## Problems on Nyquist and Bode Stability Criteria

1. Consider a closed-loop system whose open-loop transfer function is given by:

$$G(s)H(s) = \frac{K}{(\tau_1 s + 1)(\tau_2 s + 1)}$$

Examine the stability of the closed-loop system using Nyquist plots for different values of K,  $\tau_1$  and  $\tau_2$ .

2. Consider the system with the following open-loop transfer function:

$$G(s)H(s) = \frac{K}{s(\tau_1 s + 1)(\tau_2 s + 1)}$$

Determine the stability of the closed-loop system for (1) gain K small, and (2) gain K large.

3. Consider the system with the following open-loop transfer function:

$$G(s)H(s) = \frac{K(\tau_2 s + 1)}{s^2(\tau_1 s + 1)}$$

Examine the stability of the closed-loop for the cases (1)  $\tau_1 < \tau_2$ , (2)  $\tau_1 = \tau_2$ , and (3)  $\tau_1 > \tau_2$ .

4. Consider the system with the following open-loop transfer function:

$$G(s)H(s) = \frac{K}{s(\tau s - 1)}$$

Determine the stability of the closed-loop system.

5. Consider the system with the following open-loop transfer function:

$$G(s)H(s) = \frac{K(s+3)}{s(s-1)}$$

for K > 1. Determine the stability of the closed-loop system.

6. Consider the open-loop transfer function

$$G(s)H(s) = \frac{K}{(s+1)(2s+1)(4s+1)}$$

Determine the closed-loop stability for K = 1 and K = 50.

7. Plot the Bode diagrm of the open-loop transfer function

$$G(s)H(s) = \frac{20(s+1)}{s(s+5)(s^2+2s+10)}$$
(1)

Determine the gain margin, phase margin, phase-crossover frequency, and gain-crossover frequency with Matlab.

8. Consider the three-tank system discussed in the lectures, now operating with a PID controller, a perfect measuring device, and a perfect valve. In this case, the open-loop transfer function will be given by:

$$G(s)H(s) = \frac{6K_c(1 + \tau_I s + \tau_D \tau_I s^2)}{\tau_I s(s+2)(s+4)(s+6)}$$

Determine the range of stable controller gains using Nyquist stability criterion for P-only control, PI control with  $1/\tau_I=0.05$ , and PID control with  $\tau_D=10,1/\tau_I=1.33$ . Also use gain-neutral Bode plots to determine the stability limit on  $K_c$  for each controller.