Precoder Design for Asymmetric Two-way AF Shared Relay

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¹Rankov, B and Wittneben, A, "Spectral Efficient Protocols for Half-Duplex Fading Relay Channels", IEEE J. Sel. Areas Commun, vol. 25, no. 2, pp. 375–385, 2007.

Two-way relaying

Two source nodes simultaneously transmit to the relay during first phase.

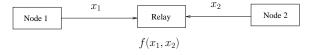


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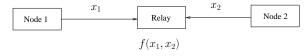


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Relay broadcasts a function of the sum-signal during second phase.

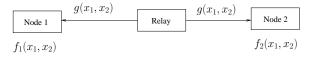


Figure: Broadcast phase of two-way relaying

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- Two-way relaying will reduce to conventional one-way relaying.

Asymmetric Two-way relaying

• Consider infrastructure relay scenario, where multiple UEs are served through a relay.

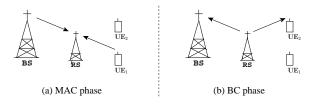


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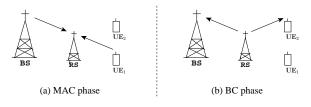


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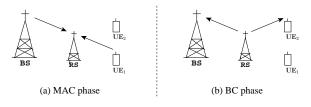


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- \bullet UE₁ has data to be sent to the BS. UE₂ wants to receive data from BS.

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- We have proposed a precoder to cancel the asymmetric back-propagating interference for UE₂.²
- Proposed precoder is shown to be better than the conventional ZF and MMSE precoders.

Asymmetric Two-way relaying for a shared relay

• Data-flow asymmetry problem is extended to shared relay in this work.³

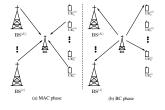


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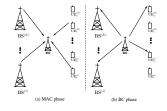


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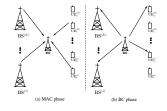


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- Signal transmit by the relay: $\mathbf{x}_r = \mathbf{W}\mathbf{y}_r$.



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- $\mathbf{D} = \mathsf{diag}\{\mathbf{D}_1, \mathbf{D}_2, \cdots, \mathbf{D}_K\}$. Permutation matrix \mathbf{D}_k is given as:
 - $\mathbf{D}_k = \begin{bmatrix} 0 & \beta \\ \beta & 0 \end{bmatrix}$. β is used to normalize the relay power.



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- IUI-free channel can be viewed as multiple single-user-pair systems.

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- Signal received by UE₂ and BS during the BC phase are re-written as:

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Sum-rate comparison between proposed and ZF precoder

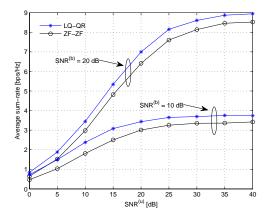


Figure: Average sum-rate comparison with two BSs and number of relay antennas = 4.

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