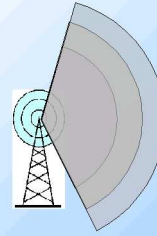


Basics of Wireless Signal Propagation

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RF Propagation



Questions:

How does RF propagate with distance?
 Behaviour under different environments
 How to quantify these?

Goals:

Estimate coverage area, link performance

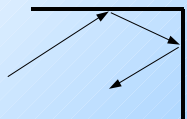
Use:

Determine network design parameters

- Locations of transmitters
- Transmit power
- Type of antenna

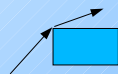


Three Basic Propagation Phenomena



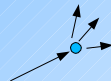
Reflection

$$\lambda \ll D$$



Diffraction

$$\lambda \simeq D$$

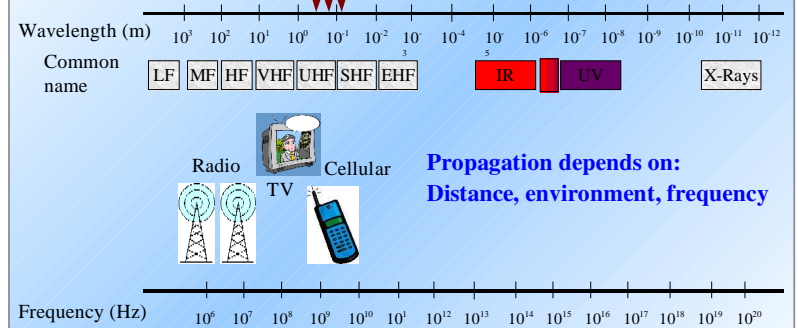


Scattering

$$\lambda \gg D$$

Electro-Magnetic Spectrum

ISM band: 902-928MHz, 2400-2483.5MHz, 5725-5785MHz



Propagation depends on:
 Distance, environment, frequency

dB: Relative Measure (to measure propapgation)

Gravitational force on a mass m at distance $d/2$
4 timers more

← Gravitational force on a mass m at distance d →

Gravitational force on a mass m at distance $10d$
100 times less

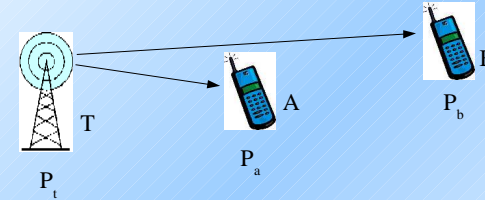
$$\text{dB} = 10 \times \log_{10}(\text{ratio})$$

6dB more

20dB less



Measuring Path Loss in dB



$$\text{Path loss at A} = 10 \times \log_{10} \left(\frac{P_t}{P_a} \right)$$

$$\text{Path loss at B} = 10 \times \log_{10} \left(\frac{P_t}{P_b} \right)$$



Measuring Absolute Power in dBm

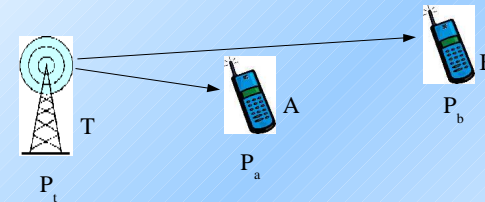
(Absolute power P) mW \equiv
 (Relative power of P w.r.t. 1mW) dBm \equiv
 $10 \times \log_{10} \left(\frac{P}{1 \text{ mW}} \right)$

Examples:

- 1 mW \equiv 0 dBm
- 0.1 mW \equiv -10 dBm
- 10 mW \equiv 10 dBm
- 100 mW \equiv 20 dBm



Putting Together dB and dBm

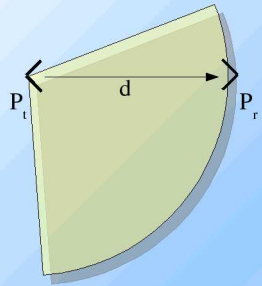


$$P_t = 20 \text{ dBm}, \text{ Path loss at A} = 30 \text{ dB}, P_a = ?$$

$$P_a = P_t - (\text{Pathloss}) = -10 \text{ dBm}$$



How to Estimate Path Loss?



Power density at receiver = $PD = \frac{P_t}{4 \times \pi \times d^2}$

$P_r = PD \times A_{eff}$, A_{eff} is the Antenna Efficiency

$A_{eff} = \frac{\lambda^2}{4 \times \pi}$ $P_r = P_t \times \left(\frac{\lambda}{4 \times \pi \times d}\right)^2$

Path loss = $\frac{P_r}{P_t} = \left(\frac{\lambda}{4 \times \pi \times d}\right)^2$

The above calculations assume the use of **isotropic antennae**

Frii's Free-Space Formula

Antenna Gain G: ratio of transmit/receive power in a particular direction, to that of an isotropic antenna
 Transmit gain == Receive gain

$$P_r = P_t \times G_t \times G_r \times \left(\frac{\lambda}{4 \times \pi \times d}\right)^2$$

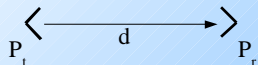
Some more useful forms of the Frii's formula:

$$P_r = P_t \times G_t \times G_r \times \left(\frac{c}{4 \times \pi \times f \times d}\right)^2$$

Free-space path-loss

$(P_r)_{dBm} = (P_t)_{dBm} + (G_t)_{dB} + (G_r)_{dB} - (32.5 + 20 \log_{10}(f) + 20 \log_{10}(d))$
 where f is in MHz and d is in km

Path Loss Example



$P_t = 50 \text{ mW}$, 2.4 GHz transmission, $d = 2 \text{ km}$, $P_r = ?$

PathLoss = $32.5 + 20 \log_{10}(2400) + 20 \log_{10}(2) \approx 106 \text{ dB}$
 $P_r = P_t - \text{PathLoss} = 17 \text{ dBm} - 106 \text{ dB} = -89 \text{ dBm}$



$G_t = 24 \text{ dBi}$, $G_r = 24 \text{ dBi}$, $P_r = ?$

$-89 \text{ dBm} + 24 \text{ dB} + 24 \text{ dB} = -41 \text{ dBm}$

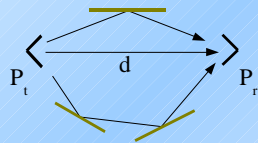
Path Loss Remarks

- Free space path loss is idealistic
- In reality, there is more path loss
 - Proportional to d^3 or higher
- Several path loss models are available
 - For indoor environments, outdoor metropolitan, etc.
- Now: more on RF propagation

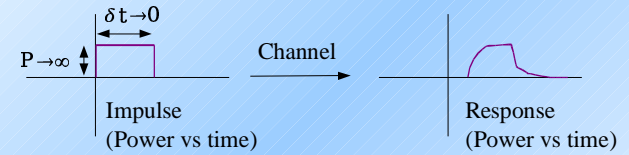
Fading and Multipath

Fading: the rapid variation of received signal strength over a small period of time

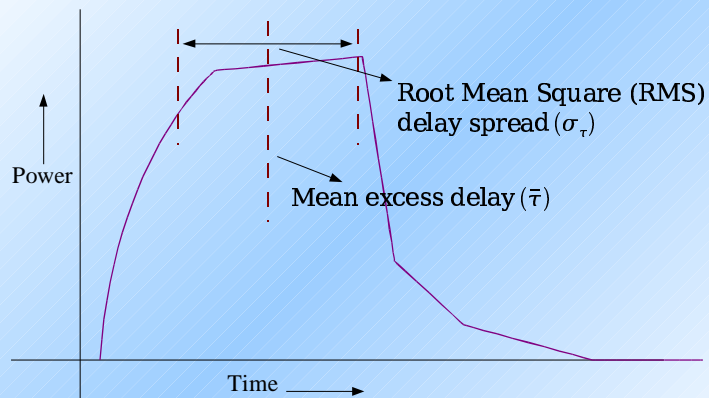
Due to multi-path Due to mobility



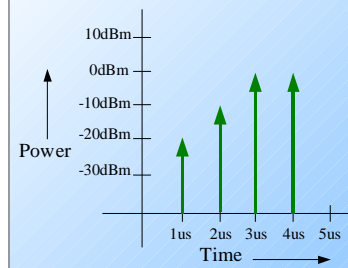
Channel Impulse Response



Power Delay Profile



An Example



$\bar{\tau}=? \quad \sigma_{\tau}=?$

$$\bar{\tau} = \frac{(0.01 \times 1 + 0.1 \times 2 + 1 \times 3 + 1 \times 4)}{(0.01 + 0.1 + 1 + 1)}$$

$\bar{\tau} = 3.42 \mu\text{s}$

$$\bar{\tau}^2 = \frac{(0.01 \times 1^2 + 0.1 \times 2^2 + 1 \times 3^2 + 1 \times 4^2)}{(0.01 + 0.1 + 1 + 1)}$$

$\bar{\tau}^2 = 12.04 \mu\text{s}^2$

$$\sigma_{\tau} = \sqrt{12.04 - 3.42^2} = 0.59 \mu\text{s}$$

Some Remarks

- RMS delay spread is a good measure of multi-path
 - Urban environments: 2-10 μ s
 - Indoors: 10-500 ns
- **Symbol time**: time to transmit a bit (0/1)
- Symbol time \sim RMS delay spread \implies **Inter-Symbol Interference (ISI)**
 - Equalization required
 - Generally, ISI results when
 - symbol time $< 10 \times$ RMS-delay-spread

