

# Joint Precoder and Receiver Design for Asymmetric Two-way MIMO AF Relaying

Rohit Budhiraja

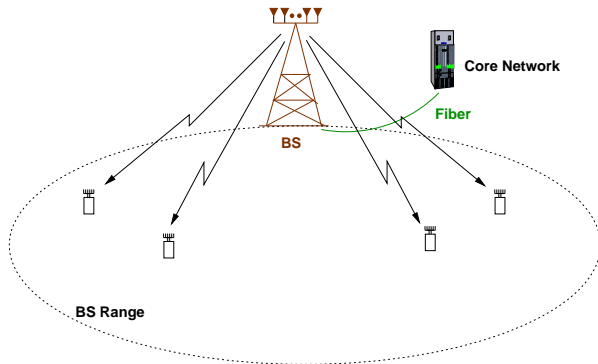
Advisor – Bhaskar Ramamurthi

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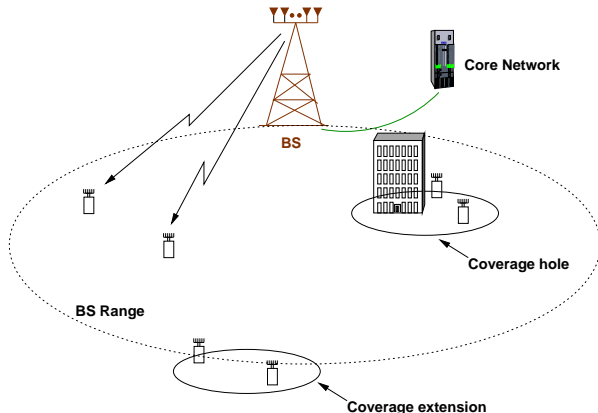
Second Ph.D Seminar January 22, 2015

# Single-hop cellular architecture



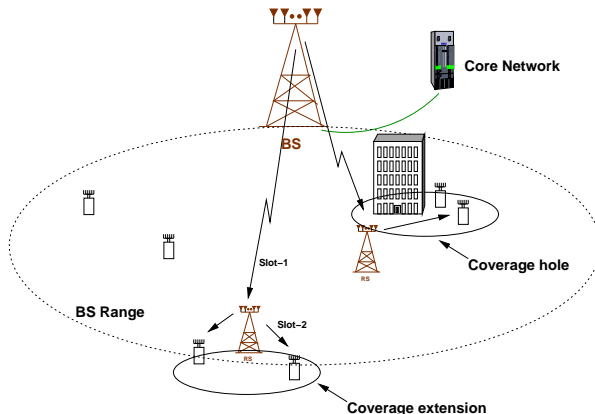
- Two links – wireless access link and **wired backhaul link**.
- Single-hop architecture works well if direct access links are strong.

# Cellular scenarios with weak direct links



- Two examples: 1) Coverage extension; and 2) Coverage hole.
- Installing a BS for few users is costly **due to core network & backhaul link**.

# Cellular systems with relays



- Relay is a (simplified) BS without backhaul infrastructure.
  - ▶ Relay functionality can vary from a simple repeater to a full-blown BS.

# Half-duplex relaying

- Half-duplex constraint is imposed on the relay (**easy to design**).
  - ▶ Full-duplex technology is currently being practically evaluated.
- Relay cannot transmit and receive on same spectral resource at same time.
- Two widely studied half-duplex relaying protocols:
  - ▶ **One-way relay**: Needs four time slots to exchange two data units.
  - ▶ Spectrally inefficient when compared with direct communication.

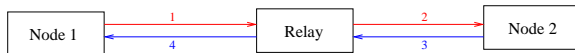


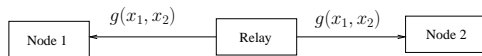
Figure: One-way relaying protocol.

# Two-way relaying<sup>1</sup>

- Consists of two phases.
- MAC phase:** Two source nodes simultaneously transmit to the relay.



- Broadcast phase:** Relay broadcasts a function of the **sum-signal**.



- Both nodes can cancel **back-propagating interference** as both know self-data.
- Two slots are required to exchange two data units – **spectrally efficient**.

<sup>1</sup>Rankov, B and Wittneben, A, "Spectral Efficient Protocols for Half-Duplex Fading Relay Channels", IEEE J. Sel. Areas Commun, vol. 25, no. 2, pp. 375–385, 2007.

# Basic assumption in two-way relaying

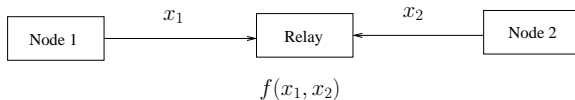
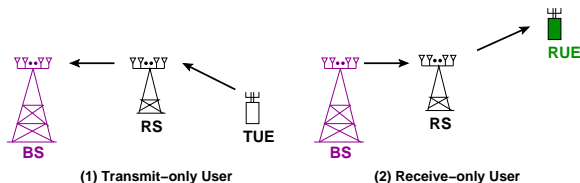


Figure: MAC phase of two-way relaying

- Two nodes want to exchange data via a relay.
- Both nodes should have data to send and receive.
- Strong assumption!

# Data exchange in cellular systems

- Usually does not happen!<sup>2</sup>



Non-simultaneous traffic scenarios

- E.g., TUE uploading a Youtube video / RUE watching a Netflix movie.
- Users either want to send or receive data.

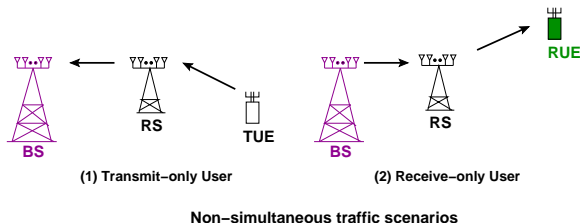
Two way relaying cannot be used in these scenarios.

<sup>2</sup>Rohit Budhiraja, Karthik KS and Bhaskar Ramamurthi "Precoder design for Asymmetric Multi-user Two-way AF Relaying in Cellular Systems", ICC 2013, Hungary.



# Option for BS to serve TUE and RUE

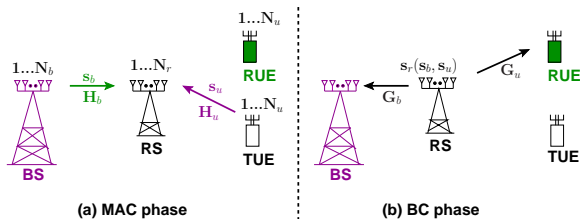
- Use one way relaying.



- BS will require 4 time slots – spectrally inefficient.

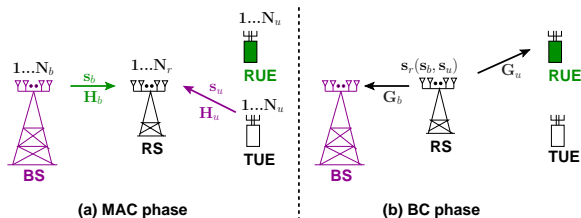
# Proposed asymmetric two-way relaying (ATWR)

- MAC phase: Both BS and TUE simultaneously transmit to the relay.
- BC phase: Relay broadcasts to both BS and RUE.



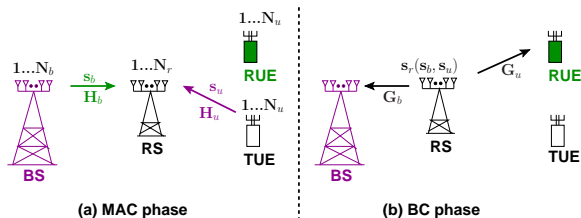
- BS requires two slots to serve two users.

# Back-propagating interference in ATWR



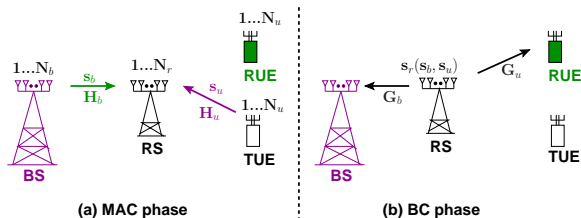
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- Relay transmit signal:  $\mathbf{s}_r = f(\mathbf{y}_r) = f(\mathbf{s}_u, \mathbf{s}_b)$ .
- BS receive signal:  $\mathbf{y}_b = \mathbf{G}_b \cdot f(\mathbf{s}_u, \mathbf{s}_b)$ . BS can cancel  $\mathbf{s}_b$  and detect  $\mathbf{s}_u$ .
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# State-of-the-art in ATWR

- Cancel BI using overhearding - assumes RUE overhears TUE in MAC phase.
  - ▶ Consider single antenna nodes.
  - ▶ Analysed sum-rate,<sup>3</sup> scheduling<sup>4</sup> and diversity multiplexing trade-off.<sup>5</sup>
- We do not assume overhearding and design a precoder at relay to cancel BI.
  - ▶ Consider MIMO nodes.
  - ▶ Designed relay precoder,<sup>6</sup> joint precoder<sup>7</sup> and considered multi-user scenario.<sup>8</sup>

<sup>3</sup> C. D. T. Thai et. al. Multi-Cell Multi-User Relaying Exploiting Overheard Signals, IEEE Wireless Commun. Lett., Aug. 2014.

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<sup>7</sup> Rohit Budhiraja and Bhaskar Ramamurthi "Joint Precoder and Receiver Design for AF Non-Simultaneous Two-way MIMO Relaying", submitted after minor revision to IEEE Trans. Wireless Commun.

<sup>8</sup> Rohit Budhiraja and Bhaskar Ramamurthi "Multiuser Two-Way Non-Regenerative MIMO Relaying With Non-Concurrent Traffic", accepted in Trans. Vehicular Tech., 2014

# Our work – two different designs

- Design a precoder at relay to cancel back-propagating interference.<sup>9</sup>
  - ▶ Assume **relay alone** has global channel knowledge.
  - ▶ Both BS and RUE use SIC to detect data; SIC can lead to errors.
  - ▶ Discussed in the first seminar.
- Joint precoder and receiver design.<sup>10</sup>
  - ▶ Assume **all nodes** have global channel knowledge.
  - ▶ Diagonalizes MIMO channels. SIC is not required.
  - ▶ Realizes beamforming gain over relay precoder.
  - ▶ Consider multi-user extension.

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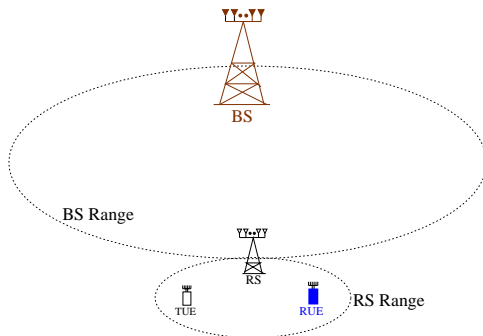
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# Classification of relays

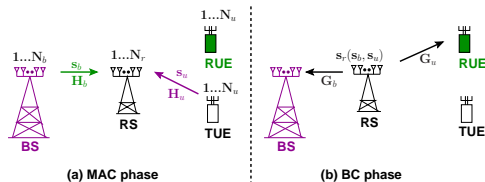
- Classified based on relay receive processing.
- **Amplify-forward**: Relay Tx signal:  $\mathbf{x}_r = \mathbf{W}\mathbf{y}_r = \mathbf{W}\mathbf{H}\mathbf{x} + \mathbf{W}\mathbf{n}_r$ .
- Amplify-forward relay **amplifies noise** but introduces minimal latency.
- **Decode-forward**: Relay decodes data. Relay Tx signal:  $\mathbf{x}_r = \mathbf{P}\mathbf{x}_d$ .
- Decode-forward relay removes noise but introduces considerable latency.

# System model (1)

- We consider an amplify and forward relay.
- No direct links between the BS and two users.
- Users observe this channel in coverage-extension/coverage-hole scenarios.

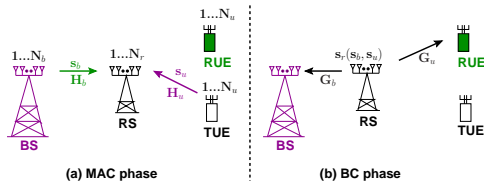


# System model (2)



- TUE and BS transmit precoded signals:  $\mathbf{s}_u = \mathbf{B}_u \mathbf{x}_u$  and  $\mathbf{s}_b = \mathbf{B}_b \mathbf{x}_b$ .
- Relay signals:
  - ▶ MAC phase received signal:  $\mathbf{y}_r = \mathbf{H}_u \mathbf{s}_u + \mathbf{H}_b \mathbf{s}_b + \mathbf{n}_r$ .
  - ▶ BC phase transmit signal:  $\mathbf{s}_r = \mathbf{W} \mathbf{y}_r$ .
- BC phase receive signal:
  - ▶ RUE:  $\mathbf{y}_u = \mathbf{G}_u \mathbf{s}_r + \mathbf{n}_u = \mathbf{G}_u \mathbf{W} \mathbf{H}_u \mathbf{s}_u + \mathbf{G}_u \mathbf{W} \mathbf{H}_b \mathbf{s}_b + \tilde{\mathbf{n}}_u$ .
  - ▶ BS:  $\mathbf{y}_b = \mathbf{G}_b \mathbf{s}_r + \mathbf{n}_b = \mathbf{G}_b \mathbf{W} \mathbf{H}_u \mathbf{s}_u + \mathbf{G}_b \mathbf{W} \mathbf{H}_b \mathbf{s}_b + \tilde{\mathbf{n}}_b$ .

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# Relay precoder design to cancel back-propagating interference

- Precoder  $\mathbf{W}$  is decomposed as  $\mathbf{W} = \mathbf{MDF}$ .
  - ▶  $\mathbf{M} = [\mathbf{M}_u \ \mathbf{M}_b]$  and  $\mathbf{F} = [\mathbf{F}_u; \ \mathbf{F}_b]$  are designed to cancel RUE's BI.
  - ▶  $\mathbf{D} = \text{anti-diag}(\mathbf{D}_u, \mathbf{D}_b)$  is used to diagonalize MIMO channels.
- Signal received by RUE and BS after substituting  $\mathbf{W} = \mathbf{MDF}$ :

$$\mathbf{y} = [\mathbf{y}_u; \mathbf{y}_b] = \mathbf{GWHs} + \tilde{\mathbf{n}} = \underbrace{\mathbf{GM}}_{\tilde{\mathbf{G}}} \underbrace{\mathbf{DFH}}_{\tilde{\mathbf{H}}} \mathbf{s} + \tilde{\mathbf{n}} = \tilde{\mathbf{G}}\tilde{\mathbf{D}}\tilde{\mathbf{H}}\mathbf{s} + \tilde{\mathbf{n}}$$

- Block matrices:  $\tilde{\mathbf{G}} = \begin{bmatrix} \tilde{\mathbf{G}}_u & \tilde{\mathbf{G}}_0 \\ \tilde{\mathbf{G}}_n & \tilde{\mathbf{G}}_b \end{bmatrix}$  and  $\tilde{\mathbf{H}} = \begin{bmatrix} \tilde{\mathbf{H}}_b & \tilde{\mathbf{H}}_n \\ \tilde{\mathbf{H}}_0 & \tilde{\mathbf{H}}_u \end{bmatrix}$ .

# Design criterion for precoders **M** and **F**

Lemma: To cancel RUE's BI alone, design **M** and **F** such that  $\tilde{\mathbf{G}}$  and  $\tilde{\mathbf{H}}$  are block lower- and upper-triangular matrices, respectively.

Proof: Recall  $\mathbf{y} = [\mathbf{y}_u; \mathbf{y}_b] = \tilde{\mathbf{G}}\mathbf{D}\tilde{\mathbf{H}}\mathbf{s} + \tilde{\mathbf{n}}$ . With lower/upper-triangular  $\tilde{\mathbf{G}}/\tilde{\mathbf{H}}$ ,

$$\begin{bmatrix} \mathbf{y}_u \\ \mathbf{y}_b \end{bmatrix} = \begin{bmatrix} (\tilde{\mathbf{G}}_u \mathbf{D}_u \tilde{\mathbf{H}}_u) \mathbf{s}_b \\ (\tilde{\mathbf{G}}_b \mathbf{D}_b \tilde{\mathbf{H}}_b) \mathbf{s}_u + (\tilde{\mathbf{G}}_n \mathbf{D}_u \tilde{\mathbf{H}}_u + \tilde{\mathbf{G}}_b \mathbf{D}_b \tilde{\mathbf{H}}_n) \mathbf{s}_b \end{bmatrix} + \tilde{\mathbf{n}}. \quad (1)$$

- RUE receive signal:  $\mathbf{y}_u = (\tilde{\mathbf{G}}_u \mathbf{D}_u \tilde{\mathbf{H}}_u) \mathbf{s}_b + \tilde{\mathbf{n}}_u$ .
- BS received signal (after BI cancellation):  $\mathbf{y}_b = (\tilde{\mathbf{G}}_b \mathbf{D}_b \tilde{\mathbf{H}}_b) \mathbf{s}_u + \tilde{\mathbf{n}}_b$ .
- Precoders **M** and **F** are designed based on null-space projection.
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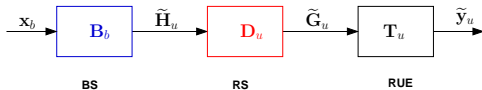
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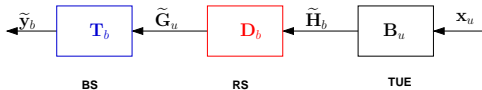
# Objectives achieved with previous lemma

- 1 Cancelled RUE's BI alone.
- 2 Decoupled a **two-way** relay channel into two **non-interfering one-way** relay channels:

- Downlink (BS $\rightarrow$ RS $\rightarrow$ RUE):



- Uplink (TUE $\rightarrow$ RS $\rightarrow$ BS):



# Downlink joint transceiver design



- Design  $\mathbf{B}_b$ ,  $\mathbf{D}_u$  and  $\mathbf{T}_u$  to diagonalize BS $\rightarrow$ RS $\rightarrow$ RUE MIMO channel.

► Recall, we assume all nodes have global CSI.

- Perform SVD of  $\tilde{\mathbf{H}}_u = \mathbf{U}_h \mathbf{\Sigma}_h \mathbf{V}_h^H$  and  $\tilde{\mathbf{G}}_u = \mathbf{U}_g \mathbf{\Sigma}_g \mathbf{V}_g^H$  and choose:

$$\mathbf{B}_b = \mathbf{U}_h^H, \quad \mathbf{D}_u = \mathbf{V}_h \mathbf{\Delta}_u \mathbf{U}_g^H, \quad \mathbf{T}_u = \mathbf{V}_g.$$

- Diagonalized MIMO channel:  $\tilde{\mathbf{y}}_u = \mathbf{\Sigma}_g \mathbf{\Delta}_u \mathbf{\Sigma}_h \mathbf{x}_b + \mathbf{T}_u \tilde{\mathbf{n}}_u$ .

- Open problem – structure is optimal for one-way relay. Optimal for ATWR?

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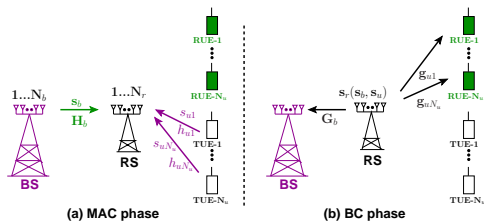
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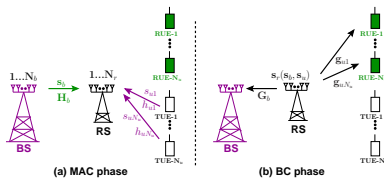
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# Multi-user asymmetric two-way relaying



- RUE- $n$  experiences
  - ▶ Back-propagating interference from the MAC-phase transmission of TUEs.
  - ▶ Co-channel interference from data transmitted by BS to other  $N_u - 1$  RUEs.
- RUEs receive interference-free signal by slightly modifying earlier design.

# Multi-user asymmetric two-way relaying



- Relay signals:

► MAC phase:  $\mathbf{y}_r = \mathbf{H}_b \mathbf{s}_b + \sum_{i=1}^{N_u} \mathbf{h}_{ui} s_{ui} + \mathbf{n}_r$ ; and BC phase:  $\mathbf{s}_r = \mathbf{W} \mathbf{y}_r$

- RUE- $n$  receive signal:

►  $y_{un} = \mathbf{g}_{un}^T \mathbf{s}_r = \mathbf{g}_{un}^T \mathbf{W} (\mathbf{h}_{bi} s_{bi} + \underbrace{\sum_{i \neq n} \mathbf{h}_{bi} s_{bi}}_{\text{CCI}} + \underbrace{\sum_{i=1}^{N_u} \mathbf{h}_{ui} s_{ui}}_{\text{BI}} + \tilde{n}_{un}).$

- Relay precoder  $\mathbf{W}$  is designed to cancel BI.

# Decoupling of channels in single-user scenario

- Relay precoder decouples two-way channel in two one-way relay channels.

- Downlink one-way relay channel:

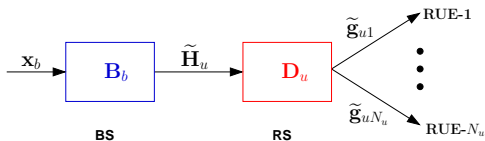


- Uplink one-way relay channel:

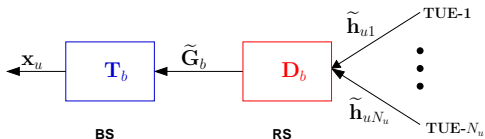


# Decoupling of channels in multi-user scenario

- Relay precoder decouples two-way channel in two one-way relay channels.
  - Relay broadcast channel in downlink:



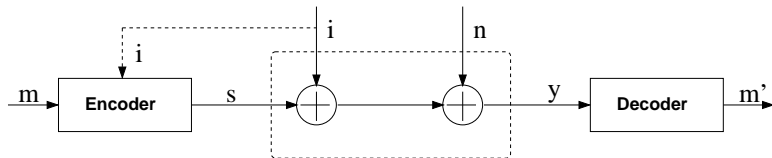
- Relay MAC channel in uplink:





# Dirty-paper-coding for point-to-point scalar channels

- Consider the following scalar interference channel  $y = s + i + n$ 
  - $i$  and  $n$  are independent Gaussian random variables.

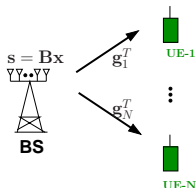


## Theorem (Dirty Paper Coding)

*If interference  $i$  is known non-casually at the transmitter then the capacity of the Gaussian channel is the same as if  $i$  were not present.*

# DPC for vector broadcast channels (ZF-DPC)

- Consider the vector broadcast channel:



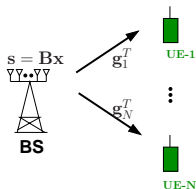
- Signal received by UE- $n$ :

$$\blacktriangleright y_n = \mathbf{g}_n^T \mathbf{B} \mathbf{x} + n_n = \mathbf{g}_n^T \mathbf{b}_n x_n + \underbrace{\sum_{j \neq n} \mathbf{g}_n^T \mathbf{b}_j x_j}_{\text{CCI}} + n_n$$

- Stacked signals of UE- $n, \forall n$ :  $\mathbf{y} = \mathbf{G} \mathbf{B} \mathbf{x} + \mathbf{n}$ .

# DPC for vector broadcast channels (ZF-DPC)<sup>11</sup>

- Consider the vector broadcast channel:



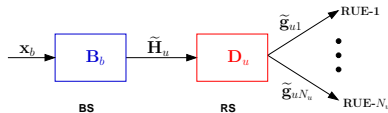
- In ZF-DPC,  $\mathbf{G}$  is decomposed as  $\mathbf{G} = \mathbf{L}\mathbf{Q}$ . And precoder  $\mathbf{B} = \mathbf{Q}^H$ .
- Equivalently  $\mathbf{y} = \mathbf{G}\mathbf{B}\mathbf{x} + \mathbf{n} = \mathbf{L}\mathbf{x} + \mathbf{n}$ :

$$\begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \begin{bmatrix} \times & 0 & 0 & 0 \\ \times & \times & 0 & 0 \\ \times & \times & \times & 0 \\ \times & \times & \times & \times \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} + \mathbf{n}. \quad (2)$$

<sup>11</sup>G. Caire and S. Shamai, On the achievable throughput of a multiantenna Gaussian broadcast channel, IEEE Trans. Inf. Theory, Jul. 2003.

# Downlink transceiver design

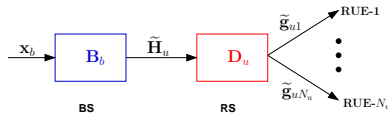
- After BI cancellation, downlink is one-way relay broadcast channel:



- Signals received by RUE- $n, \forall n$ :  $\mathbf{y}_u = \tilde{\mathbf{G}}_u \mathbf{D}_u \tilde{\mathbf{H}}_u \mathbf{B}_b \mathbf{x}_b + \tilde{\mathbf{n}}_u$ .
- Design BS and RS precoders such that BS employs DPC to cancel CCI.
  - Perform SVD of  $\tilde{\mathbf{H}}_u = \mathbf{U}_h \Sigma_h \mathbf{V}_h^H$  and LQ dec. of  $\tilde{\mathbf{G}}_u = \mathbf{L}_g \mathbf{Q}_g$ .
  - Choose  $\mathbf{B}_b = \mathbf{U}_h^H$  and  $\mathbf{D}_u = \mathbf{Q}_g^H \Delta_u \mathbf{V}_h$ .
- Lower-triangular MIMO channel:  $\mathbf{y}_u = \mathbf{L}_g \Delta_u \Sigma_h \mathbf{x}_b + \tilde{\mathbf{n}}_u$ .

# Downlink transceiver design

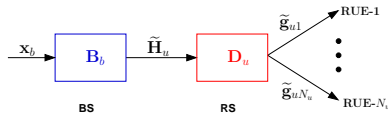
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# Downlink transceiver design

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# SNR experienced by BS and RUE

- SNR observed by the  $m$ th stream received by the RUE and BS:

$$\text{SNR}_i^m = \frac{a_i^m \delta_{i,m}}{\sigma_r^2 (\sum_{k=1}^M b_{i,k}^m \delta_{u,k} + c_{i,k}^m \delta_{b,k}) + \sigma^2}.$$

- Here  $\{a_i^m, b_{i,k}^m, c_{i,k}^m\} \geq 0$ .
- Note that coefficients of power allocation variables  $\delta_{u,k}$  and  $\delta_{b,k}$  are positive.
- Fact will be used to prove the convexity of sum-rate optimization program.
  - ▶  $R_{\text{sum}}(\delta) = \frac{1}{2} \sum_{m=1}^M \log(1 + \text{SNR}_u^m(\delta)) + \log(1 + \text{SNR}_b^m(\delta))$

# Sum-rate maximization

- Will cast sum-rate max. as a **geometric program**; we explain its terminology.

- A **monomial** is a function  $f : \mathbf{R}_{++}^n \rightarrow \mathbf{R}$  of the form

$$f(\mathbf{x}) = cx_1^{a_1}x_2^{a_2}\cdots x_n^{a_n}, \text{ where } c > 0 \text{ and } a_j \in \mathbf{R}.$$

- A positive sum of monomials is called a **posynomial**:

$$f(\mathbf{x}) = \sum_{k=1}^K c_k x_1^{a_{1k}} x_2^{a_{2k}} \cdots x_n^{a_{nk}}, \text{ where } c_k > 0$$

- Posynomials are closed under addition & multiplication, not under division.
- In a GP, the objective function and inequality constraints are posynomials.



# Sum-rate maximization subject to relay power constraint

- Optimization problem can be cast as:

$$\begin{aligned} \text{Max.}_{\delta: \delta \succeq 0} \quad & R_{\text{sum}}(\delta) \\ \text{s.t.} \quad & P(\delta) \leq P_r \end{aligned} \tag{3}$$

- To cast (3) as a GP, both  $R_{\text{sum}}(\delta)$  and  $p_r(\delta)$  must be posynomials.
- Relay power  $p_r(\delta)$  is a posynomial.<sup>12</sup> We show that  $R_{\text{sum}}$  is not a posynomial.

$$\begin{aligned} R_{\text{sum}}(\delta) &= \frac{1}{2} \sum_{m=1}^M \log(1 + \text{SNR}_u^m(\delta)) + \log(1 + \text{SNR}_b^m(\delta)) \\ &= \frac{1}{2} \log \left[ \prod_m (1 + \text{SNR}_u^m(\delta))(1 + \text{SNR}_b^m(\delta)) \right]. \end{aligned}$$

<sup>12</sup>Rohit Budhiraja, Karthik KS and Bhaskar Ramamurthi "Linear Precoders for Non-Regenerative Asymmetric Two-way Relaying in Cellular Systems", IEEE Trans. Wireless Commun., vol. 13, pp. 50025014, Sep. 2014

# Sum-rate maximization

- Recall SNR observed by the  $m$ th stream received by the RUE and BS:

$$\text{SNR}_i^m = \frac{a_i^m \delta_{i,m}}{\sigma_r^2 (\sum_{k=1}^M b_{i,k}^m \delta_{u,k} + c_{i,k}^m \delta_{b,k}) + \sigma^2}.$$

- Here  $\{a_i^m, b_{i,k}^m, c_{i,k}^m\} \geq 0$ . Equivalently  $\text{SNR}_i^m = \frac{\text{monomial}}{\text{posynomial}}$ .
- Sum-rate:  $R_{\text{sum}}(\delta) = \frac{1}{2} \log \prod (1 + \text{SNR}_u^m(\delta))(1 + \text{SNR}_b^m(\delta))$ .
- $R_{\text{sum}}$  is a ratio of two posynomials – not a posynomial.
  - Sum-rate maximization is not a GP.

# Sum-rate maximization

- Use high SNR approximation:  $\log(1 + \text{SNR}) \simeq \log(\text{SNR})$ .

- Therefore

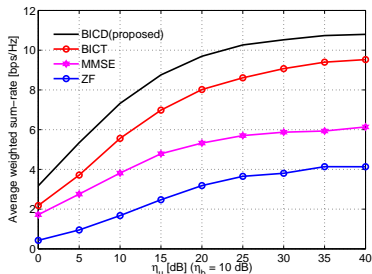
▶  $R_{\text{sum}} \simeq \frac{1}{2} \log \left[ \prod_m \text{SNR}_u^m(\delta) \text{SNR}_b^m(\delta) \right] = -\frac{1}{2} \log \left[ \prod_m \text{ISNR}_u^m(\delta) \text{ISNR}_b^m(\delta) \right].$

▶ Here  $\text{ISNR}_u^m = 1/\text{SNR}_u^m$ . Note that  $\text{ISNR} = \frac{\text{posynomial}}{\text{monomial}}$  is a posynomial.

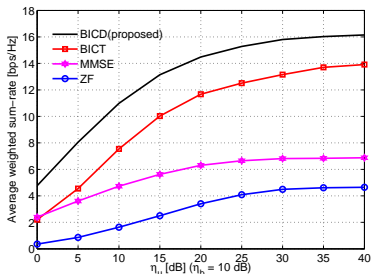
- Sum-rate maximization can now be cast as a GP:

$$\begin{aligned} & \underset{\delta \succeq 0}{\text{Min.}} && \prod_m \text{ISNR}_u^m(\delta) \text{ISNR}_b^m(\delta) \\ & \text{s.t.} && p_r(\delta) \leq P_r. \end{aligned}$$

# Sum-rate comparison of different precoders



(a)  $N_r = 4$  and  $N_u = N_b = 2$ .



(b)  $N_r = 8$  and  $N_u = N_b = 4$ .

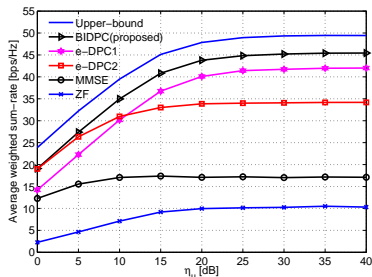
- Precoders – BICD,<sup>13</sup> BICT<sup>14</sup> and ZF/MMSE.<sup>15</sup>

<sup>13</sup> Budhiraja et. al. "Joint Precoder/Receiver Design for AF Non-Simultaneous Two-way MIMO Relaying", Trans. Wireless Commun.

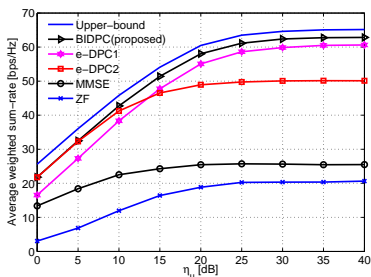
<sup>14</sup> Budhiraja et. al. "Linear Precoders for Non-Regenerative Asymmetric Two-way Relaying in Cellular Systems", Trans. Wireless Commun., Sep. 2014

<sup>15</sup> Unger et. al. "Duplex schemes in multiple antenna two-hop relaying", EURASIP J. Adv. Signal Process., vol. 2008, pp. 114, 2008.

# Sum-rate comparison for multi-user ATWR



(c) With  $\eta_b = 15$  dB.



(d) With  $\eta_b = 20$  dB.

- Precoders – BIDPC,<sup>16</sup> e-DPC1,<sup>17</sup> e-DPC2,<sup>18</sup> and ZF/MMSE.<sup>19</sup>

<sup>16</sup>Budhiraja et. al. "Joint Precoder/Receiver Design for AF Non-Simultaneous Two-way MIMO Relaying", Trans. Wireless Commun.

<sup>17</sup>Budhiraja et. al. "Multiuser Two-Way MIMO Relaying With Non-Concurrent Traffic", Trans. Vehicular Tech., 2014

<sup>18</sup>Zhang et. al., "Beamforming design for multi-user two-way relaying with MIMO amplify and forward relays", ICASSP, 2011.

<sup>19</sup>Joung et. al. "User selection methods for multiuser two-way relay communications using space division multiple access", IEEE Trans. Wireless Commun., Jul. 2010.

# Conclusions

- Considered problem of asymmetric data-flow in two-way relaying.
- Designed a novel precoder to selectively cancel back-propagating interference.
- Maximized sum-rate using geometric programming.
- Proposed precoder outperforms conventional precoders.