

Introduction to R Software

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Lecture 10

Matrices

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Slides can be downloaded from
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Matrix

An element in the i -th row and j -th column is denoted by X_{ij} (book version) or $X[i, j]$ ("program version"), $i = 1, 2, \dots, n, j = 1, 2, \dots, p$.

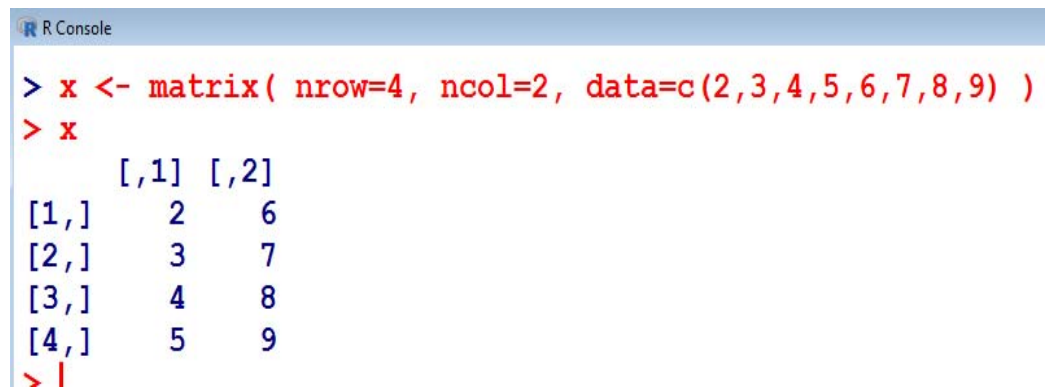
An element of a matrix can also be an object, for example a string. However, in mathematics, we are mostly interested in numerical matrices, whose elements are generally real numbers

Matrix

In R, a 4×2 -matrix X can be created with a following command:

```
> x <- matrix( nrow=4, ncol=2,  
               data=c(2,3,4,5,6,7,8,9) )
```

```
> x  
      [,1] [,2]  
[1,]    2    6  
[2,]    3    7  
[3,]    4    8  
[4,]    5    9
```



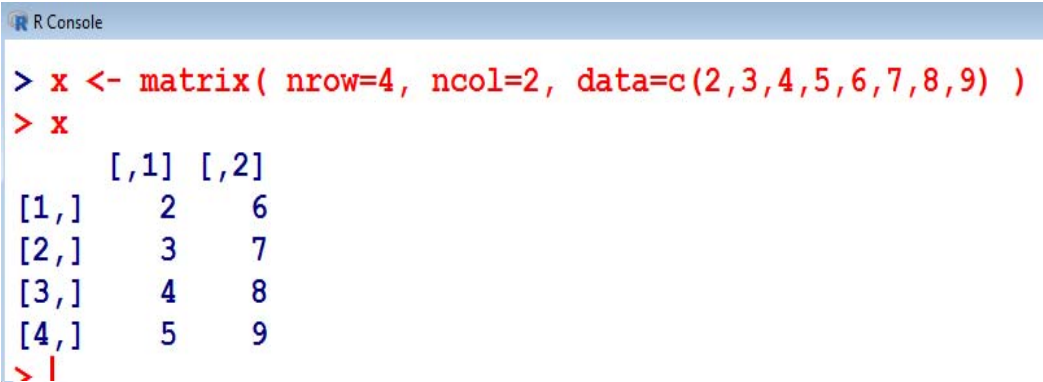
```
R Console  
> x <- matrix( nrow=4, ncol=2, data=c(2,3,4,5,6,7,8,9) )  
> x  
      [,1] [,2]  
[1,]    2    6  
[2,]    3    7  
[3,]    4    8  
[4,]    5    9  
> |
```

Matrix

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```
R Console  
> x <- matrix( nrow=4, ncol=2, data=c(2,3,4,5,6,7,8,9) )  
> x  
      [,1] [,2]  
[1,]    2    6  
[2,]    3    7  
[3,]    4    8  
[4,]    5    9  
> |
```

Matrix

We see:

The parameter `nrow` defines the row number of a matrix.

The parameter `ncol` defines the column number of a matrix.

The parameter `data` assigns specified values to the matrix elements.

The values from the parameters are written column-wise in matrix.

Matrix

```
> x
```

```
      [,1] [,2]  
[1,]    2    6  
[2,]    3    7  
[3,]    4    8  
[4,]    5    9
```

```
R Console  
> x <- matrix( nrow=4, ncol=2, data=c(2,3,4,5,6,7,8,9) )  
> x  
      [,1] [,2]  
[1,]    2    6  
[2,]    3    7  
[3,]    4    8  
[4,]    5    9  
> |
```

One can access a single element of a matrix with `x[i,j]`:

```
> x[4,2]
```

```
[1] 9
```

Matrix

```
> x
```

```
      [,1] [,2]  
[1,]    2    6  
[2,]    3    7  
[3,]    4    8  
[4,]    5    9
```

```
R Console  
> x <- matrix( nrow=4, ncol=2, data=c(2,3,4,5,6,7,8,9) )  
> x  
      [,1] [,2]  
[1,]    2    6  
[2,]    3    7  
[3,]    4    8  
[4,]    5    9  
> |
```

One can access a single element of a matrix with `x[i,j]`:

```
> x[2,1]  
[1] 3
```

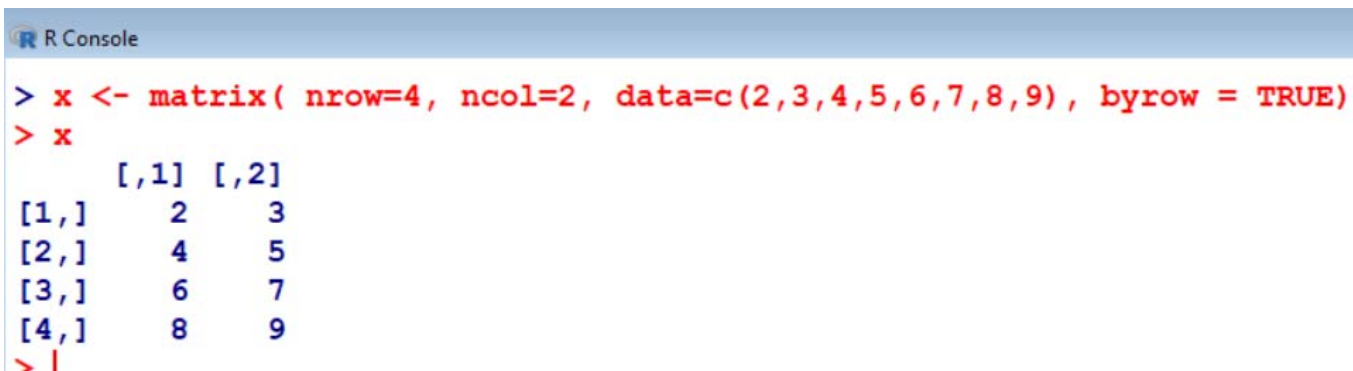
```
R Console  
> x[2,1]  
[1] 3  
>
```

Matrix

In case, the data has to be entered row wise, then a 4×2 -matrix X can be created with

```
> x <- matrix( nrow=4, ncol=2,  
              data=c(2,3,4,5,6,7,8,9), byrow = TRUE)
```

```
> x  
      [,1] [,2]  
[1,]    2    3  
[2,]    4    5  
[3,]    6    7  
[4,]    8    9
```



```
R Console  
> x <- matrix( nrow=4, ncol=2, data=c(2,3,4,5,6,7,8,9), byrow = TRUE)  
> x  
      [,1] [,2]  
[1,]    2    3  
[2,]    4    5  
[3,]    6    7  
[4,]    8    9  
> |
```


Matrix

R Console

```
> x <- matrix( nrow=4, ncol=2, data=c(2,3,4,5,6,7,8,9))
```

```
> x
```

```
      [,1] [,2]  
[1,]    2    6  
[2,]    3    7  
[3,]    4    8  
[4,]    5    9
```

```
>
```

```
> x <- matrix( nrow=4, ncol=2, data=c(2,3,4,5,6,7,8,9),byrow = TRUE)
```

```
> x
```

```
      [,1] [,2]  
[1,]    2    3  
[2,]    4    5  
[3,]    6    7  
[4,]    8    9
```

```
>
```

Properties of a Matrix

We can get specific *properties* of a matrix:

`> dim(x)` # tells the dimension of matrix

`[1] 4 2`

```
R Console
> x <- matrix( nrow=4, ncol=2, data=c(2,3,4,5,6,7,8,9))
> x
      [,1] [,2]
[1,]    2    6
[2,]    3    7
[3,]    4    8
[4,]    5    9
>
```

`> nrow(x)` # tells the number of rows

`[1] 4`

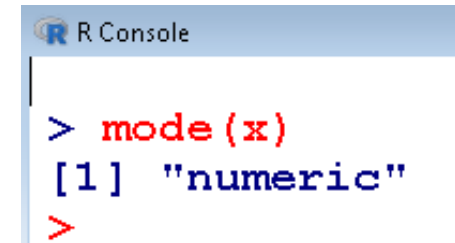
```
R Console
> dim(x)
[1] 4 2
>
> nrow(x)
[1] 4
>
> ncol(x)
[1] 2
>
```

`> ncol(x)` # tells the number of columns

`[1] 2`

Properties of a Matrix

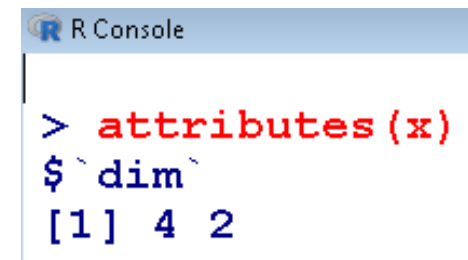
```
> mode(x)           # Informs the type or storage
[1] "numeric"       mode of an object, e.g.,
                    numerical, logical etc.
```



```
R Console
> mode(x)
[1] "numeric"
>
```

`attributes` provides all the attributes of an object

```
> attributes(x) #Informs the dimension of matrix
$dim [1] 4 2
```



```
R Console
> attributes(x)
$`dim`
[1] 4 2
```

Help on the Object "Matrix"

To know more about these important objects, we use R-help on "matrix".

```
> help("matrix")
```

```
matrix      package:base      R Documentation
```

Matrices

Description:

'**matrix**' creates a matrix from the given set of values.

'**as.matrix**' attempts to turn its argument into a matrix.

'**is.matrix**' tests if its argument is a (strict) matrix. It is generic:

you can write methods to handle specific classes of objects, see

Internal Methods.

Help on the Object "Matrix"

Arguments:

data: an optional data vector.

nrow: the desired number of rows

ncol: the desired number of columns

byrow: logical. If '**FALSE**' (the default) the matrix is filled by columns, otherwise the matrix is filled by rows.

dimnames: A '**dimnames**' attribute for the matrix: a '**list**' of length 2.

x: an R object.

Help on the Object "Matrix"

Then, the meaning of each parameter is explained:

Details:

If either of `'nrow'` or `'ncol'` is not given, an attempt is made to infer it from the length of `'data'` and the other parameter.

If there are too few elements in `'data'` to fill the array, then the elements in `'data'` are recycled. If `'data'` has length zero, `'NA'` of an appropriate type is used for atomic vectors and `'NULL'` for lists.

`'is.matrix'` returns `'TRUE'` if `'x'` is a matrix (i.e., it is `_not_` a `'data.frame'` and has a `'dim'` attribute of length 2) and `'FALSE'` otherwise.

Help on the Object "Matrix"

'`as.matrix`' is a generic function. The method for data frames will convert any non-numeric/complex column into a character vector using '`format`' and so return a character matrix, except that all-logical data frames will be coerced to a logical matrix.

Finally, references and cross-references are displayed...

References:

Becker, R. A., Chambers, J. M. and Wilks, A.R. (1988) The New S Language. Wadsworth & Brooks/Cole.

Help on the Object "Matrix"

See Also:

'`data.matrix`', which attempts to convert to a numeric matrix.

.. as well as an example:

Examples:

```
is.matrix(as.matrix(1:10))
data(warpbreaks)
!is.matrix(warpbreaks) # data.frame, NOT matrix!
warpbreaks[1:10,]
as.matrix(warpbreaks[1:10,]) #using
  as.matrix.data.frame(.) method
```