

TUTORIAL EXERCISES (NEED NOT BE SUBMITTED)

1. Find the limits of the following sequences if they exist. Else explain why they do not exist.

(i)  $\frac{\cos n}{n}$

(ii)  $\frac{\sin n^2}{\sqrt{n}}$

(iii)  $\frac{n^2}{n-3}$

2. Find the infimum and supremum of  $\left\{ \frac{3n+7}{n} \mid n \in \mathbb{N} \right\}$ .

3. Find the infimum and supremum of  $\left\{ \frac{1}{n} - \frac{1}{m} \mid n, m \in \mathbb{N} \right\}$ .

4. Give examples of following type of sequences.

(i) Bounded but not convergent

(ii) Monotone but not bounded

(iii) Monotone but not Cauchy