

Two-way MIMO DF Relaying for Non-Simultaneous Traffic in Cellular Systems

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Background

- Cooperative communication vastly improves performance of wireless systems.
- Half-duplex one-way relaying is an example.¹
- Half-duplex constraint is imposed on the relay (**easy to design**)
 - ▶ Relay cannot concurrently transmit and receive on same resource.

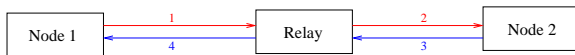


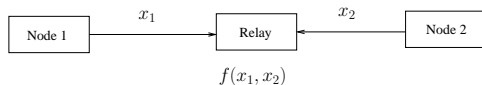
Figure: One-way relaying protocol.

- Four channel uses are required to exchange two data units.

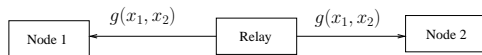
¹ L. Sanguinetti, A. D'Amico, and Y. Rong, A tutorial on the optimization of amplify-and-forward MIMO relay systems, IEEE J. Sel. Areas Commun., vol. 30, pp. 1331-1346, Sep. 2012.

Half-duplex two-way relaying²

- Two source nodes simultaneously transmit to the relay during first phase.



- Relay broadcasts a function of the sum-signal during second phase.



- Both nodes can cancel back-propagating interference as both know self-data.
- Two channel uses are required to exchange two data units

²Y. Rong, Joint source and relay optimization for two-way linear non-regenerative MIMO relay communications, IEEE Trans. Signal Process., vol. 60, pp. 65336546, Dec. 2012.

Basic assumption in two-way relaying

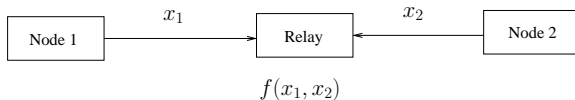


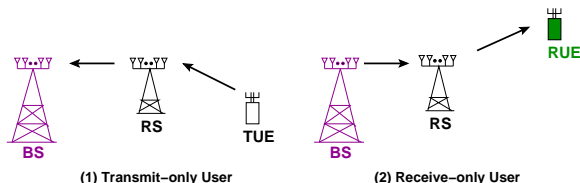
Figure: First phase of two-way relaying

Two nodes want to exchange data via a relay.

Two flows are aggregated to establish bi-directional data flow via a relay.

Data exchange in cellular systems

- Usually does not happen!



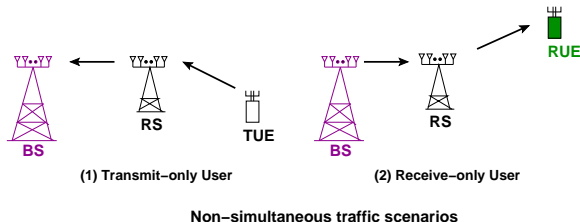
Non-simultaneous traffic scenarios

- Example 1: User TUE uploading a Youtube video.
- Example 2: User RUE watching a Netflix movie.
- Two flows cannot be aggregated to establish bi-directional data flow via relay.

Two way relaying cannot be used in these scenarios.

Option for BS to serve TUE and RUE

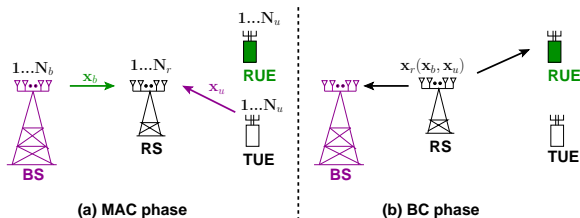
- Use one way relaying.



- One way relaying creates two non-interfering end-to-end links
 - ▶ $TUE \rightarrow RS \rightarrow BS$ and $BS \rightarrow RS \rightarrow RUE$.
- BS will require 4 time slots – spectrally inefficient.

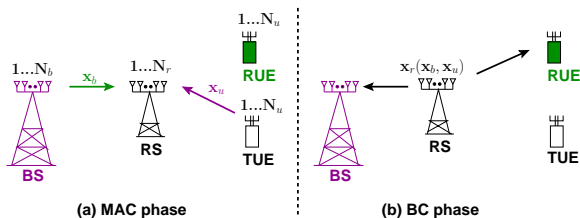
Proposed non-simultaneous two-way relaying (NS-TWR)

- Aggregates two flow to establish bi-directional data flow via relay.
- MAC phase: Both BS and TUE transmit to the relay.
- BC phase: Relay broadcasts to both BS and RUE.



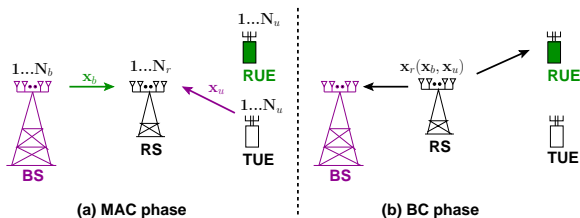
- BS requires two channel uses to serve two users.

Proposed non-simultaneous two-way relaying (NS-TWR)



- Relay Rx signal: $\mathbf{y}_r = \mathbf{H}_u \mathbf{x}_u + \mathbf{H}_b \mathbf{x}_b + \mathbf{n}_r$.
- Relay Tx signal: $\mathbf{x}_r = \mathbf{W} \mathbf{y}_r$ (for an AF relay).
- RUE Rx signal: $\mathbf{y}_u = \mathbf{G}_u \mathbf{x}_r = \mathbf{G}_u (\underbrace{\mathbf{W} \mathbf{H}_u \mathbf{x}_u}_{\text{BI}} + \mathbf{W} \mathbf{H}_b \mathbf{x}_b + \mathbf{W} \mathbf{n}_r) + \mathbf{n}_u$.
- BS Rx signal: $\mathbf{y}_b = \mathbf{G}_b \mathbf{x}_r = \mathbf{G}_b (\mathbf{W} \mathbf{H}_u \mathbf{x}_u + \underbrace{\mathbf{W} \mathbf{H}_b \mathbf{x}_b}_{\text{BI}} + \mathbf{W} \mathbf{n}_r) + \mathbf{n}_b$.

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Proposed non-simultaneous two-way relaying (NS-TWR)

- TUE \rightarrow RS \rightarrow BS link is BI-free while the BS \rightarrow RS \rightarrow RUE link experiences BI.
 - ▶ Unlike one-way relaying solution where both these links are non-interfering.

Aim: Cancel BI for BS \rightarrow RS \rightarrow RUE link.

- NS-TWR will create two non-interfering links as in one-way relaying (OWR).
- We will show that NS-TWR provides higher sum-rate than OWR.
- RUE can cancel BI by overhearing TUE's MAC-phase transmission.³
- In our work, we assume that RUE does not overhear TUE
 - ▶ Designed precoder W to cancel BI for AF relay.⁴

³ F. Sun, T. M. Kim, A. J. Paulraj, E. de Carvalho, and P. Popovski, Cell-edge multi-user relaying with overhearing, IEEE Commun. Lett., vol. 17, pp. 11601163, Jun. 2013.

⁴ Rohit Budhiraja, Karthik KS and Bhaskar Ramamurthi "Linear Precoders for Non-Regenerative Asymmetric Two-way Relaying in Cellular Systems", accepted in Trans. Wireless Commun., 2014.

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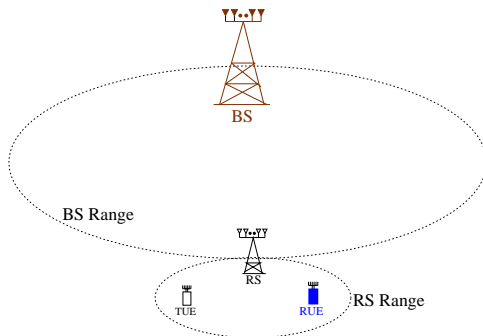
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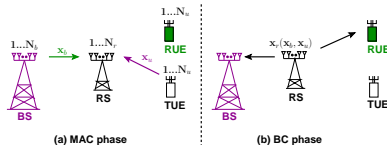
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System model for NS-TWR in present work (1)

- We consider a decode and forward relay.
- No direct links between the BS and two users.
- Users observe this channel in coverage-extension/coverage-hole scenarios.



System model for decode and forward NS-TWR (2)



- All nodes have multiple antennas.
- Relay has complete CSIT and CSIR. The BS and RUE have CSIR alone.
- Sum-signal received by the relay: $\mathbf{y}_r = \mathbf{H}_u \mathbf{x}_u + \mathbf{H}_b \mathbf{x}_b + \mathbf{n}_r$.
- Assumption: RS successfully decodes the MAC phase data.
- RS re-encodes the RUE and BS signals as \mathbf{s}_u and \mathbf{s}_b , respectively.

System model for decode and forward NS-TWR (3)

- Signal transmitted by the relay: $\mathbf{x}_r = \mathbf{W}_u \mathbf{s}_u + \mathbf{W}_b \mathbf{s}_b = \mathbf{W} \mathbf{s}$.
 - ▶ Covariance matrices of \mathbf{s}_u and \mathbf{s}_b are $\mathbf{\Lambda}_u$ and $\mathbf{\Lambda}_b$.
- RUE receive signal: $\mathbf{y}_u = \mathbf{G}_u \mathbf{W}_u \mathbf{s}_u + \underbrace{\mathbf{G}_u \mathbf{W}_b \mathbf{s}_b}_{\text{BI}} + \mathbf{n}_u$.
- BS receive signal: $\mathbf{y}_b = \underbrace{\mathbf{G}_b \mathbf{W}_u \mathbf{s}_u}_{\text{BI}} + \mathbf{G}_b \mathbf{W}_b \mathbf{s}_b + \mathbf{n}_b$.

Objectives

- 1) Design precoder \mathbf{W} to cancel BI for RUE alone.
- 2) Design $\mathbf{\Lambda}_u$ and $\mathbf{\Lambda}_b$ to maximize sum-rate – algorithm uses two SDPs.

Proposed precoder design (1)

- \mathbf{W} can be chosen as ZF/MMSE precoder. Cancels BI for both BS and RUE.
- ZF/MMSE precoders are sub-optimal as BS can itself cancel BI.

Proposed precoder design

- ▶ Cancels BI for RUE alone.
- ▶ Sum-rate performance is better than ZF/MMSE precoders.

- Stack the signals received by RUE and BS during the BC phase:

$$\begin{bmatrix} \mathbf{y}_u \\ \mathbf{y}_b \end{bmatrix} = \underbrace{\begin{bmatrix} \mathbf{G}_u \mathbf{W}_u & \mathbf{G}_u \mathbf{W}_b \\ \mathbf{G}_b \mathbf{W}_u & \mathbf{G}_b \mathbf{W}_b \end{bmatrix}}_{\tilde{\mathbf{G}}} \begin{bmatrix} \mathbf{s}_u \\ \mathbf{s}_b \end{bmatrix} + \begin{bmatrix} \mathbf{n}_u \\ \mathbf{n}_b \end{bmatrix}. \quad (1)$$

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Proposed precoder design (2)

Lemma

To cancel RUE's BI, design \mathbf{W} such that $\tilde{\mathbf{G}}$ is a block lower-triangular matrix.

With the block lower-triangular matrix, $\tilde{\mathbf{G}}$, Eq. (1) will become:

$$\begin{bmatrix} \mathbf{y}_u \\ \mathbf{y}_b \end{bmatrix} = \begin{bmatrix} \mathbf{G}_u \mathbf{W}_u & \mathbf{0} \\ \mathbf{G}_b \mathbf{W}_u & \mathbf{G}_b \mathbf{W}_b \end{bmatrix} \begin{bmatrix} \mathbf{s}_u \\ \mathbf{s}_b \end{bmatrix} + \begin{bmatrix} \mathbf{n}_u \\ \mathbf{n}_b \end{bmatrix} \quad (2)$$

$$\begin{bmatrix} \mathbf{y}_u \\ \mathbf{y}_b \end{bmatrix} = \begin{bmatrix} \mathbf{G}_u \mathbf{W}_u \mathbf{s}_u \\ \mathbf{G}_b \mathbf{W}_u \mathbf{s}_u + \mathbf{G}_b \mathbf{W}_b \mathbf{s}_b \end{bmatrix} + \begin{bmatrix} \mathbf{n}_u \\ \mathbf{n}_b \end{bmatrix} \quad (3)$$

- RUE receives its desired data \mathbf{s}_u without experiencing BI.
- As desired, BI experienced by BS is not cancelled.

Proposed precoder design (3)

- For a block lower-triangular $\tilde{\mathbf{G}} = \begin{bmatrix} \mathbf{G}_u \mathbf{W}_u & \mathbf{G}_u \mathbf{W}_b \\ \mathbf{G}_b \mathbf{W}_u & \mathbf{G}_b \mathbf{W}_b \end{bmatrix}$, $\mathbf{G}_u \mathbf{W}_b = \mathbf{0}$.

- The SVD of \mathbf{G}_u is performed to determine its nullspace:

$$\mathbf{G}_u = \mathbf{U}_{\mathbf{G}_u} \mathbf{\Sigma}_{\mathbf{G}_u} [\mathbf{V}_{\mathbf{G}_u}^{(1)} \mathbf{V}_{\mathbf{G}_u}^{(0)}]^H, \quad (4)$$

- The columns of $\mathbf{V}_{\mathbf{G}_u}^{(0)}$ form an orthonormal basis set for the nullspace of \mathbf{G}_u .
 - ▶ We choose $\mathbf{V}_{\mathbf{G}_u}^{(0)}$ as the precoder matrix \mathbf{W}_b .
- To design \mathbf{W}_u , we note that RUE receive signal $\mathbf{y}_u = \mathbf{G}_u \mathbf{W}_u \mathbf{s}_u + \mathbf{n}_u$.
 - ▶ To decode RUE signal, $\mathbf{G}_u \mathbf{W}_u \neq \mathbf{0}$ (\mathbf{W}_u should not lie in nullspace of \mathbf{G}_u).
 - ▶ Columns of $\mathbf{V}_{\mathbf{G}_u}^{(1)}$ form an orthonormal basis for the row space of \mathbf{G}_u .
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Sum-rate comparison of various precoders

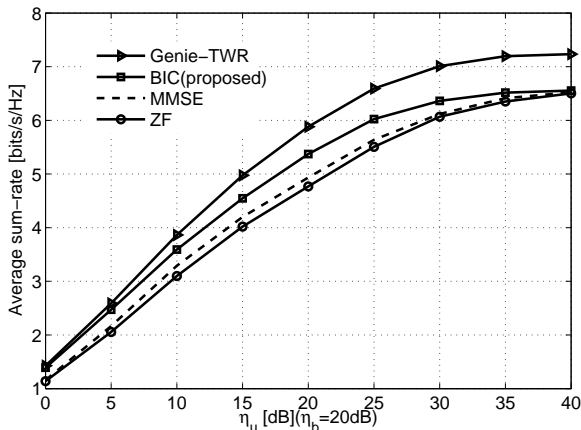
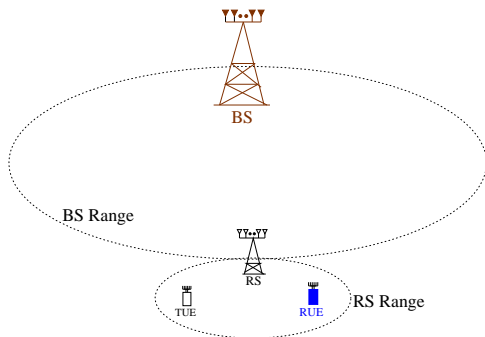


Figure: Sum-rate with 2 antennas at the RS and 1 antenna at the TUE, RUE and BS.

System-level comparison of various protocols

- Coverage extension scenario.
- Distance between BS and RS is 1 Km.
- RUE is located at the edge of RS range (500 m).



System parameters based on 802.16j methodology

System parameters	Value
System Bandwidth	10 MHz
Carrier Frequency	2 GHz
Noise Figure	5 dB
Thermal Noise	-174 dBm/Hz
BS / UE Transmit power	46 dBm / 24 dBm
BS / RS / UE height	30 m / 15 m / 1 m
BS-RS channel model	IEEE 802.16j, Type D
BS-MS / RS-UE channel model	IEEE 802.16j, Type B
RS Transmit power	37 dBm

Table: System parameters

System-level comparison of various protocols

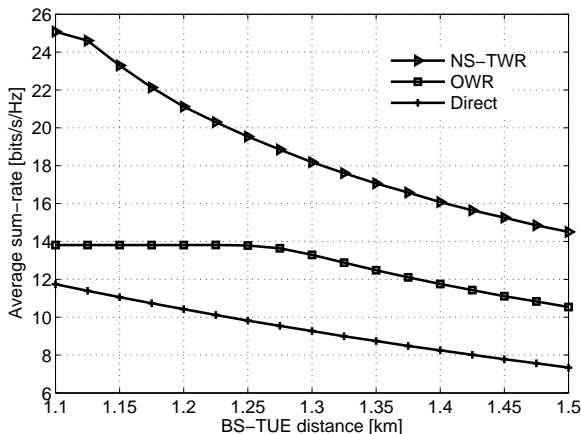


Figure: Average sum-rate comparison with 6 antennas at the RS, 3 antennas at the TUE, RUE and BS. Here BS-RUE distance = 1.5 km.

Conclusions

- Considered problem of non-simultaneous data-flow in two-way DF relaying.
- Designed a novel precoder to selectively cancel back-propagating interference.
- Maximized sum-rate using SDP-based algorithm.
- Proposed precoder outperforms conventional precoders.
- Sum-rate of proposed protocol is significantly better than OWR.

Extensions of the Work

- Designed precoder with global CSI at all the nodes.^{5 6}
- Extended the system model to include multiple such TUEs and RUEs.⁷

⁵ Rohit Budhiraja and Bhaskar Ramamurthi "Diagonalized Two-way MIMO AF Relaying for Non-Simultaneous Traffic in Cellular Systems", presented in SPAWC 2014, Toronto.

⁶ Rohit Budhiraja and Bhaskar Ramamurthi "Two-way Diagonalized MIMO AF Relaying for Non-Simultaneous Traffic in Cellular Systems", submitted to Trans. Wireless Commun. 2014.

⁷ Rohit Budhiraja and Bhaskar Ramamurthi "Multiuser Two-Way Non-Regenerative MIMO Relaying With Non-Concurrent Traffic", accepted in Trans. Vehicular Tech., 2014