

## ESO 208A; ESO 218

### Computational methods in engineering

#### Assignment # 4

**Due date: September 12, 2013**

1: Solve the following system of equations using  $LU$  decomposition without partial pivoting:

$$2x_1 - 6x_2 - x_3 = -38$$

$$-3x_1 - x_2 + 7x_3 = -34$$

$$-8x_1 + x_2 - 2x_3 = -20$$

2: Determine the total flops as a function of the number of equations  $n$  for the (a) decomposition, (b) forward-substitution, and (c) back-substitution phases of the  $LU$  decomposition version of Gauss elimination.

3: Use  $LU$  decomposition to determine the matrix inverse for the following system. Do not use a pivoting strategy. And check your result by verifying that  $[A] [A]^{-1} = [1]$ .

$$10x_1 + 2x_2 - x_3 = 27$$

$$-3x_1 - 6x_2 + 2x_3 = -61.5$$

$$x_1 + x_2 + 5x_3 = -21.5$$

4: Solve the following set of equations with  $LU$  decomposition:

$$3x_1 - 2x_2 + x_3 = -10$$

$$2x_1 + 6x_2 - 4x_3 = 44$$

$$-x_1 - 2x_2 + 5x_3 = -26$$