

Introduction to R Software

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Lecture 12

Matrix Operations and Missing Data

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Slides can be downloaded from
<http://home.iitk.ac.in/~shalab/sp>

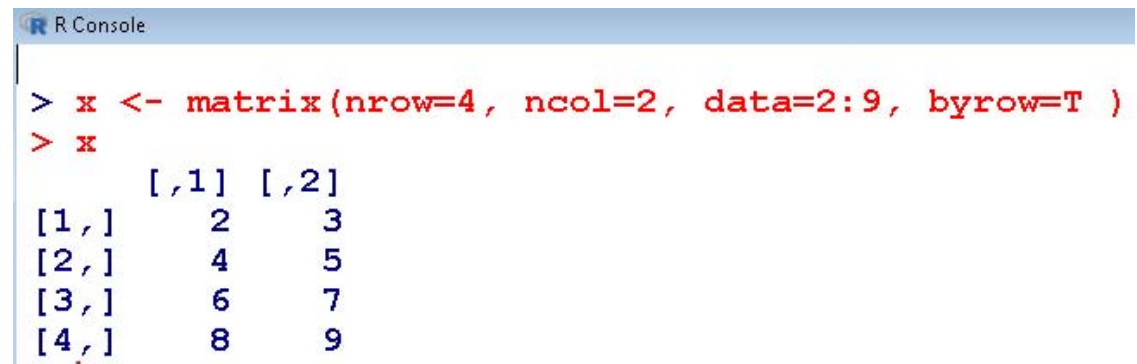


Transpose of a matrix X: X'

```
> x <- matrix(nrow=4, ncol=2, data=2:9, byrow=T )
```

```
> x
```

	[,1]	[,2]
[1,]	2	3
[2,]	4	5
[3,]	6	7
[4,]	8	9



```
R Console  
> x <- matrix(nrow=4, ncol=2, data=2:9, byrow=T )  
> x  
      [,1] [,2]  
[1,]    2    3  
[2,]    4    5  
[3,]    6    7  
[4,]    8    9
```

Transpose of a matrix X : X'

```
> xt <- t(x)
```

```
> xt
```

```
      [,1] [,2] [,3] [,4]
[1,]    2    4    6    8
[2,]    3    5    7    9
```

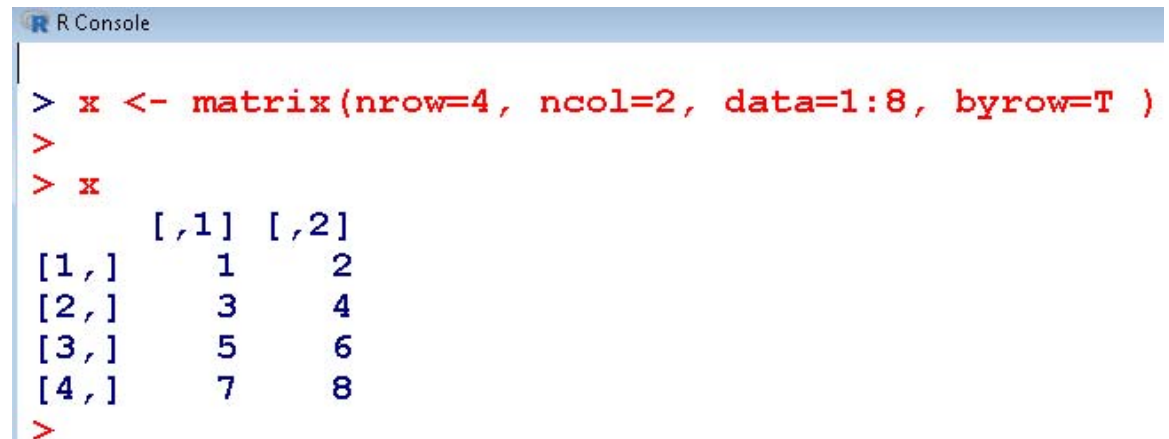
```
R Console
> xt <- t(x)
> xt
      [,1] [,2] [,3] [,4]
[1,]    2    4    6    8
[2,]    3    5    7    9
>
```

Multiplication of a matrix with a constant

```
> x <- matrix(nrow=4, ncol=2, data=1:8, byrow=T )
```

```
> x
```

```
      [,1] [,2]  
[1,]    1    2  
[2,]    3    4  
[3,]    5    6  
[4,]    7    8
```



```
R Console  
> x <- matrix(nrow=4, ncol=2, data=1:8, byrow=T )  
>  
> x  
      [,1] [,2]  
[1,]    1    2  
[2,]    3    4  
[3,]    5    6  
[4,]    7    8  
>
```

Multiplication of a matrix with a constant

```
> 4*x
```

	[,1]	[,2]
[1,]	4	8
[2,]	12	16
[3,]	20	24
[4,]	28	32

```
R Console  
> 4*x  
      [,1] [,2]  
[1,]    4    8  
[2,]   12   16  
[3,]   20   24  
[4,]   28   32  
>
```

Matrix multiplication: operator %*%

Consider the multiplication of X' with X

```
> xtx <- t(x) %*% x
```

```
> xtx
```

```
      [,1] [,2]  
[1,]   84  100  
[2,]  100  120
```

```
R Console  
> xtx <- t(x) %*% x  
>  
> xtx  
      [,1] [,2]  
[1,]   84  100  
[2,]  100  120
```

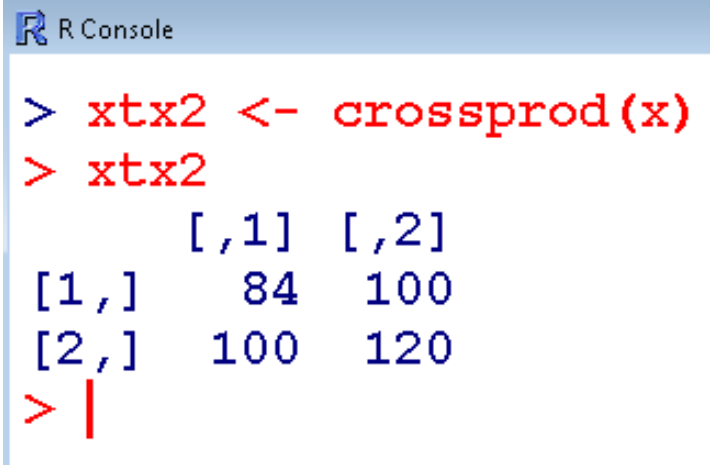
Cross product of a matrix X - $X'X$ with a function

`crossprod`

```
> xtx2 <- crossprod(x)
```

```
> xtx2
```

```
      [,1] [,2]
[1,]   84  100
[2,]  100  120
```



```
R Console
> xtx2 <- crossprod(x)
> xtx2
      [,1] [,2]
[1,]   84  100
[2,]  100  120
> |
```

Note: Command `crossprod()` executes the multiplication faster than the conventional method with `t(x)%*%x`

Addition and subtraction of matrices (of same dimensions) can be executed with the usual operators + and -

```
> x <- matrix(nrow=4, ncol=2, data=1:8, byrow=T)
```

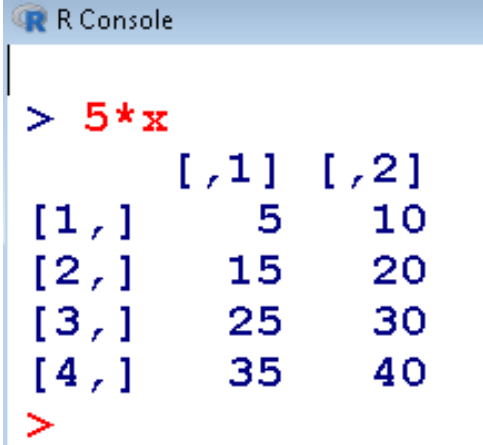
```
> x
```

```
      [,1] [,2]
[1,]    1    2
[2,]    3    4
[3,]    5    6
[4,]    7    8
```

```
R Console
> x <- matrix(nrow=4, ncol=2, data=1:8, byrow=T)
> x
      [,1] [,2]
[1,]    1    2
[2,]    3    4
[3,]    5    6
[4,]    7    8
>
```


Addition and subtraction of matrices (of same dimensions!) can be executed with the usual operators + and -

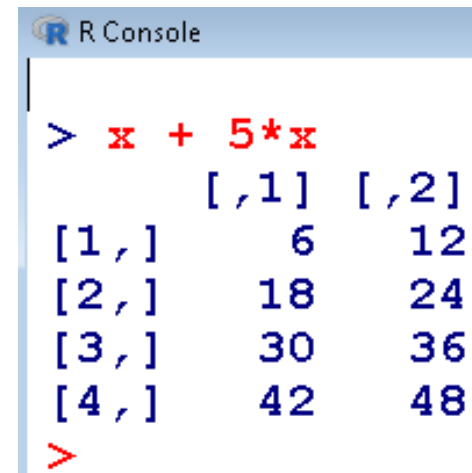
```
> 5*x  
      [,1] [,2]  
[1,]    5  10  
[2,]   15  20  
[3,]   25  30  
[4,]   35  40
```



```
R Console  
> 5*x  
      [,1] [,2]  
[1,]    5  10  
[2,]   15  20  
[3,]   25  30  
[4,]   35  40  
>
```

**Addition and subtraction of matrices (of same dimensions!)
can be executed with the usual operators + and -**

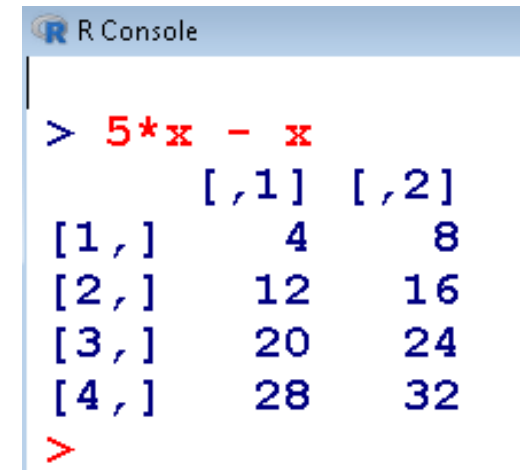
```
> x + 5*x
      [,1] [,2]
[1,]    6  12
[2,]   18  24
[3,]   30  36
[4,]   42  48
```



```
R Console
> x + 5*x
      [,1] [,2]
[1,]    6  12
[2,]   18  24
[3,]   30  36
[4,]   42  48
>
```

Addition and subtraction of matrices (of same dimensions!) can be executed with the usual operators + and -

```
> 5*x - x
      [,1] [,2]
[1,]    4    8
[2,]   12   16
[3,]   20   24
[4,]   28   32
```



```
R Console
> 5*x - x
      [,1] [,2]
[1,]    4    8
[2,]   12   16
[3,]   20   24
[4,]   28   32
>
```

Inverse of a matrix

`solve()` finds the inverse of a positive definite matrix

Example:

```
> y<- matrix( nrow=2, ncol=2, byrow=T,  
data=c(48,200,200,220))
```

```
> y  
      [,1] [,2]  
[1,]   48  200  
[2,]  200  220
```

Inverse of a matrix

```
> solve(y)
```

```
      [,1]      [,2]  
[1,] -0.007472826  0.006793478  
[2,]  0.006793478 -0.001630435
```

```
R Console  
  
> y<- matrix( nrow=2, ncol=2, byrow=T, data=c(48,200,200,220))  
> y  
      [,1] [,2]  
[1,]   48  200  
[2,]  200  220  
>  
> solve(y)  
      [,1]      [,2]  
[1,] -0.007472826  0.006793478  
[2,]  0.006793478 -0.001630435
```

Eigen Values and Eigen Vectors

`eigen()` finds the eigen values and eigen vectors of a positive definite matrix.

$$|A - \lambda I| = 0,$$

$$(A - \lambda I)b = 0$$

Eigen Values and Eigen Vectors

Example:

```
> y
```

```
      [,1] [,2]  
[1,]   48  200  
[2,]  200  220
```

```
> eigen(y)
```

```
eigen() decomposition
```

```
$`values`
```

```
[1] 351.70622 -83.70622
```

```
$vectors
```

```
      [,1]      [,2]  
[1,] 0.5499874 -0.8351730  
[2,] 0.8351730  0.5499874
```

```
R Console
```

```
> y
```

```
      [,1] [,2]  
[1,]   48  200  
[2,]  200  220
```

```
>
```

```
> eigen(y)
```

```
eigen() decomposition
```

```
$`values`
```

```
[1] 351.70622 -83.70622
```

```
$vectors
```

```
      [,1]      [,2]  
[1,] 0.5499874 -0.8351730  
[2,] 0.8351730  0.5499874
```