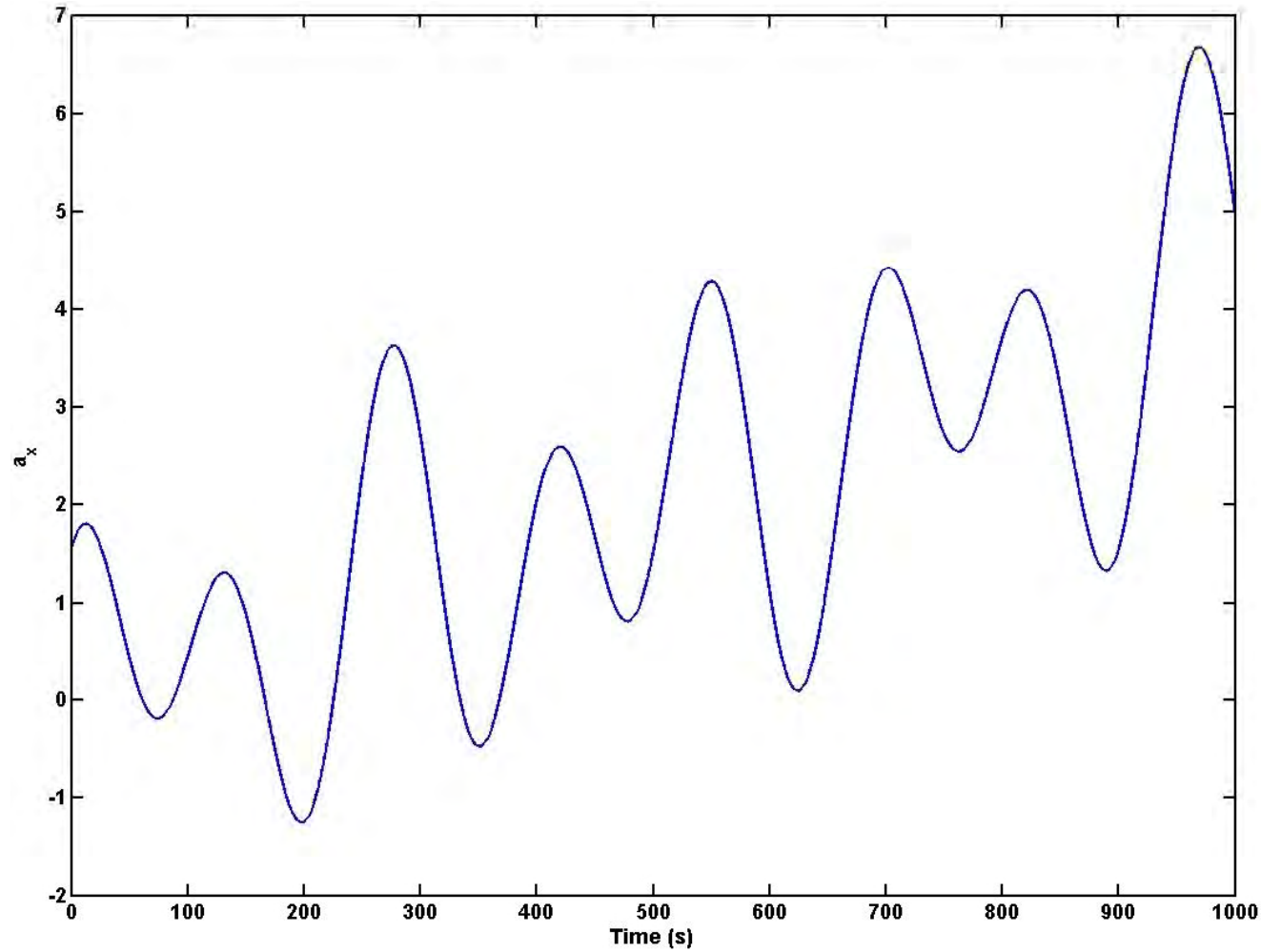
$$a_X^i = \sum_{j=1}^J A_j \sin\left(B_j \left(\frac{2\Pi}{T} (id_t)\right)\right) + \sum_{k=1}^K C_k \cos\left(D_k \left(\frac{2\Pi}{T} (id_t)\right)\right) + m(id_t)$$



j=2, k=2

$A_1$	1.78
$A_2$	0.25
$B_1$	4.38
$B_2$	2.45
$C_1$	1.78
$C_2$	1.24
$D_1$	3.23
$D_2$	2.34
m	0.003
dt	0.001
T	1000

$$a_X^i = \sum_{j=1}^J A_j \sin\left(B_j \left(\frac{2\Pi}{T} (id_t)\right)\right) + \sum_{k=1}^K C_k \cos\left(D_k \left(\frac{2\Pi}{T} (id_t)\right)\right) + m(id_t)$$

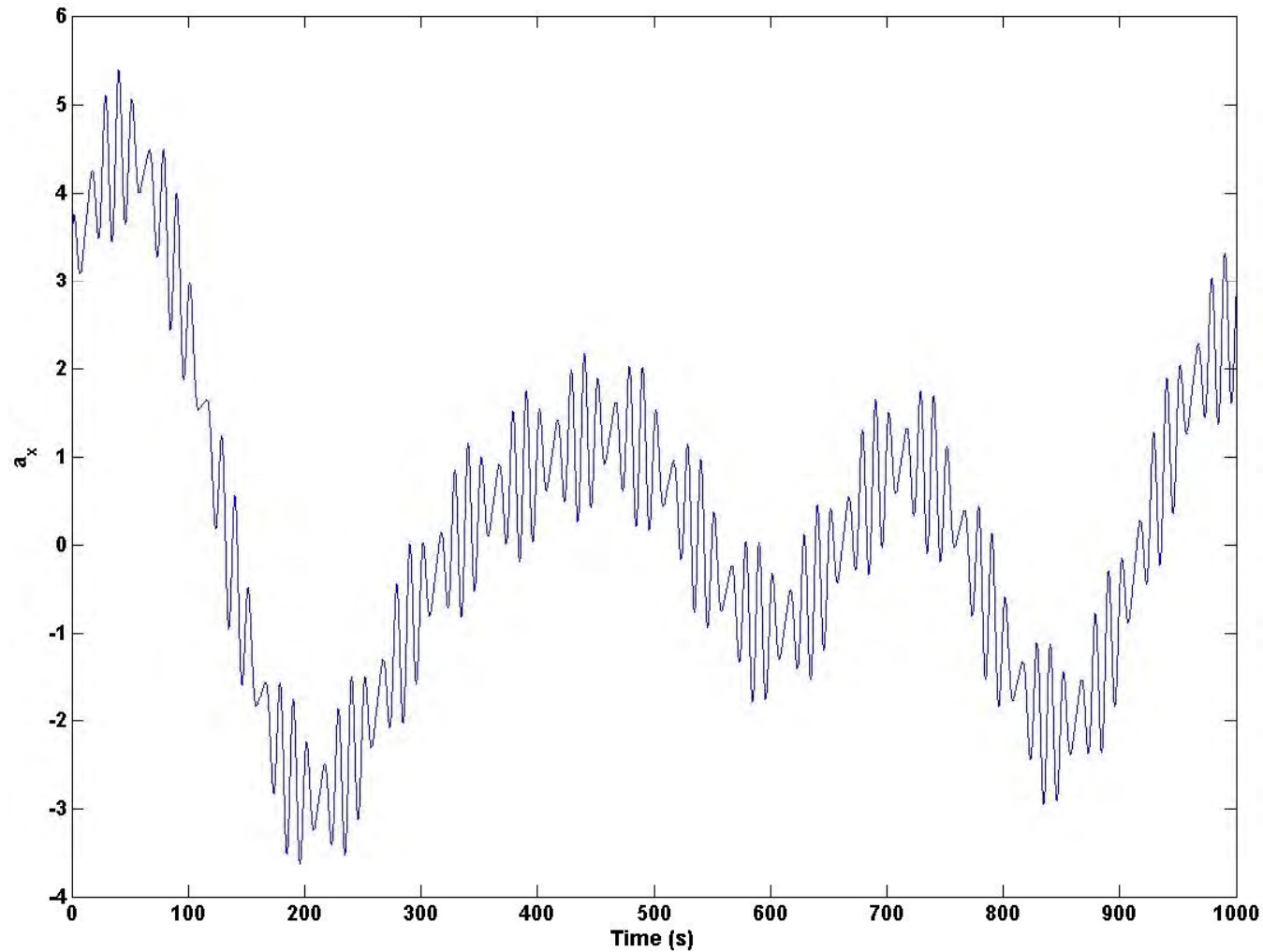


j=2, k=2

$A_1$	1.0
$A_2$	0.25
$B_1$	4.38
$B_2$	5.45
$C_1$	0.78
$C_2$	1.24
$D_1$	7.23
$D_2$	4.34
m	0.004
dt	0.001
T	1000

$$a_X^i = \sum_{j=1}^J A_j \sin\left(B_j \left(\frac{2\Pi}{T} (id_t)\right)\right) + \sum_{k=1}^K C_k \cos\left(D_k \left(\frac{2\Pi}{T} (id_t)\right)\right) + m(id_t)$$

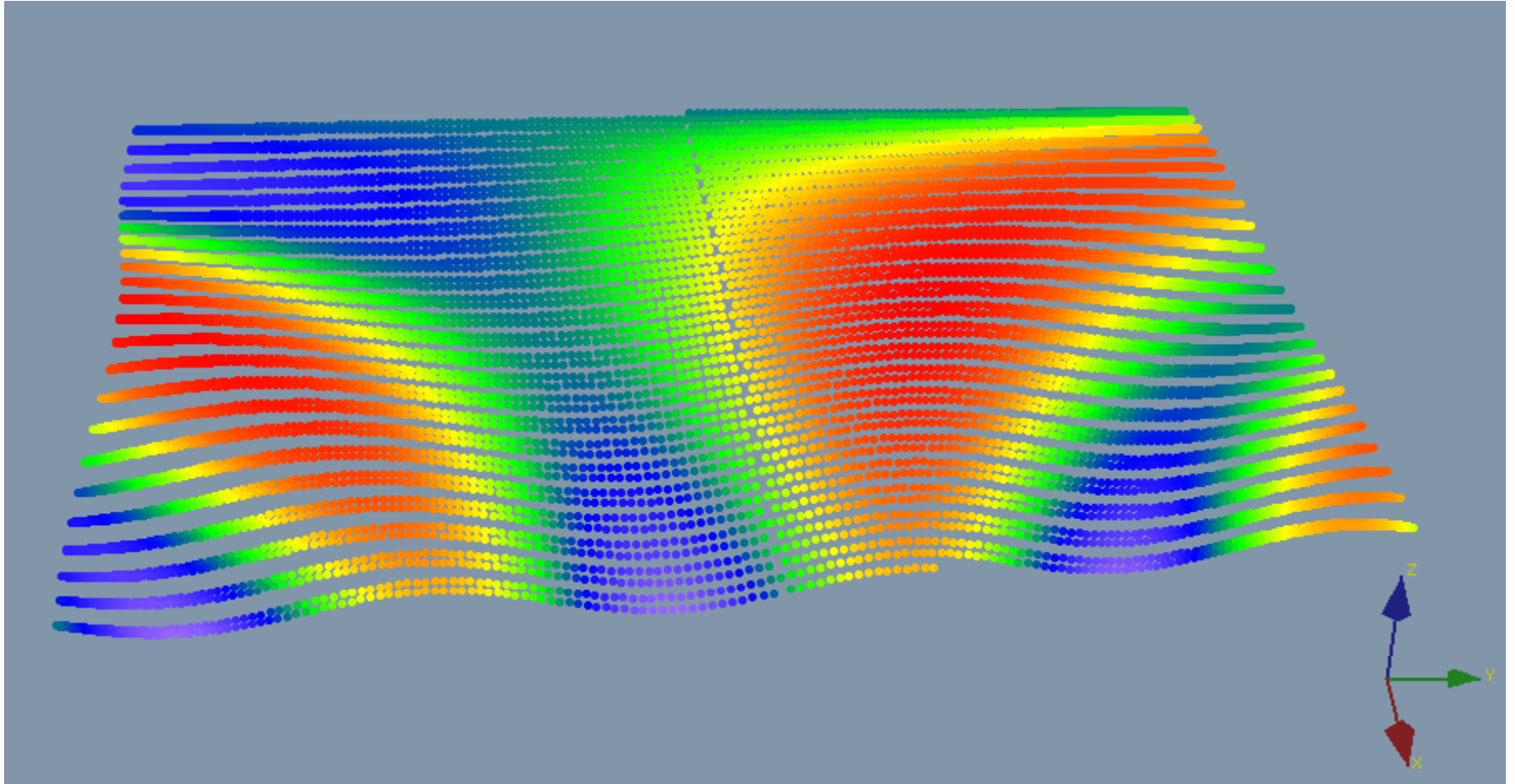
j=3, k=3



$A_1$	2.75
$A_2$	0.65
$A_3$	0.6
$B_1$	2.38
$B_2$	4.45
$B_3$	80
$C_1$	1.51
$C_2$	1.77
$C_3$	0.35
$D_1$	2.77
$D_2$	3.38
$D_3$	100
$m$	0.0
$dt$	0.006
$T$	1000

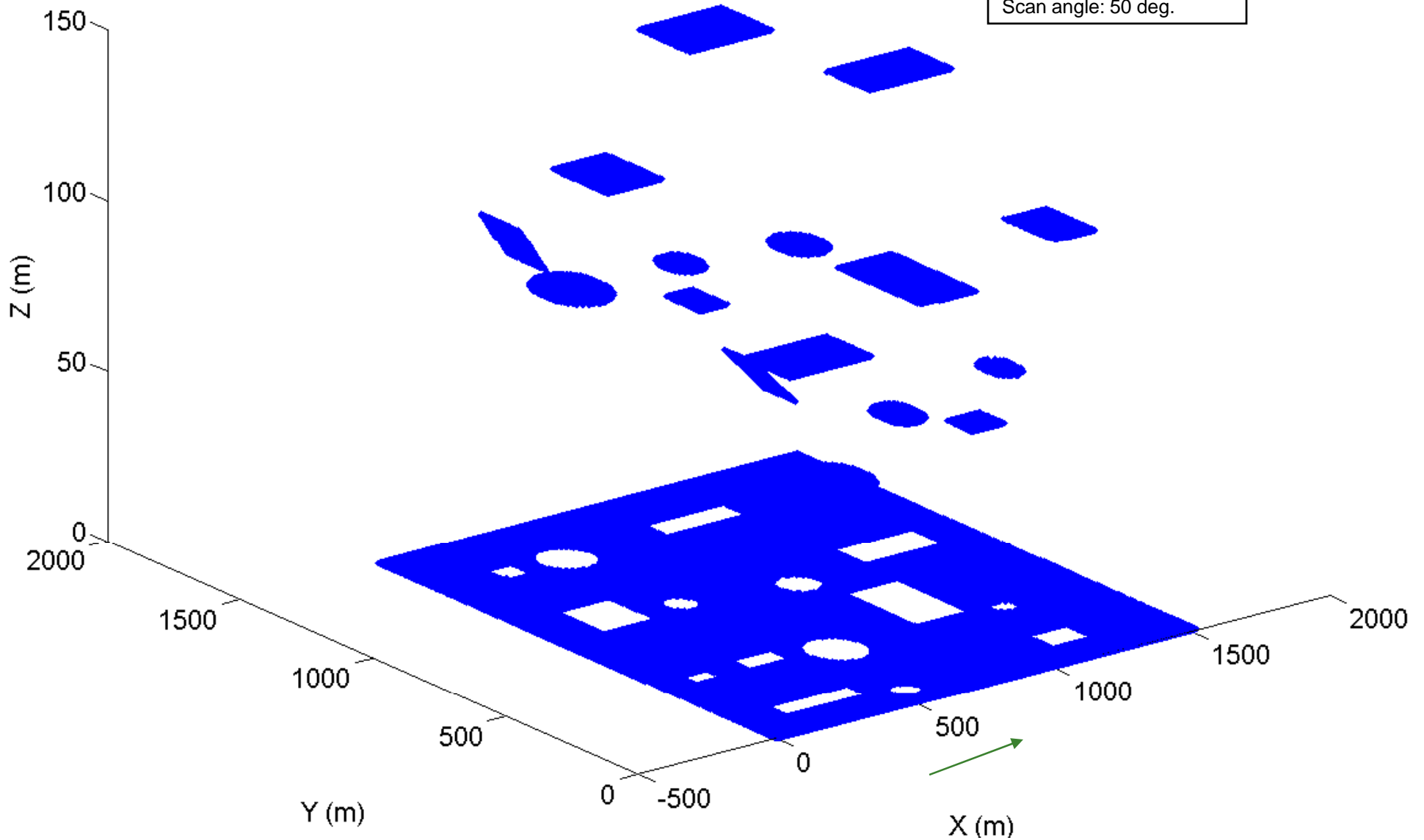
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# Point cloud for complex surface

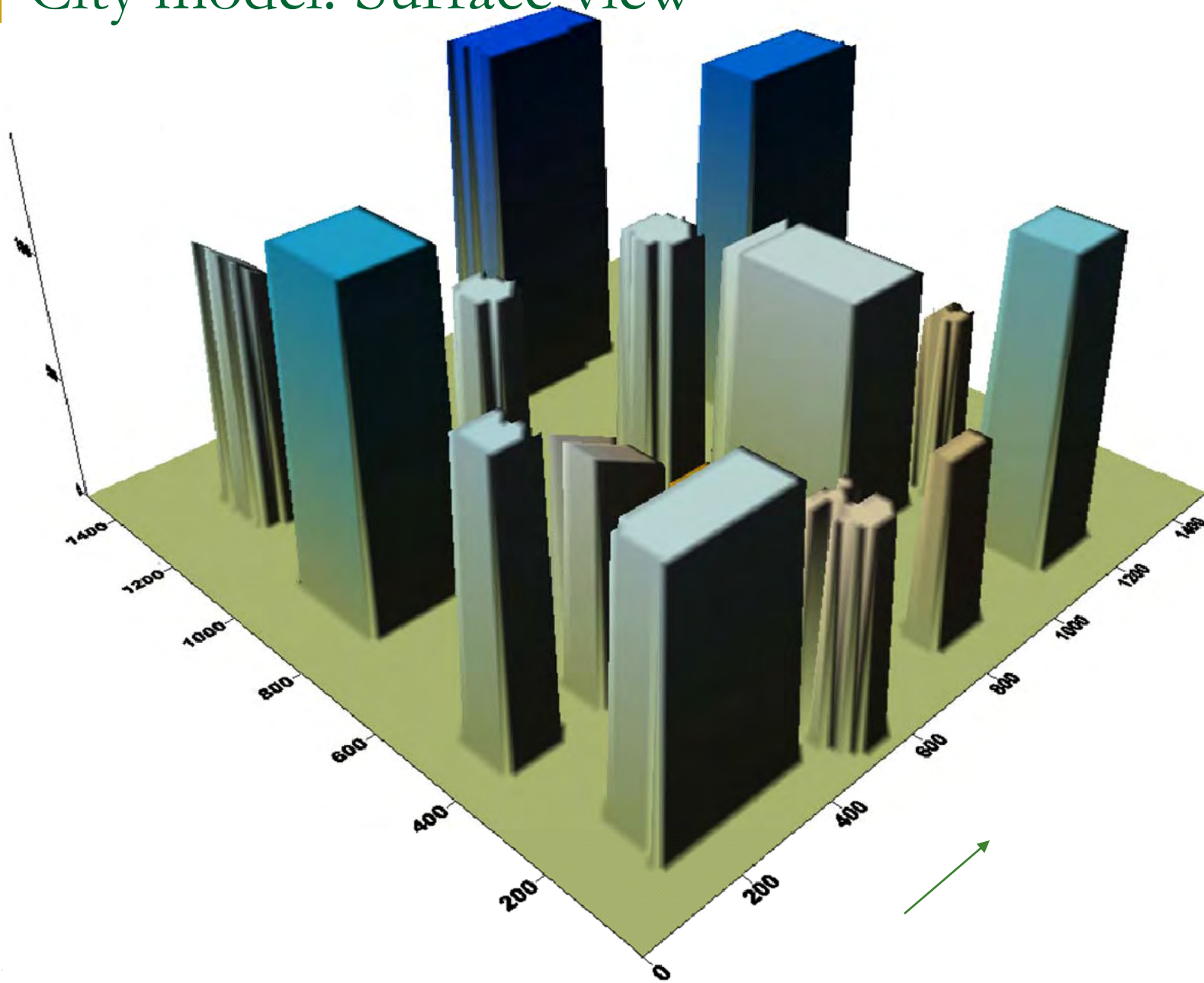


# Point cloud for city model

Flight velocity: 60 m/s.  
Flight height: 1610 m.  
Distance: 1500 m.  
Firing frequency: 20000 Hz.  
Scan frequency: 48 Hz.  
Scan angle: 50 deg.



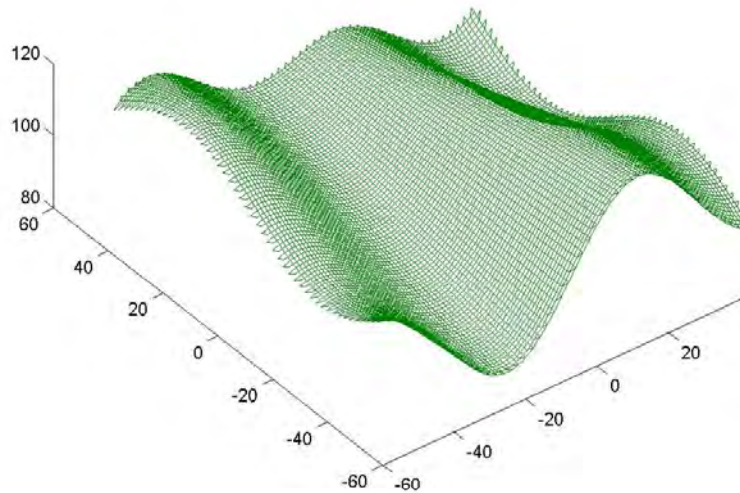
# City model: Surface view



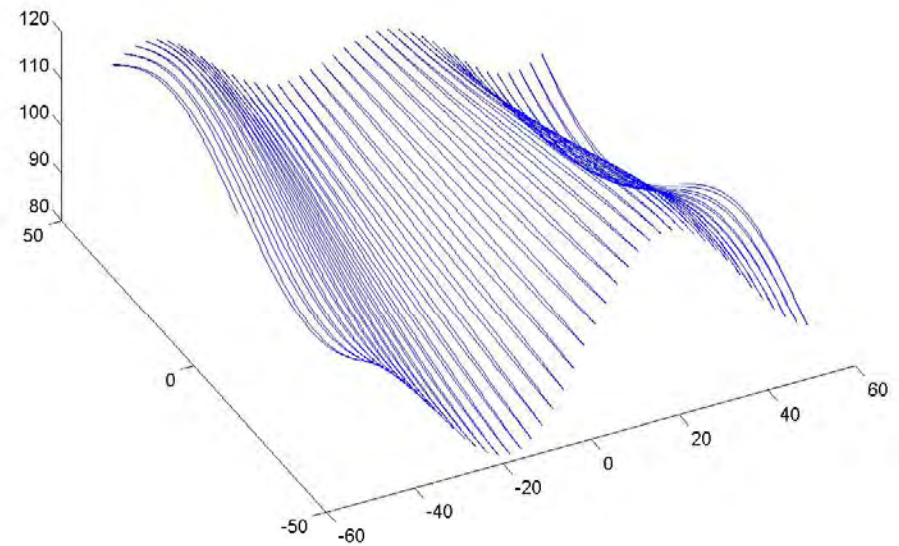


# Complex surfaces

$$Z = 10[\sin(X/10) - \sin(XY/800)] + 100$$



Generated in MATLAB

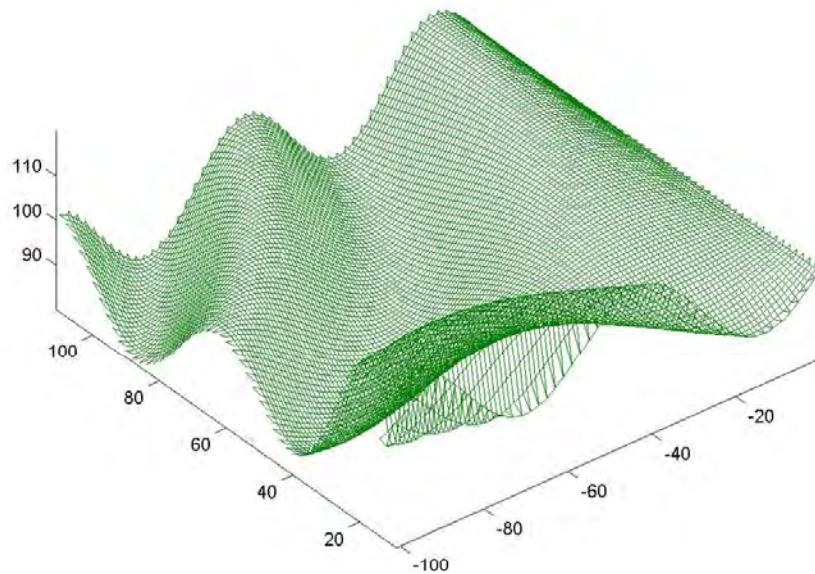


Generated in simulator

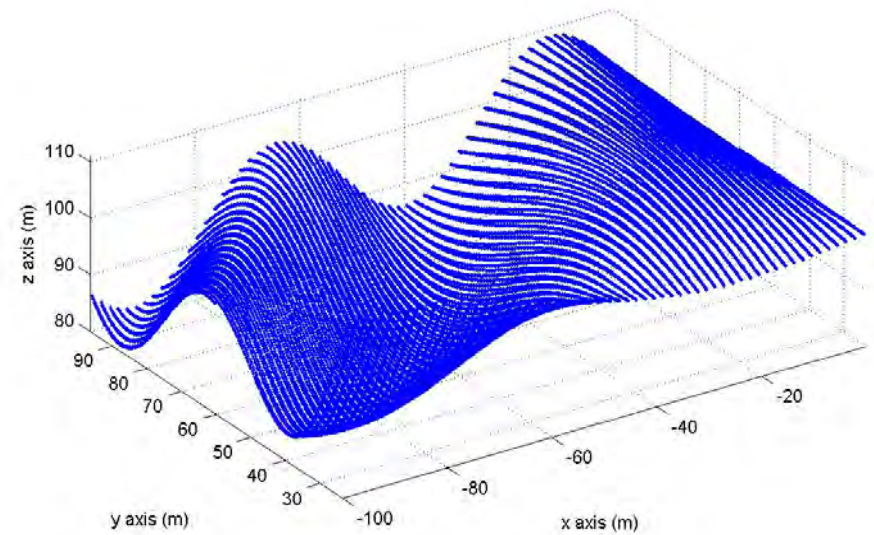


# Complex surfaces

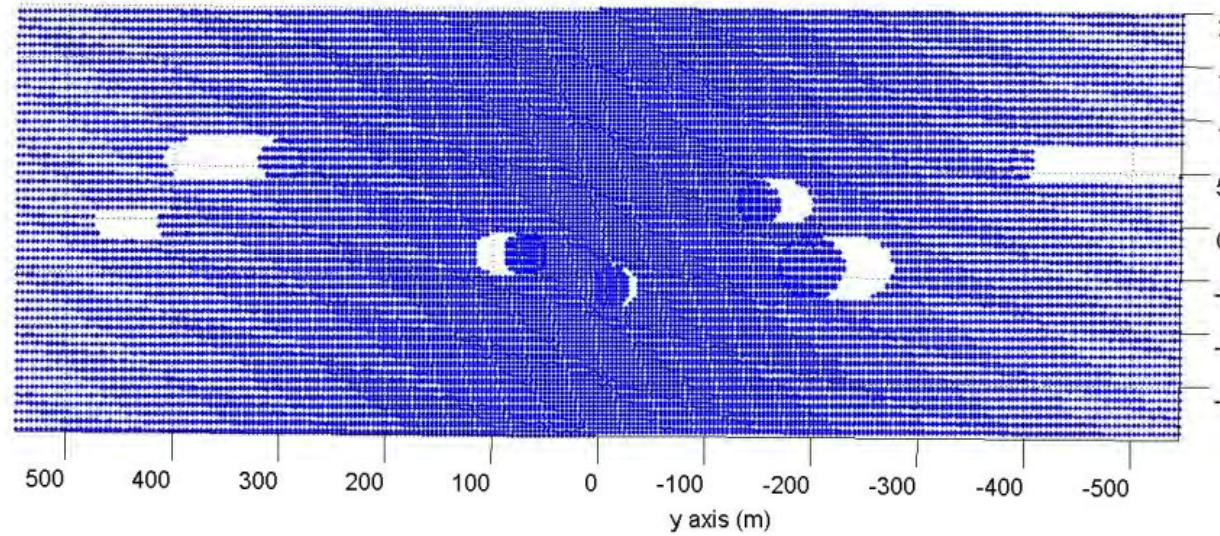
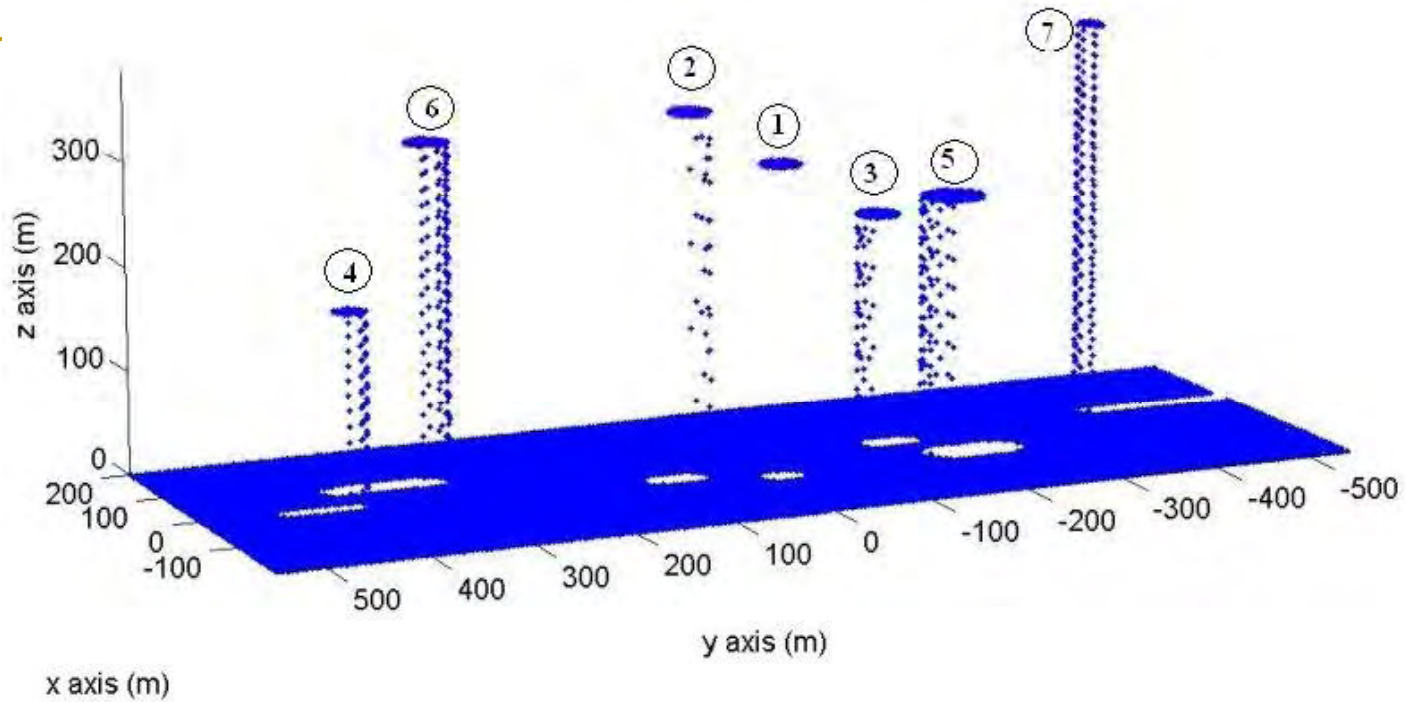
$$Z = 10[\sin(X/Y) - \sin(XY/800)] + 100$$



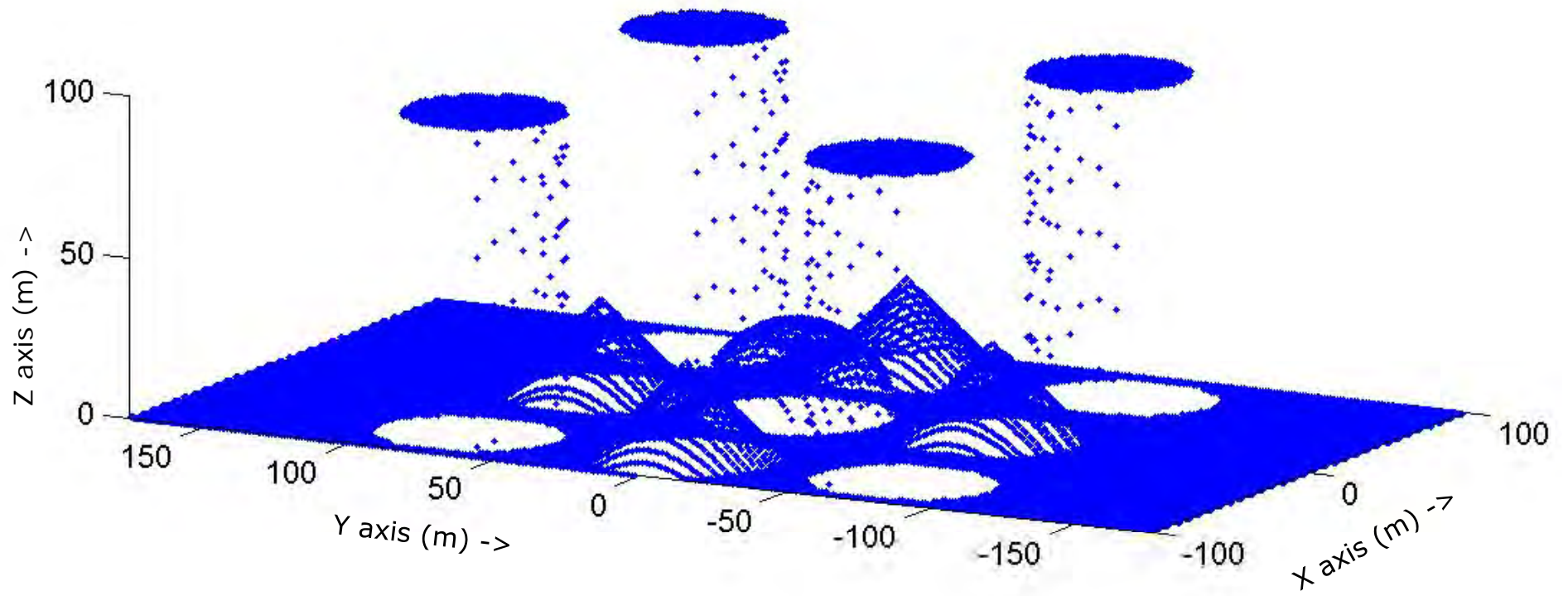
Generated in MATLAB



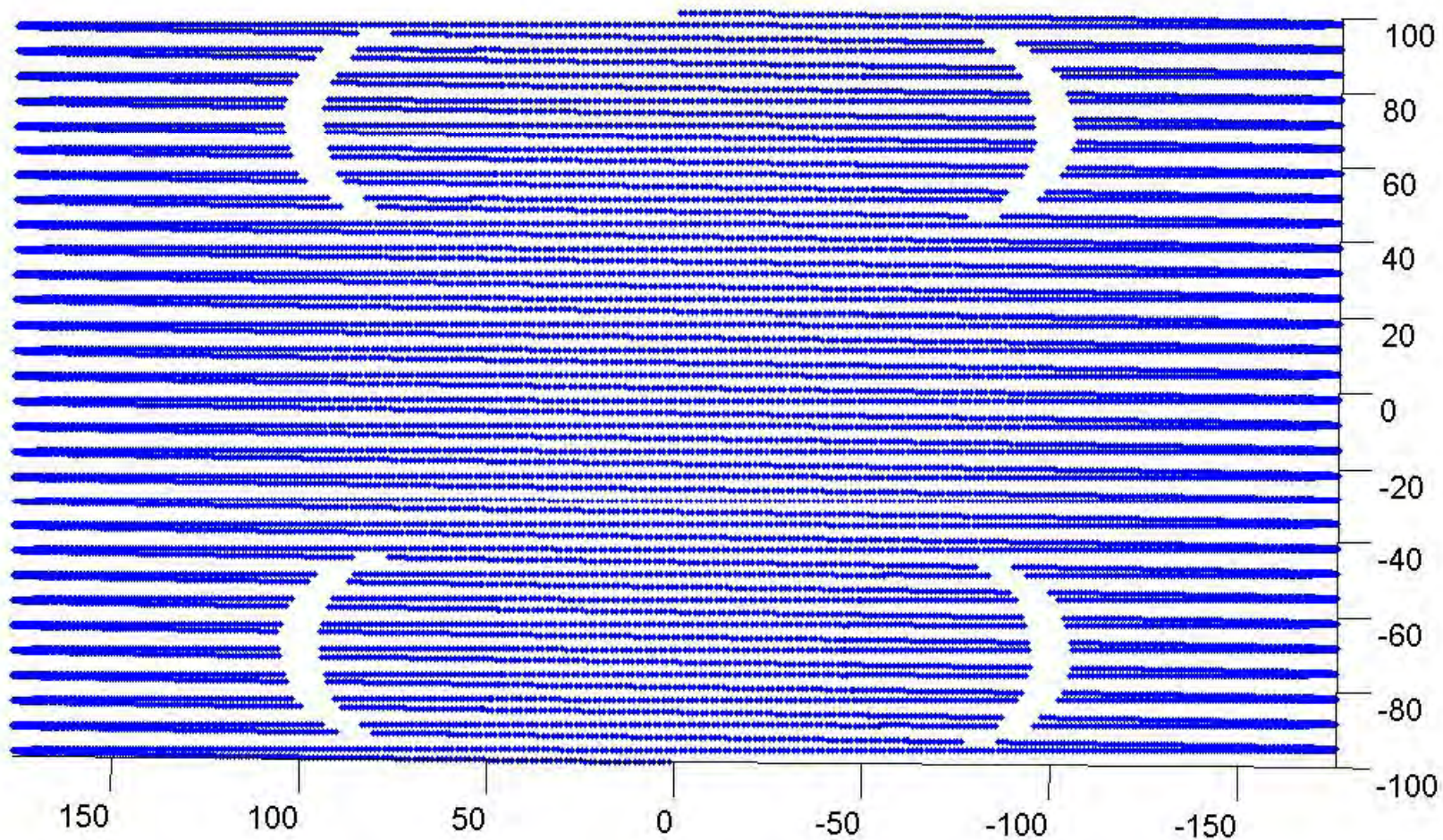
Generated in simulator



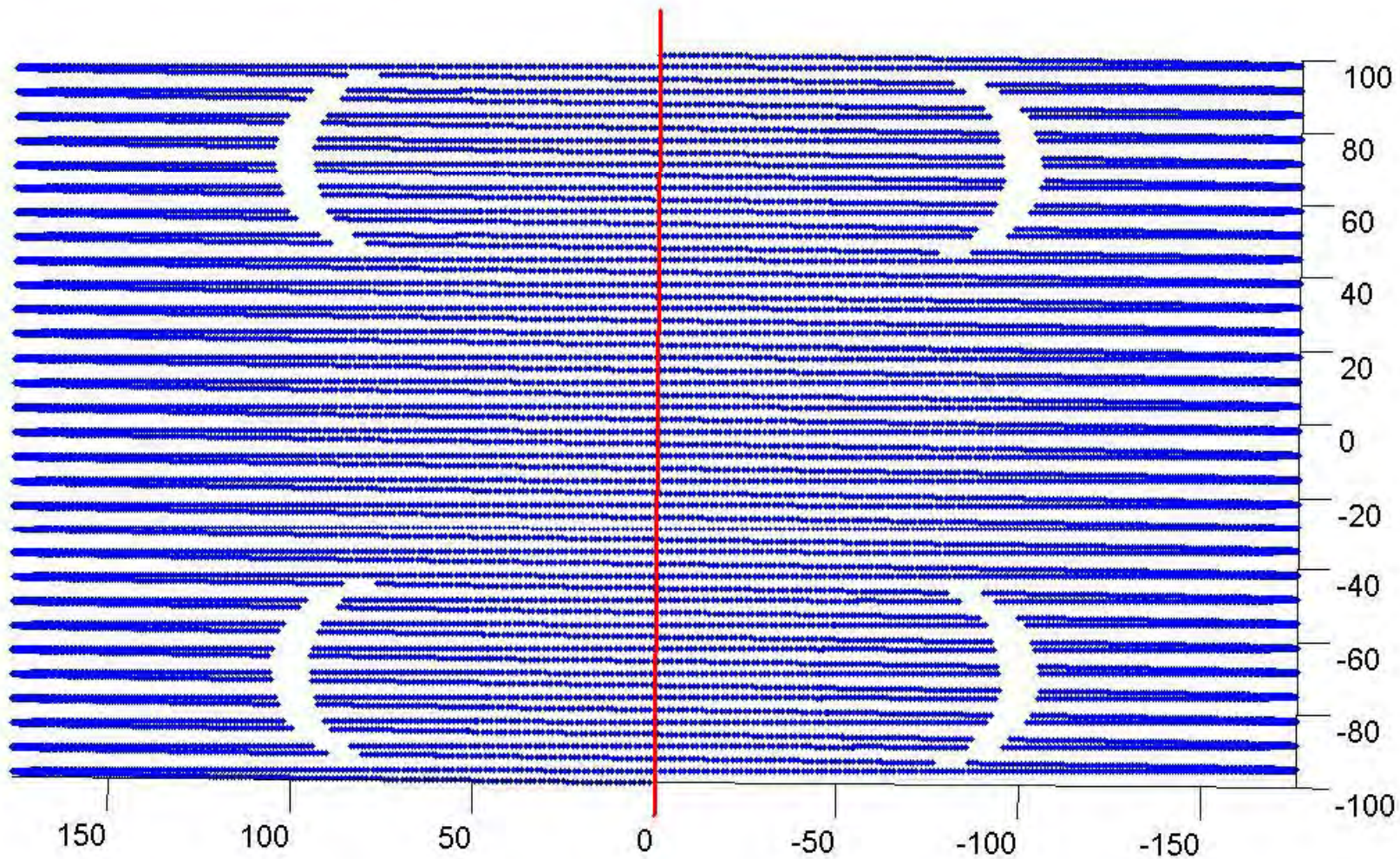
Top view (shadow effect)

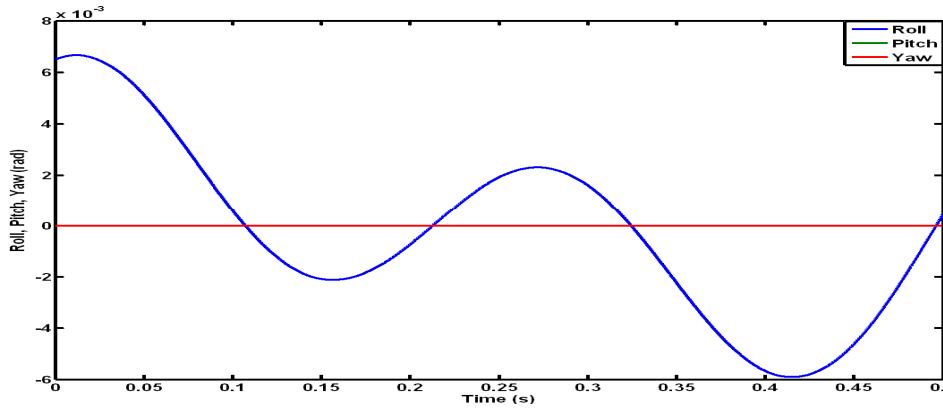






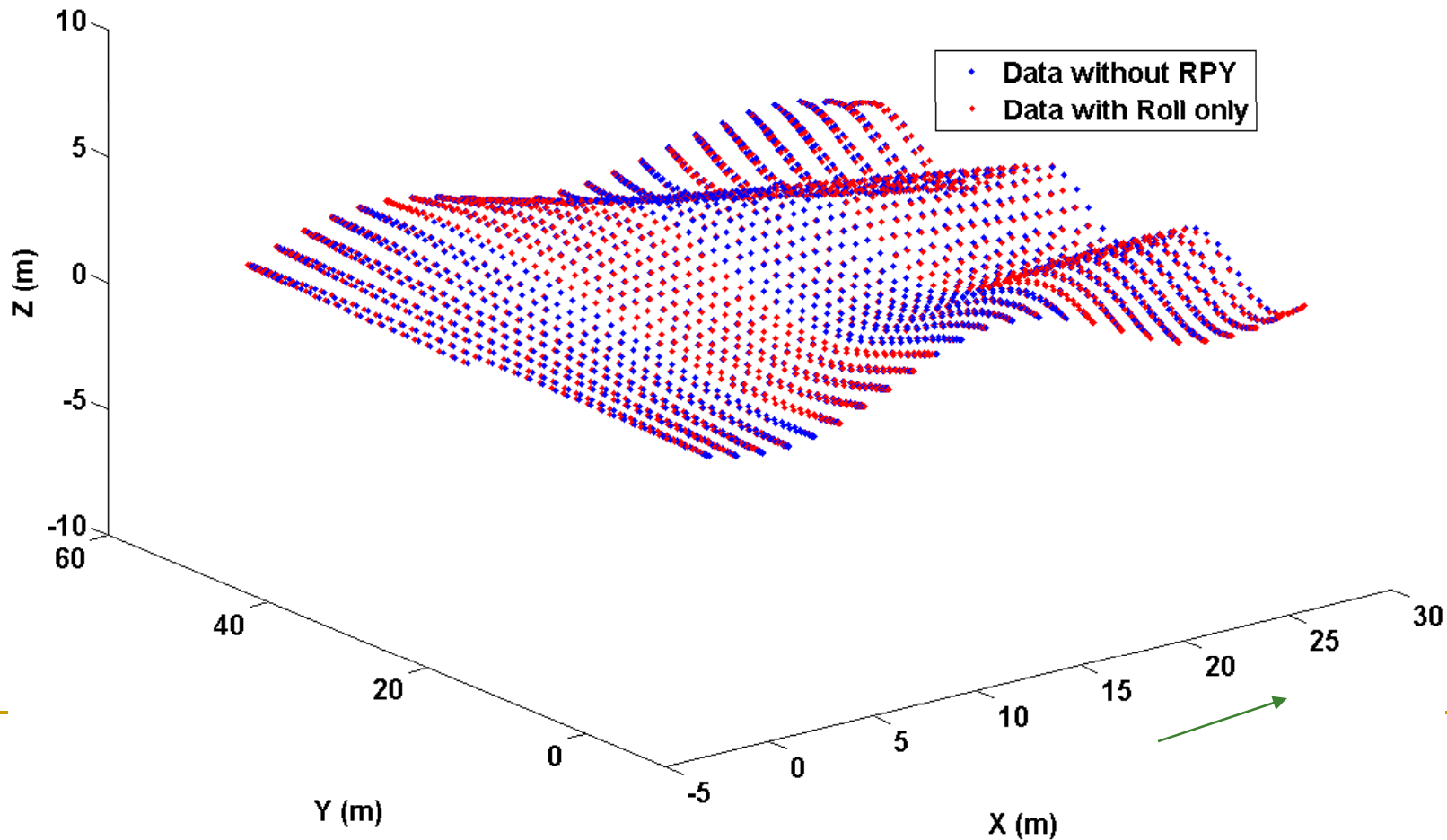


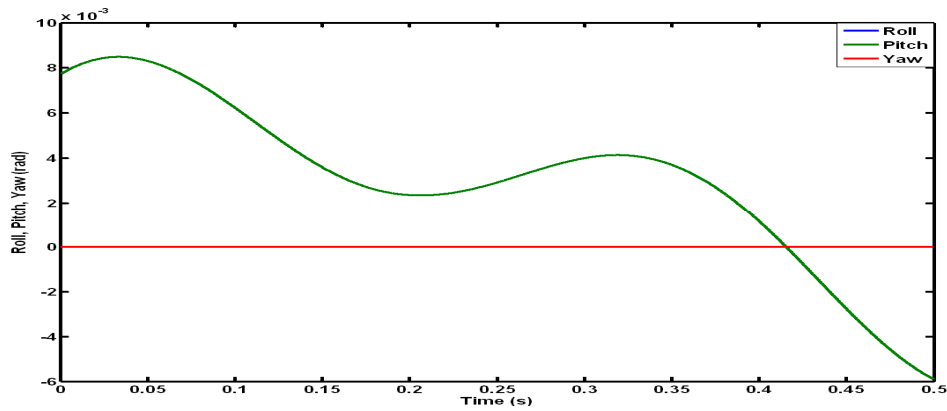




## Comparison of data sets without RPY and with Roll only.

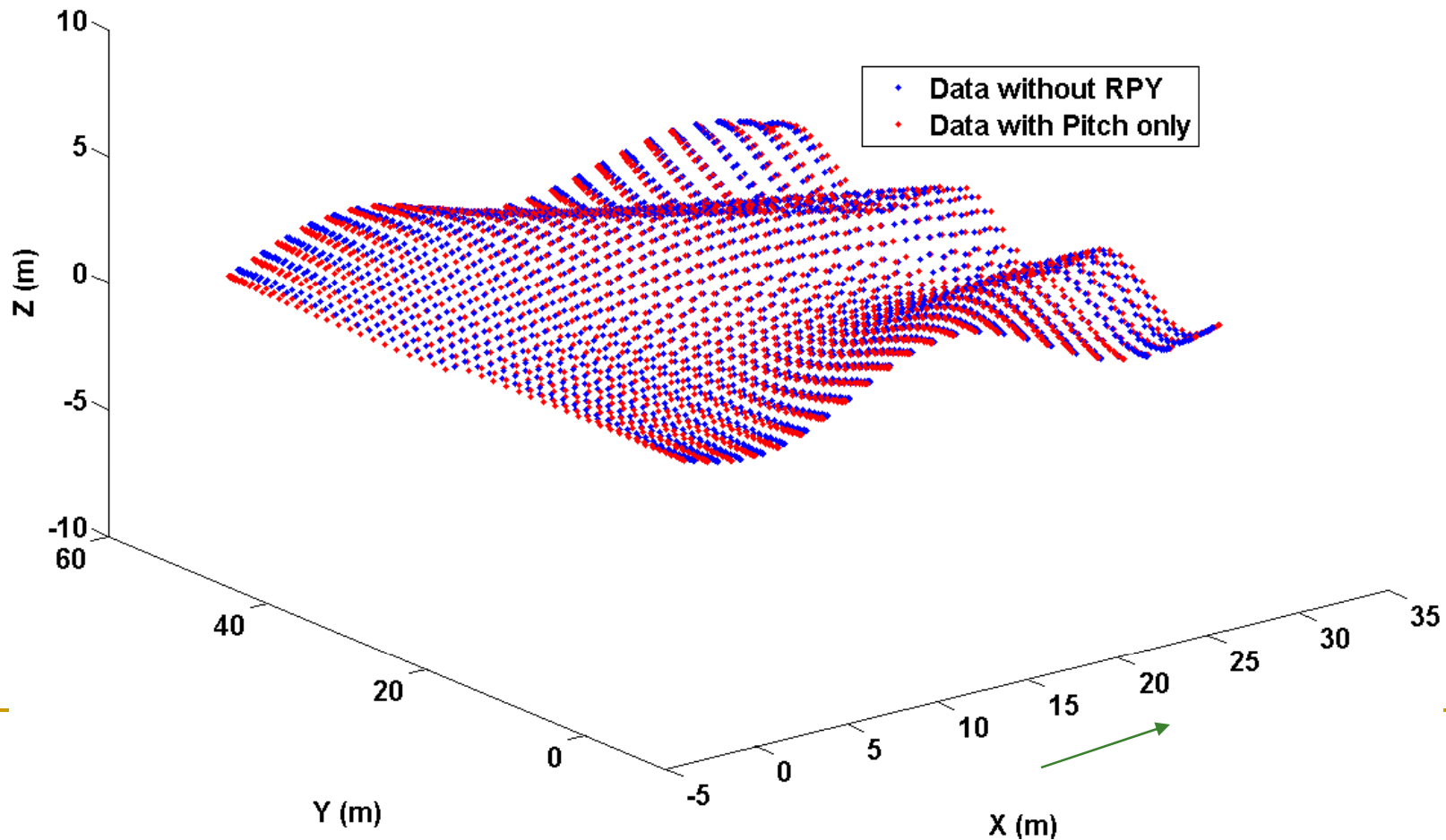
Equation of the surface:  $Z = \sin(X/10) - \sin(XY/90) - 60$ .  
 Flight velocity: 60 m/s.  
 Flight height: 60 m.  
 Distance: 30 m.  
 Firing frequency: 5000 Hz.  
 Scan frequency: 48 Hz.  
 Scan angle: 50 deg.



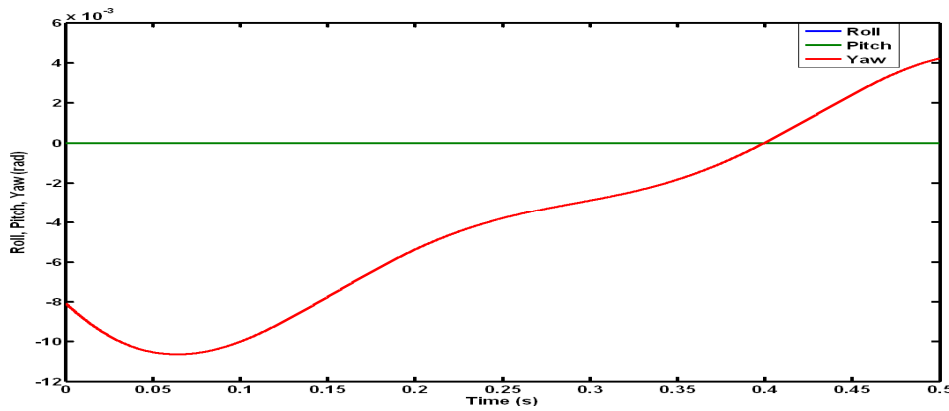


## Comparison of data sets without RPY and with Pitch only

Equation of the surface:  $Z = \sin(X/10) - \sin(XY/90) - 60$ .  
 Flight velocity: 60 m/s.  
 Flight height: 60 m.  
 Distance: 30 m.  
 Firing frequency: 5000 Hz.  
 Scan frequency: 48 Hz.  
 Scan angle: 50 deg.

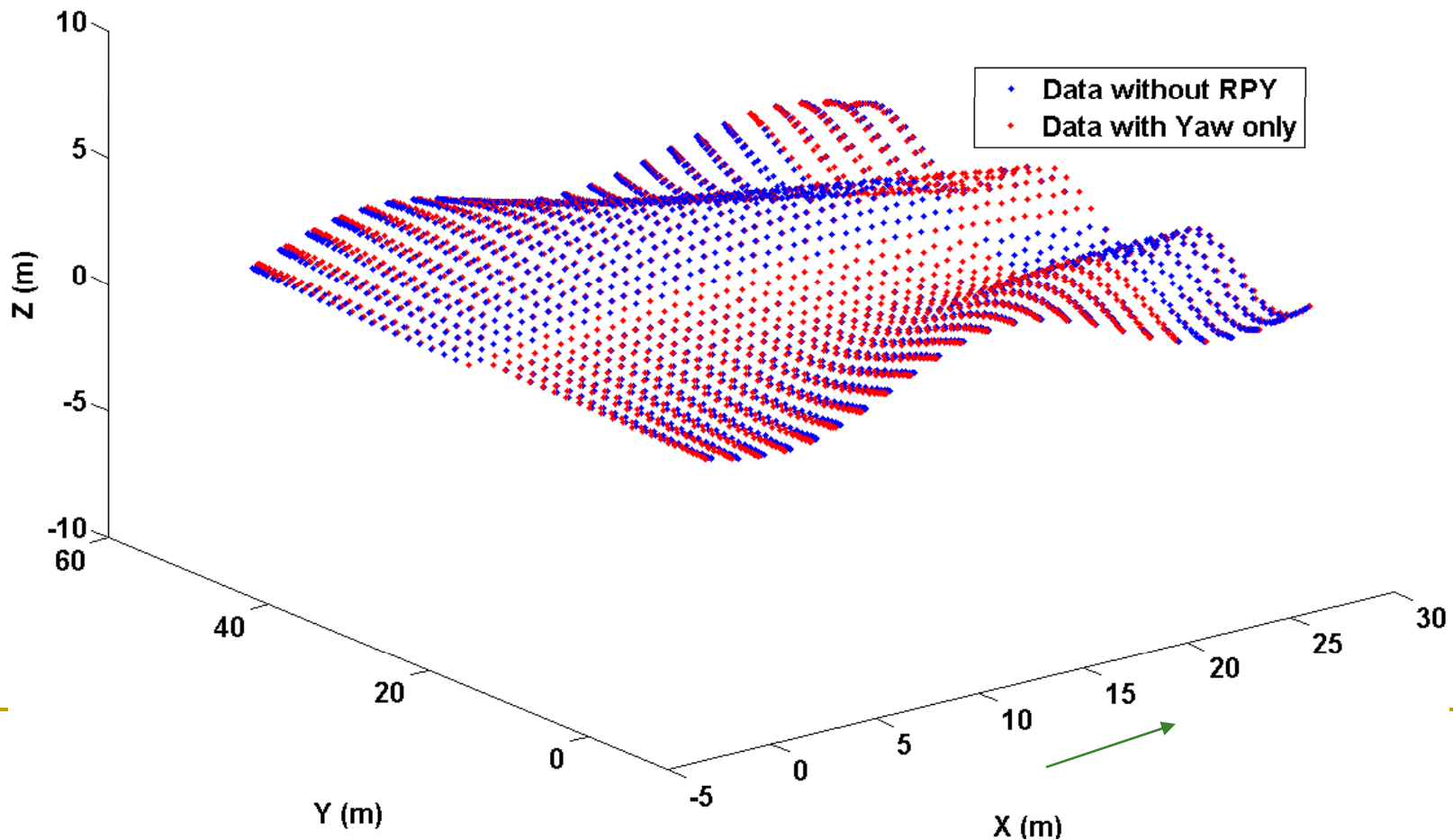




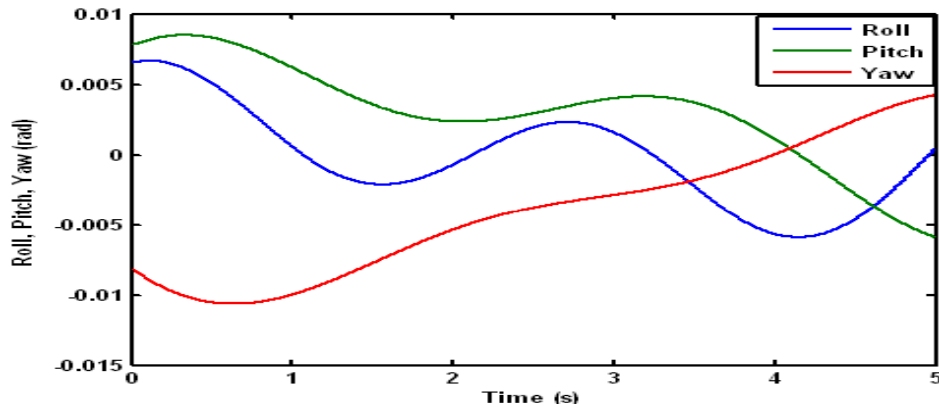


## Comparison of data sets without RPY and with Yaw only

Equation of the surface:  $Z = \sin(X/10) - \sin(XY/90) - 60$ .  
 Flight velocity: 60 m/s.  
 Flight height: 60 m.  
 Distance: 30 m.  
 Firing frequency: 5000 Hz.  
 Scan frequency: 48 Hz.  
 Scan angle: 50 deg.

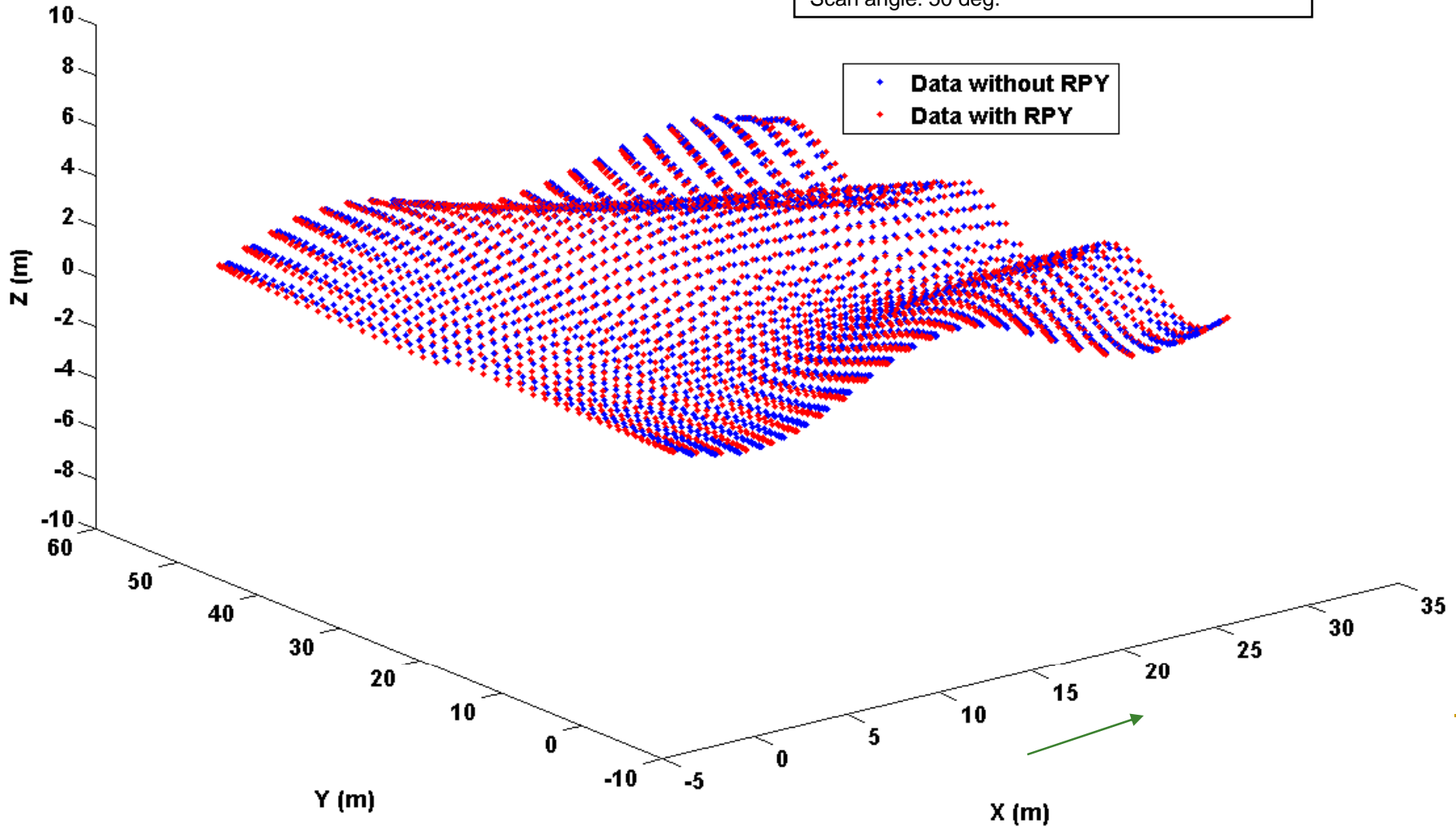




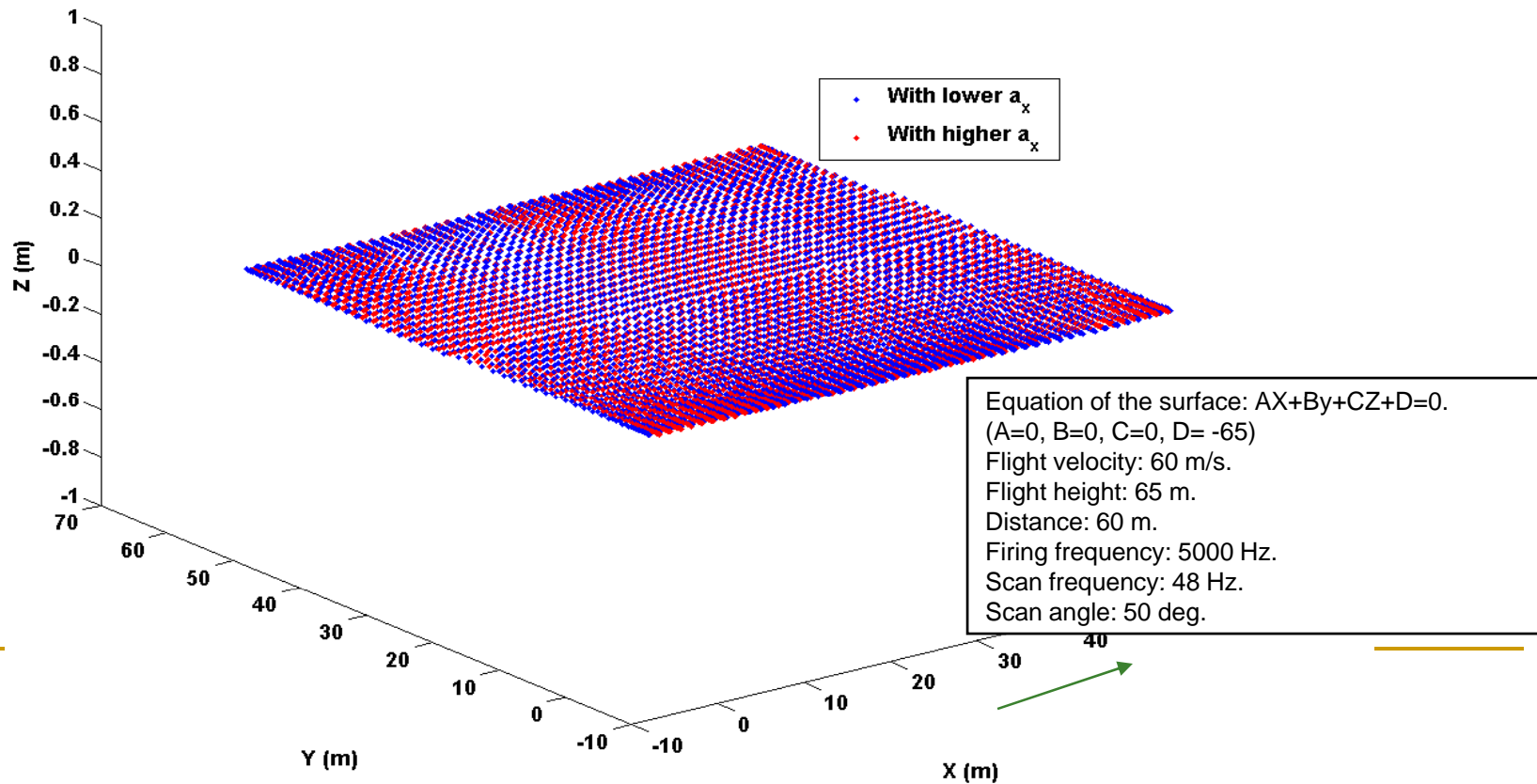
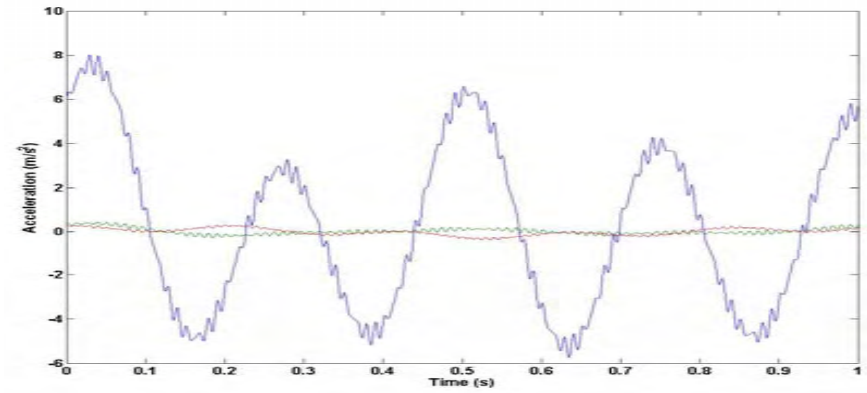
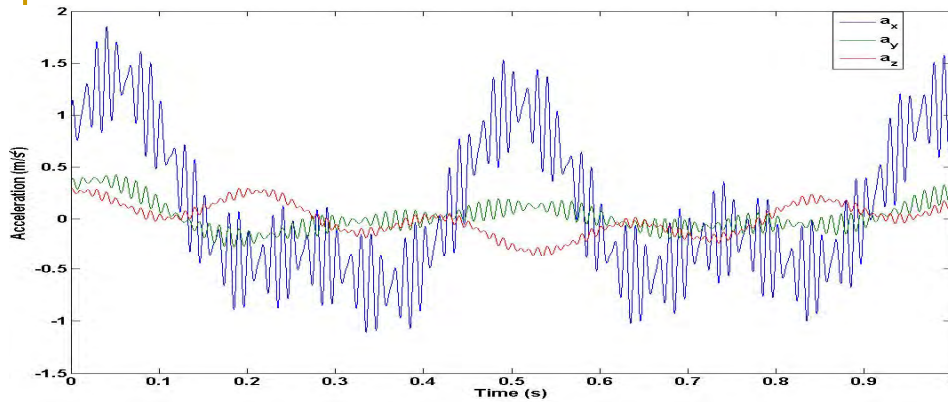


## Comparison of data sets with and without RPY

Equation of the surface:  $Z = \sin(X/10) - \sin(XY/90) - 60$ .  
 Flight velocity: 60 m/s.  
 Flight height: 60 m.  
 Distance: 30 m.  
 Firing frequency: 5000 Hz.  
 Scan frequency: 48 Hz.  
 Scan angle: 50 deg.

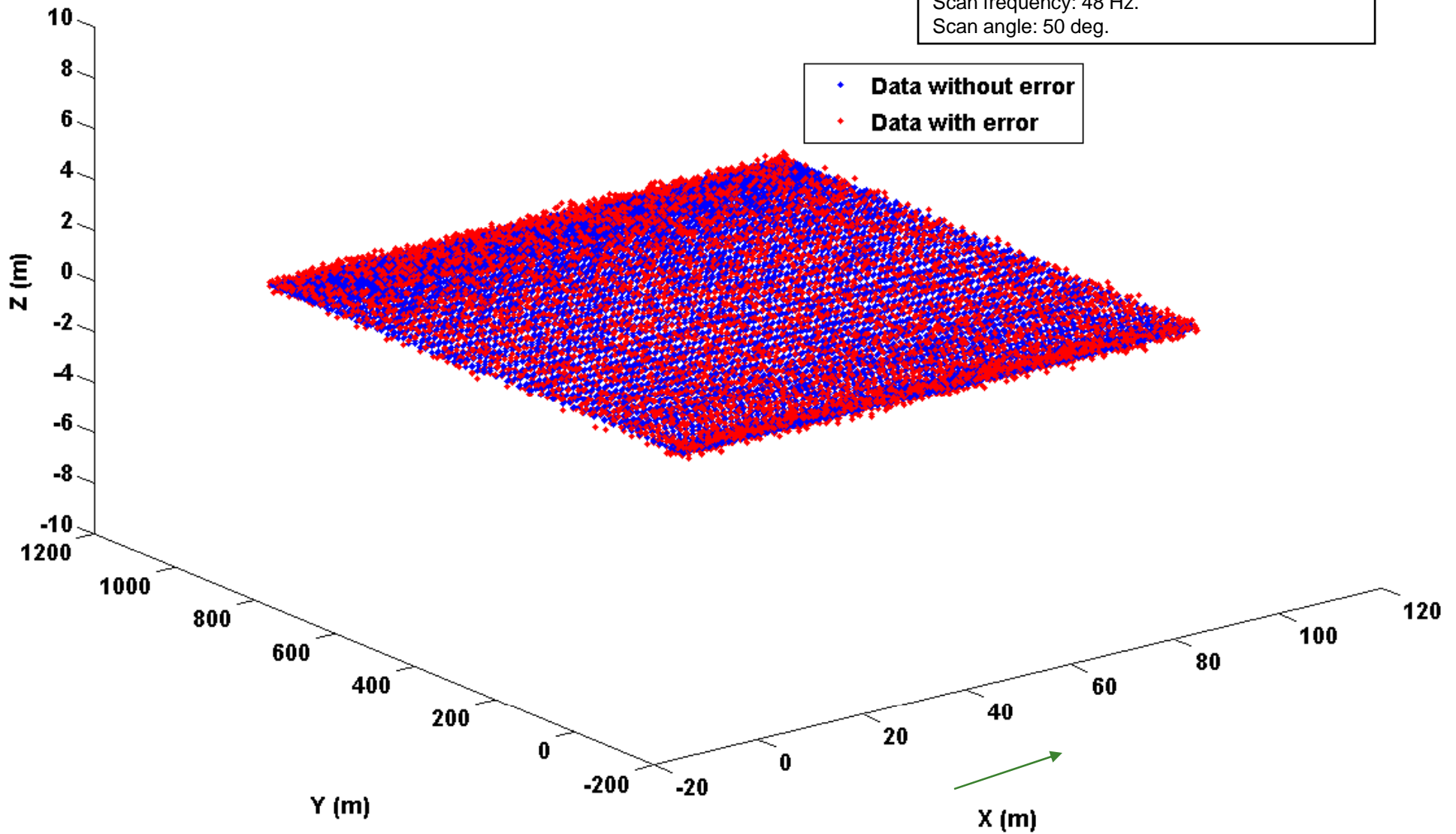


## Comparison of data sets with lower and higher $a_x$



## Comparison of data sets with and without normal error.

Equation of the surface:  $AX+By+CZ+D=0$ .  
( $A=0, B=0, C=0, D= -1100$ )  
Flight velocity: 60 m/s.  
Flight height: 1100 m.  
Distance: 100 m.  
Firing frequency: 5000 Hz.  
Scan frequency: 48 Hz.  
Scan angle: 50 deg.



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# Applications of simulator

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# Education

- To understand:
    - Process of data generation
    - Effect of change in various parameters on data
    - Effect of errors on data
-

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# Laboratory exercises

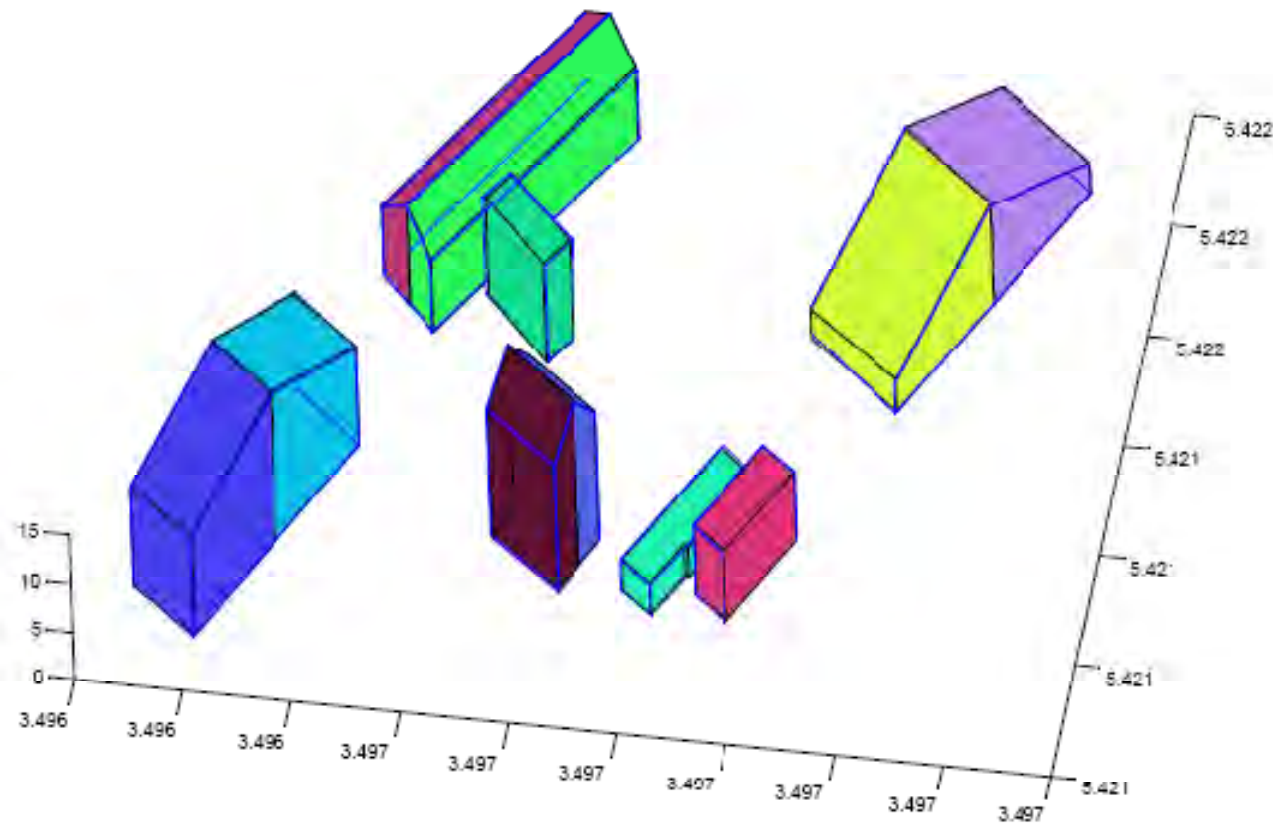
- Data with varied specifications
  - Full and accurate ground truth known
-

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# Student research projects

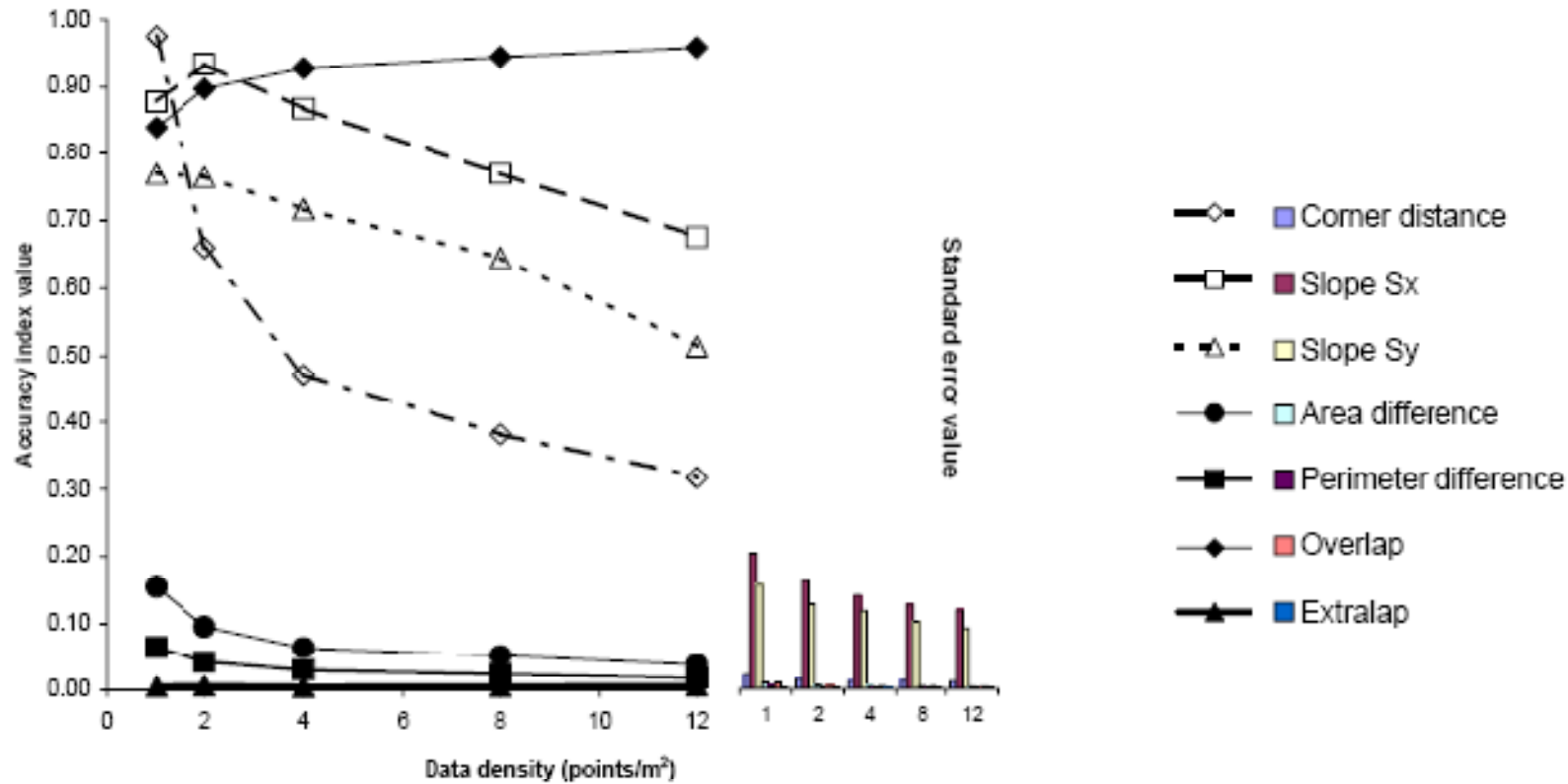
- ❑ Evaluation of Information extraction algorithms
  - ❑ Assessing effect of error on performance of algorithms
  - ❑ Finding optimal data specifications for an application
-

# Application in building identification research





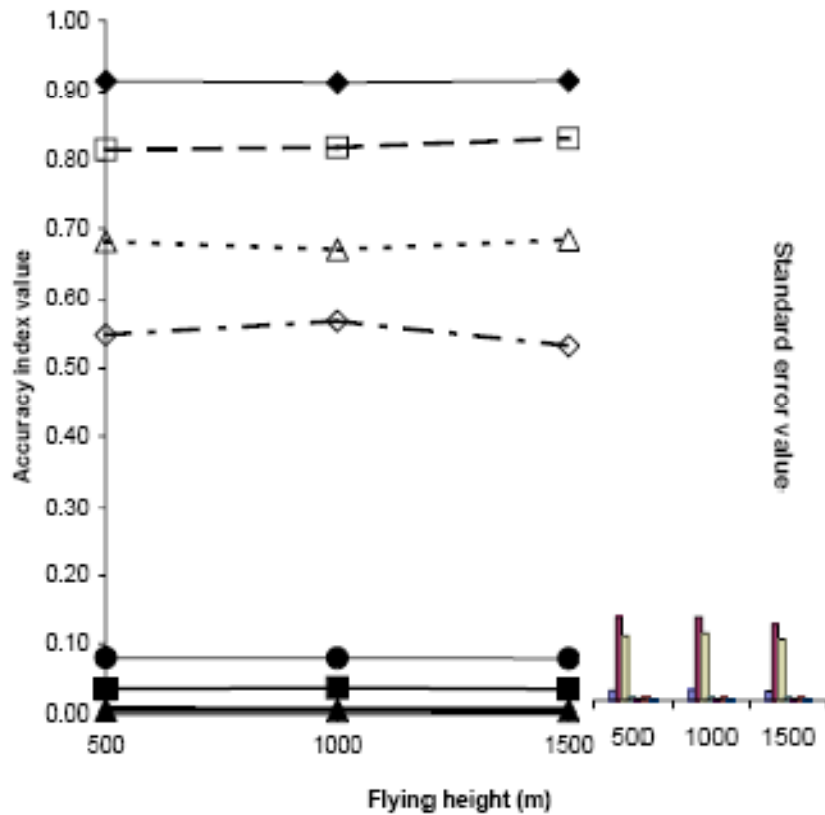
# Variation of accuracy indices



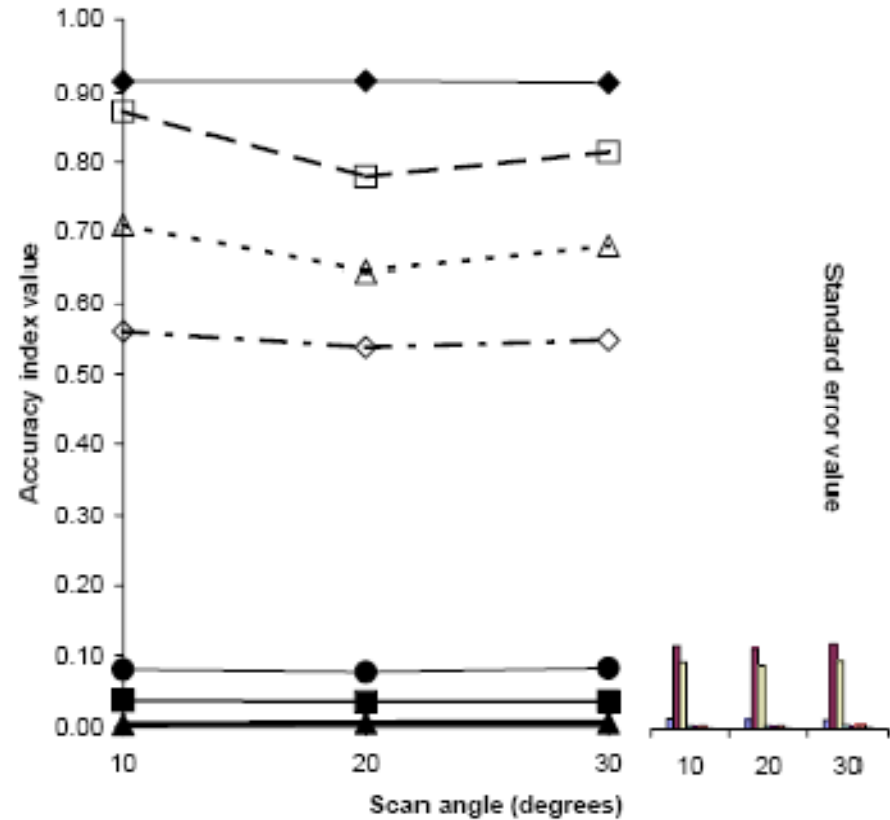
(c) With data density

(d) Legend for mean and standard error

# Variation of accuracy indices



(a) With flying height



(b) With scan angle

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Thanks!

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