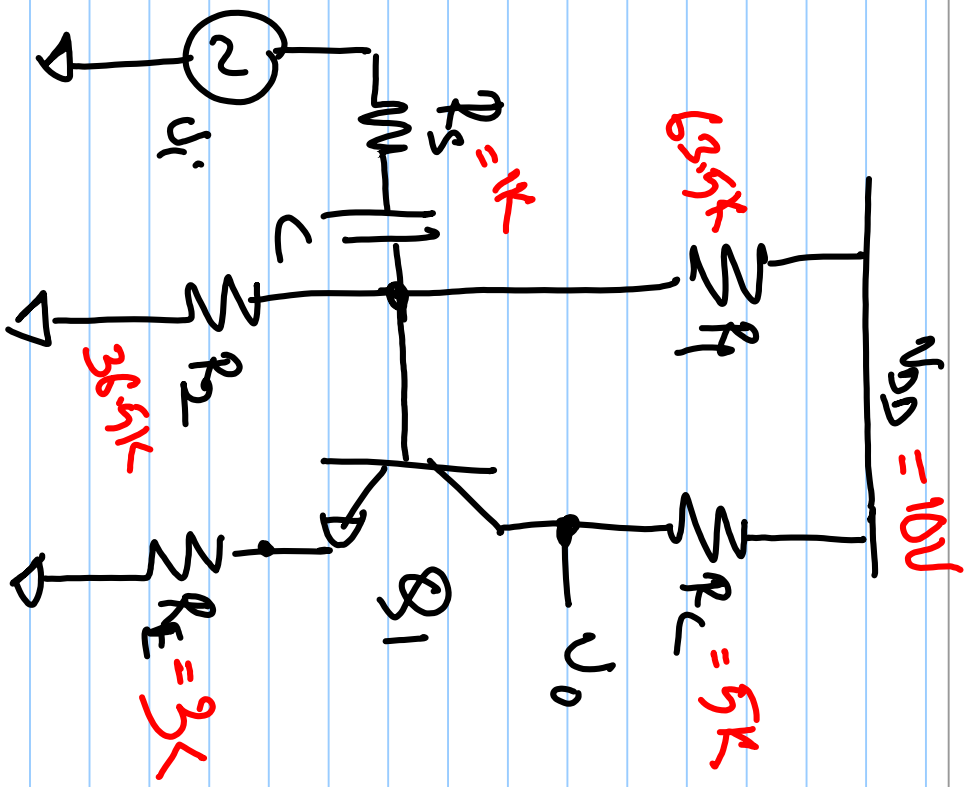


PROBLEM SET #9

①

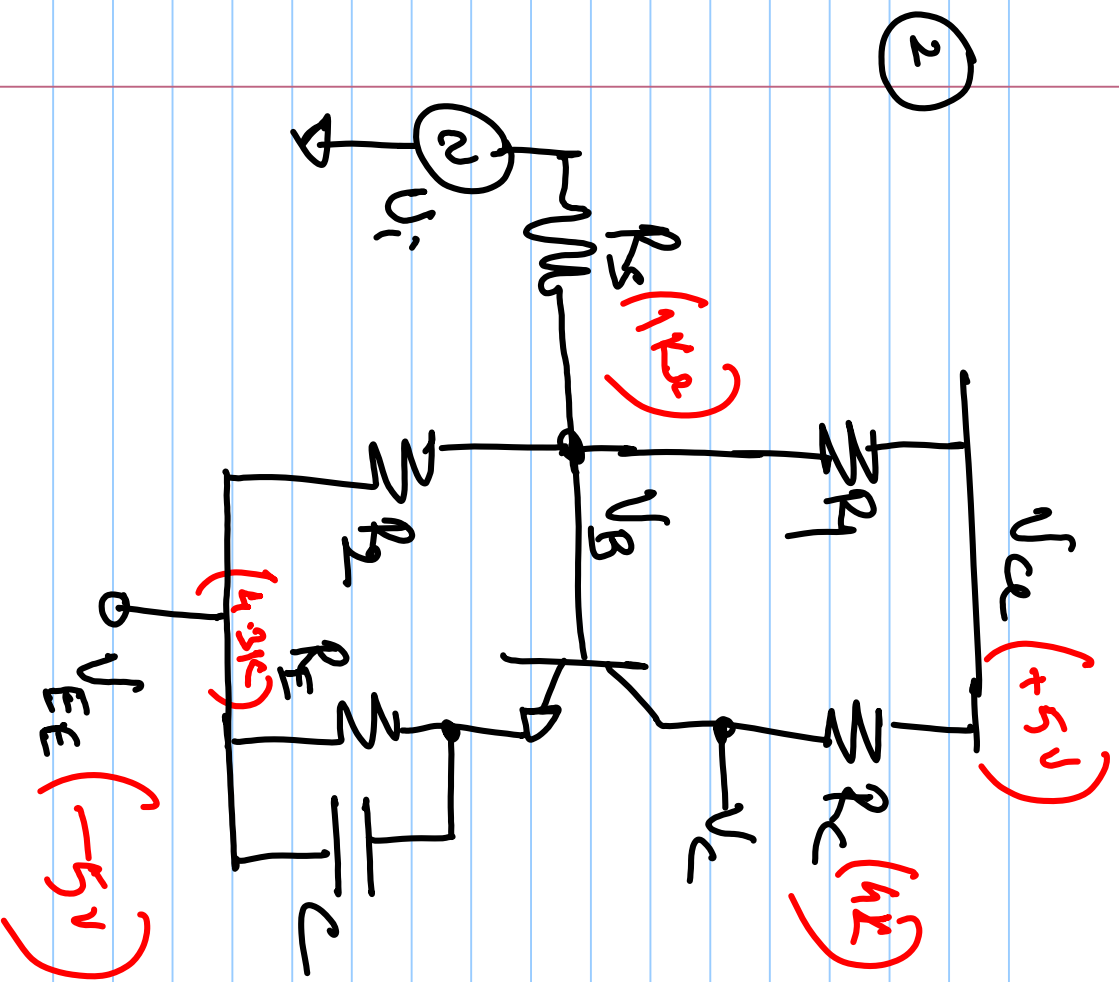


Q1 has a $\beta = 100$. (Assume $\beta = \alpha$ for bias calculation)
 Assume $V_T = 25\text{ mV}$, and C is large enough to be shorted at signal frequencies. (Assume $V_A = \infty$, and $V_{BE} = 0.69\text{ V}$)

(a) Find v_o/v_i .

(b) If $v_i = v_p \sin(\omega t)$, find ω at which $Q1$ is in active region and sufficiently β .

Use quiescent + incremental model for your analysis.



$\beta = 100$, $V_T = 25 \text{ mV}$. Note that one terminal of the i/p source is grounded, but $V_{EE} = -5 \text{ V}$. (Assume $V_A = \infty$). Assume $\beta = \infty$ for biasing.

a) Size R_1 and R_2 such that $V_{BQ} = 0 \text{ V}$, and $v_b \approx v_i$ for the following two cases.

- i) $C = 0$ ii) $C = \infty$.

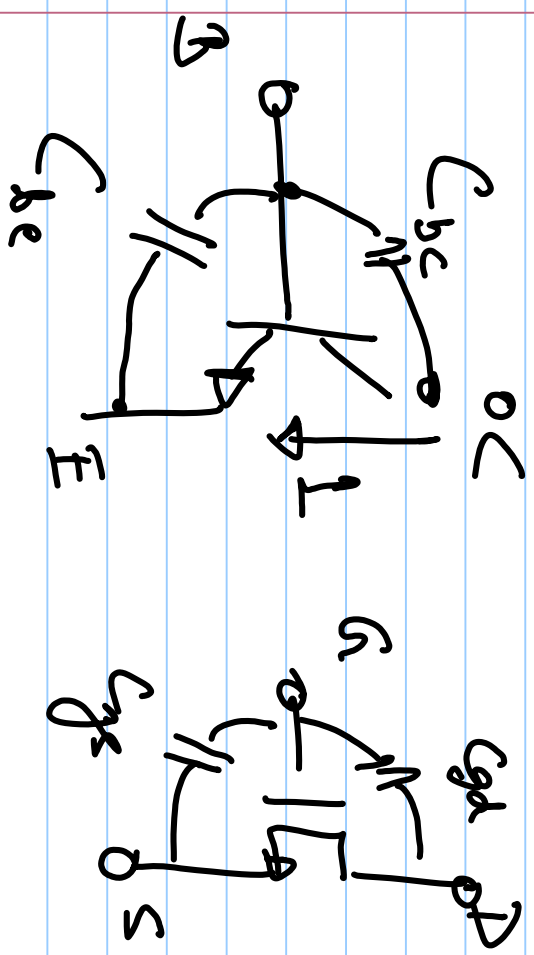
b) Find the swing limits of v_i if $v_o = V_p \sin(\omega t)$.

c) What benefit does a -ve power supply have (like the case in the figure)?

d) Find the time-constant associated with C.
How is it different from the expression that you get while using a MOSFET? What is the root cause behind it?

3

A diode has capacitances associated with its terminals.
 ∴ A BJT also has capacitances between its terminals.



BJT

$$C_{bc} = \frac{Z_T - 1}{V_T}$$

C_{bc} = depletion cap.

MOSFET

$$C_{gs} = \frac{2}{3} W L (\sqrt{V_{gs} - V_{tn}}) + C_{ovcap}$$

C_{gd} = overlap.
 Generally
 $C_{gs} \Rightarrow C_{gd}$.

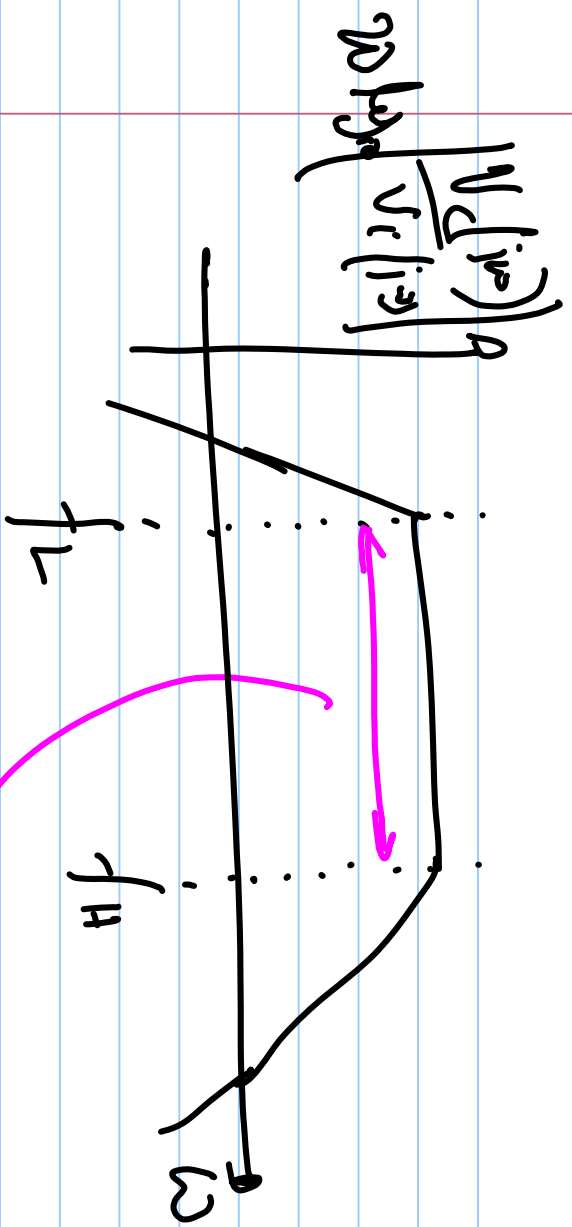
Generally
 $C_{gs} \Rightarrow C_{bc}$
 (Z_T = Device constant)

(a) Sketch the small signal model of a BJT with all the capacitances included.

(b) Find and sketch the frequency response of the amplifier in question 1, if a $C_c = 1\text{pF}$ is connected between V_c and ground.

Assume $C_{ge} = 1\text{pF}$, and neglect C_{bc} .

Size C such that the lower cutoff frequency is $10\times$ smaller than the higher cutoff frequency. (Fig. in next page)

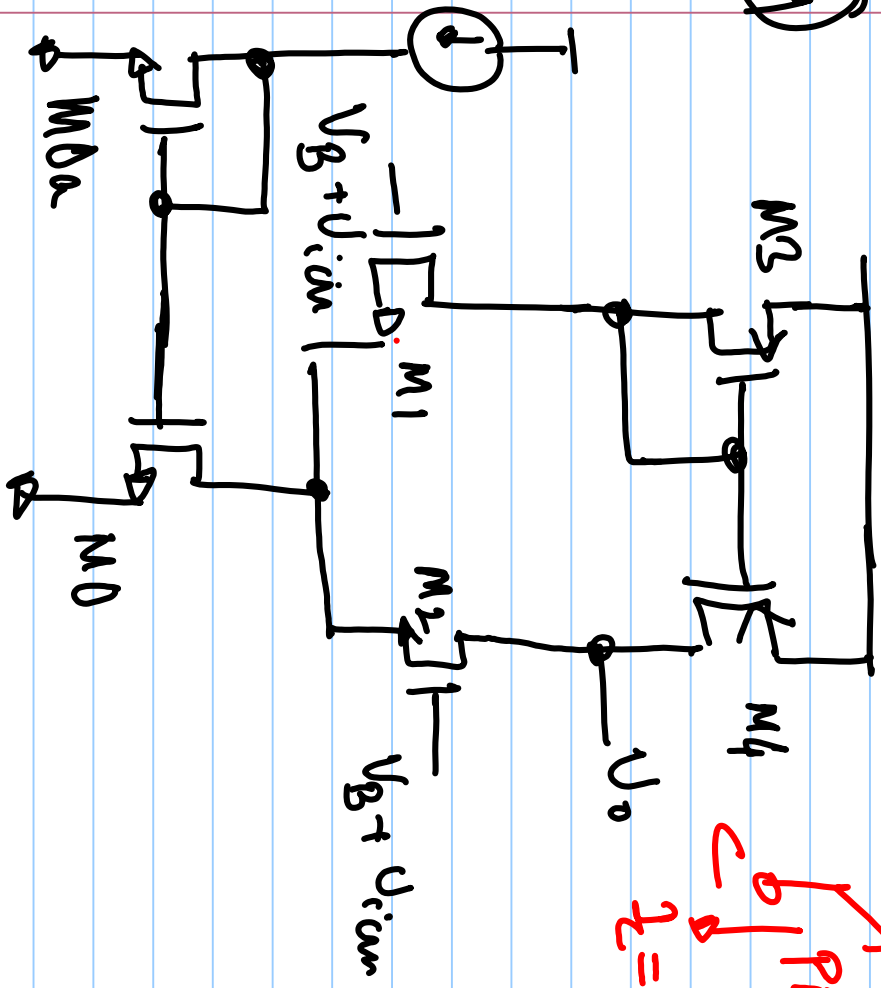


$$f_L = f_H / 10$$

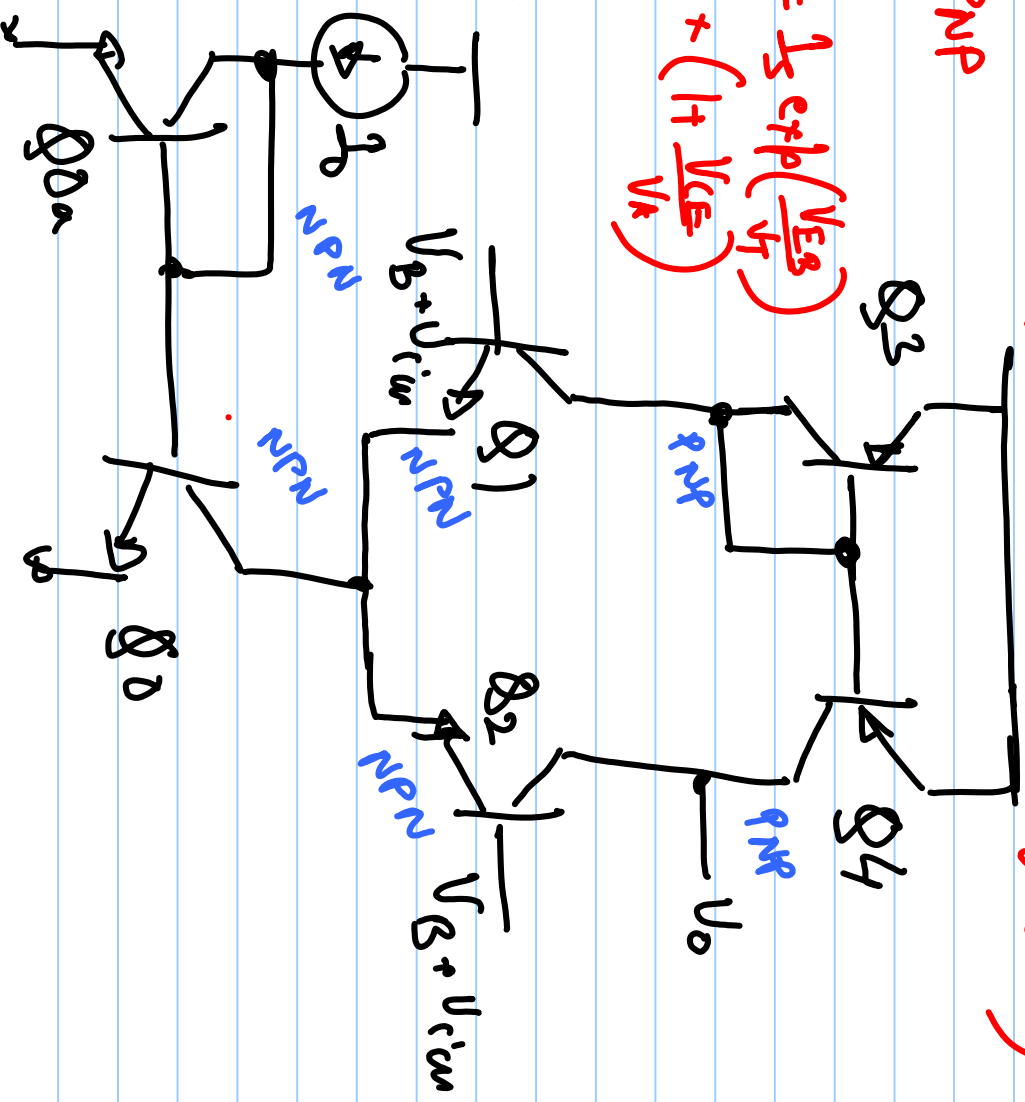
Midband Region.

③ What is the gain in the mid-band region, ie when $\omega f_L \ll \omega_0 \ll 2\pi f_H$?

(A)



$I_E \rightarrow I_B = \frac{I_E}{\beta}$ (Note the change in direction)
 $I_C = I_S \exp\left(\frac{V_{BE}}{V_T}\right) + \left(1 + \frac{V_{CE}}{V_A}\right)$



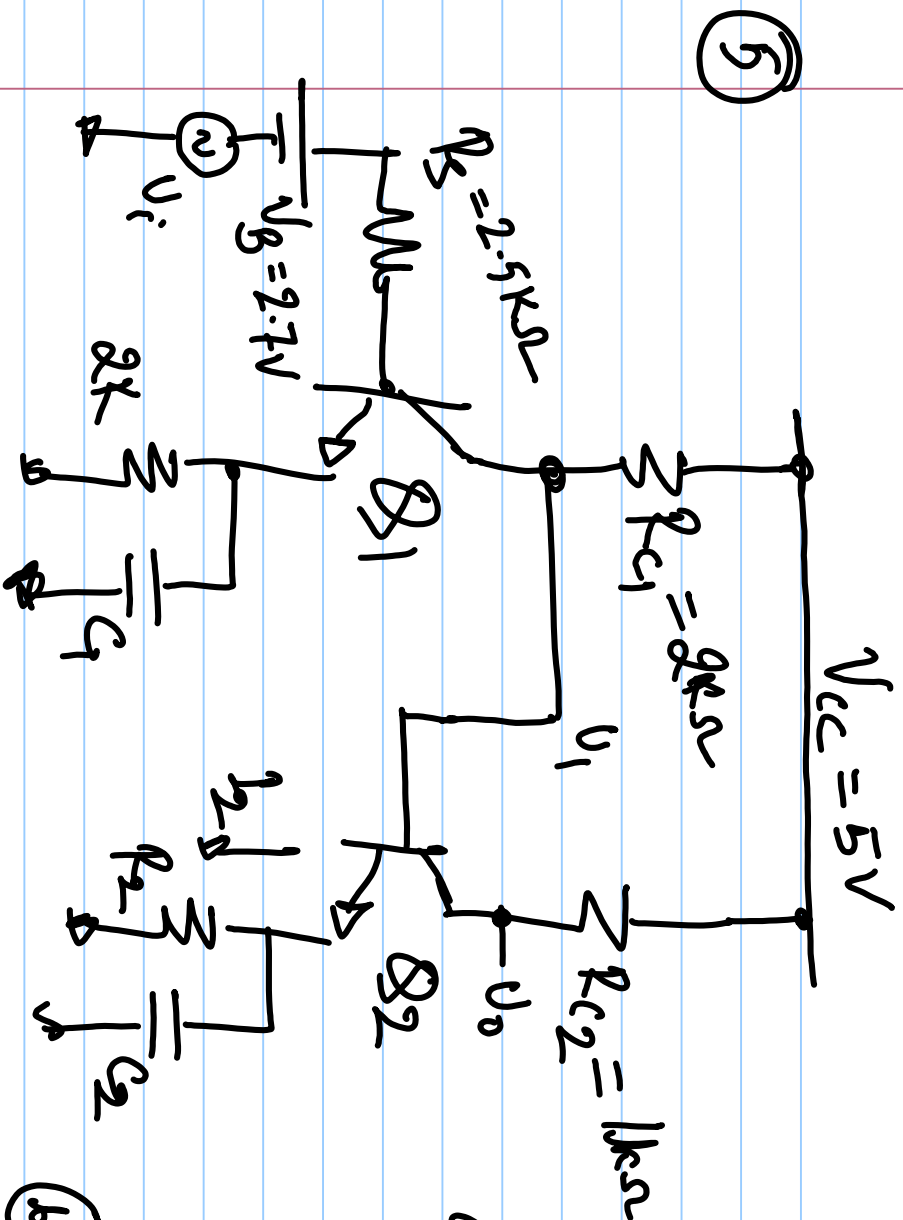
Assume all the MOSFETs and the BJTs are biased in saturation region and active region of operation respectively.

For MOSFETs neglect C_{LM} for M_1, M_2, M_{D2} , and consider C_{LM} for all other transistors.

For BJTs assume $\beta_{n1} = \infty$, (i.e. $\beta = \infty$) for all transistors.

Neglect base width modulation (i.e. assume $V_A = \infty$) for Q_1, Q_2, Q_{D2} , and assume finite V_A for all other transistors.

Find U_o/U_{in} .



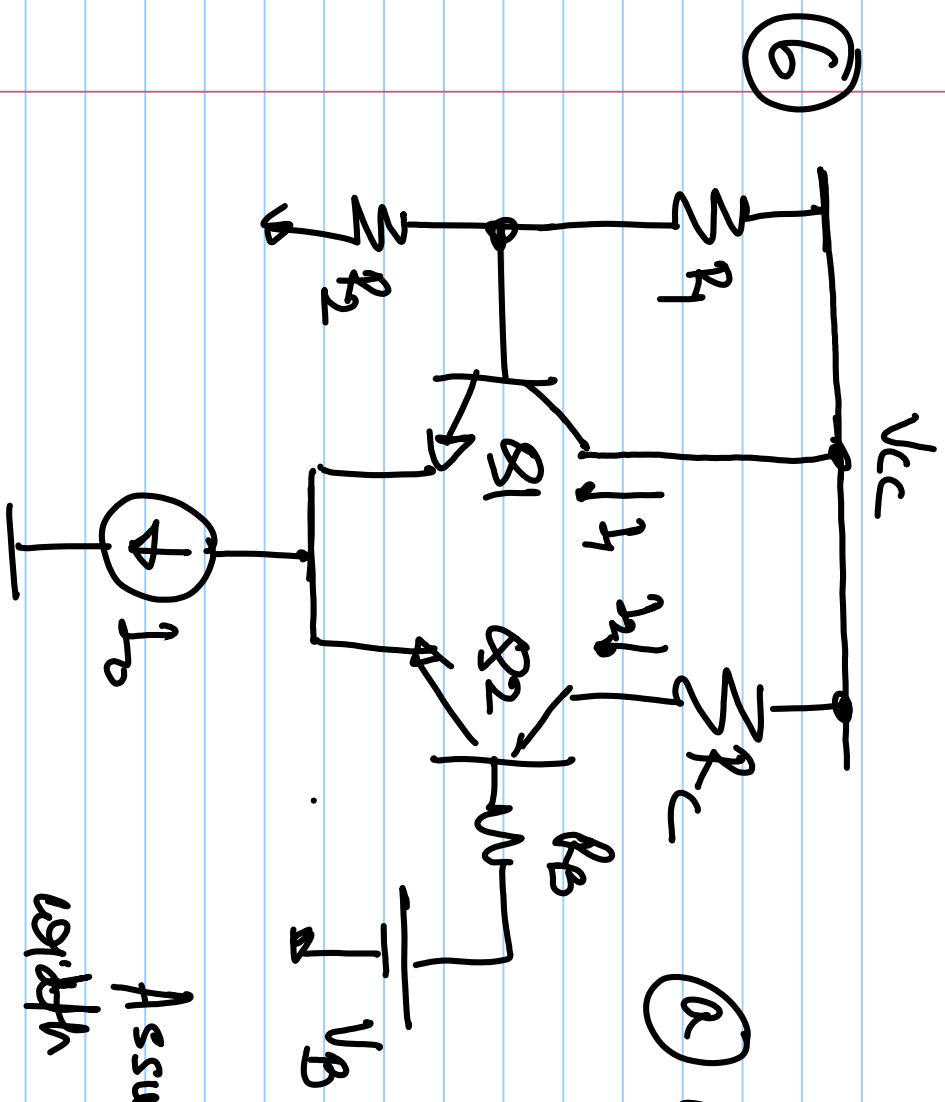
Assume $V_{BE} = 0.7V$

Neglect base current for Q-point calculation, but consider I_{B1} in incremental model. Consider $\beta = 100$, $V_T = 25mV$

(a) Size R_2 such that $I_2 = 2mA$..

(b) Find v_o/v_i ..

(c) If you don't want Q_2 to load Q_1 , suggest necessary modifications to the network. (Think V_{CC}).



$$R_1 = R_2$$

Q2 We want to ensure $I_1 = I_2$.

$$I_f V_B = \frac{V_{CC} R_2}{R_1 + R_2}$$

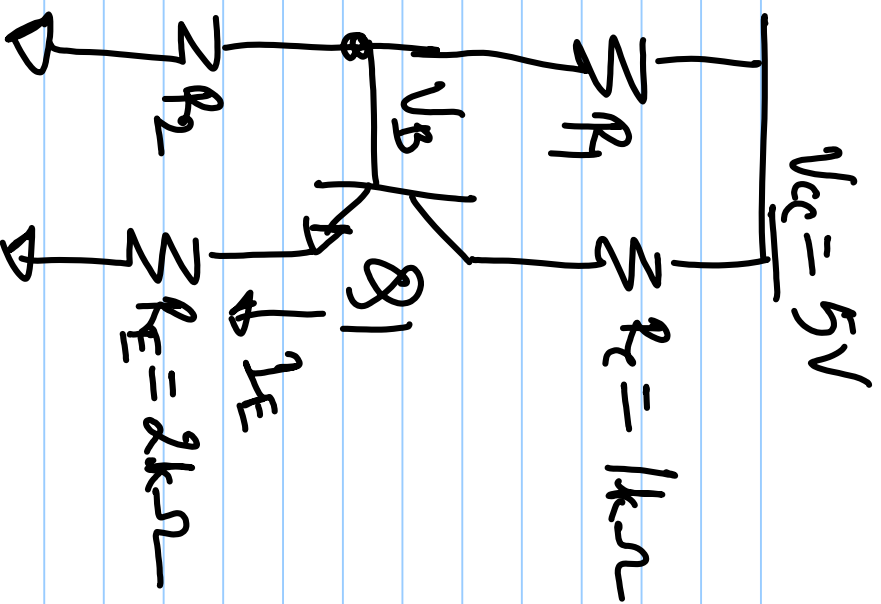
what value of R_B ensures

$$I_1 = I_2 = I_0/2 ?$$

Assume finite β , and neglect base current modulation. (i.e. $V_A = \infty$)

Q3 Why does the output make sense?

7

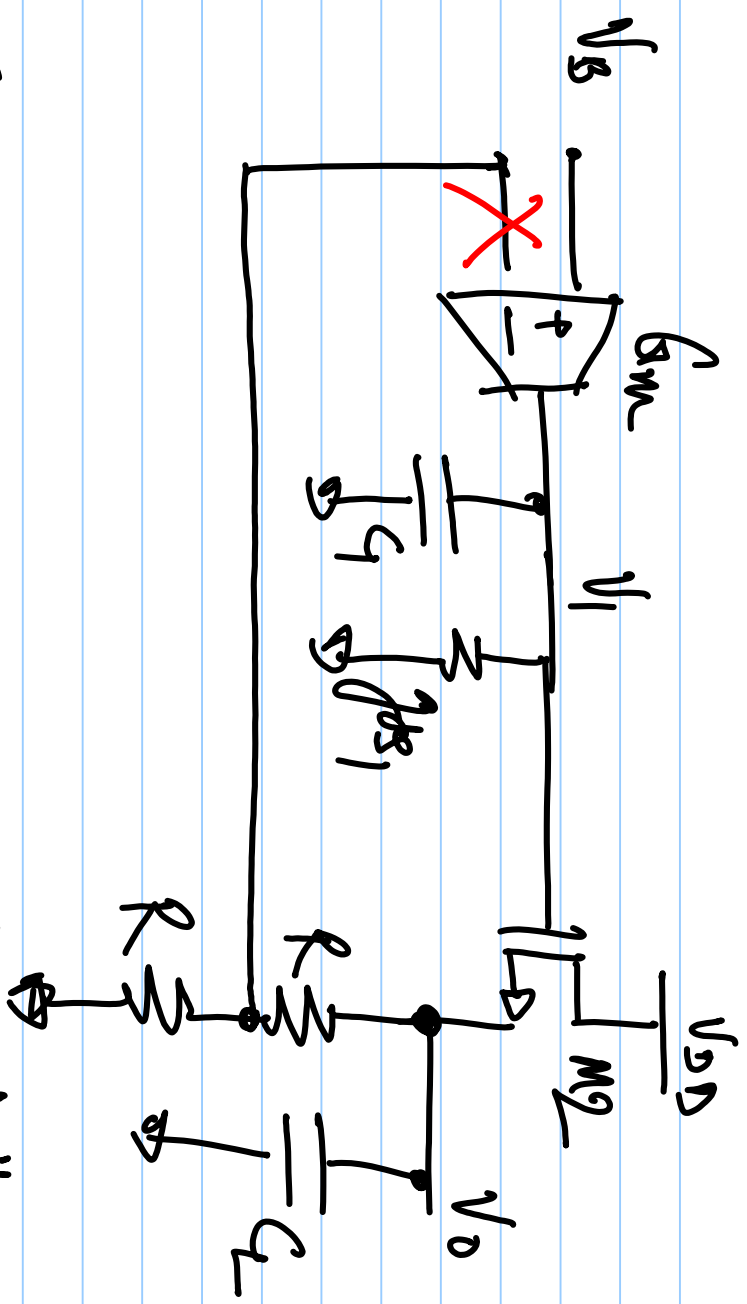


$\beta = 100$, $V_{BE} = 0.7V$.

Q Find R_1, R_2 such that $I_E = 1mA$,
and $Z_{in} \rightarrow (R_1 || R_2)$.

Do not ignore base current for
Q-point calculation.

8



$$\frac{g_m}{g_{s1}} = 100, \quad g_m = 1 \text{ mS}$$

$$C_1 = 0.1 \text{ pF}$$

$$R = 5 \text{ k}\Omega$$

g_{m2} CLM for M2.

$$V_B = 1.5 \text{ V}, \quad V_{DD} = 5 \text{ V}$$

$$I_{D1} = 500 \mu\text{A}$$

$$\mu_n C_{ox} = 0.2 \text{ mA/V}^2$$

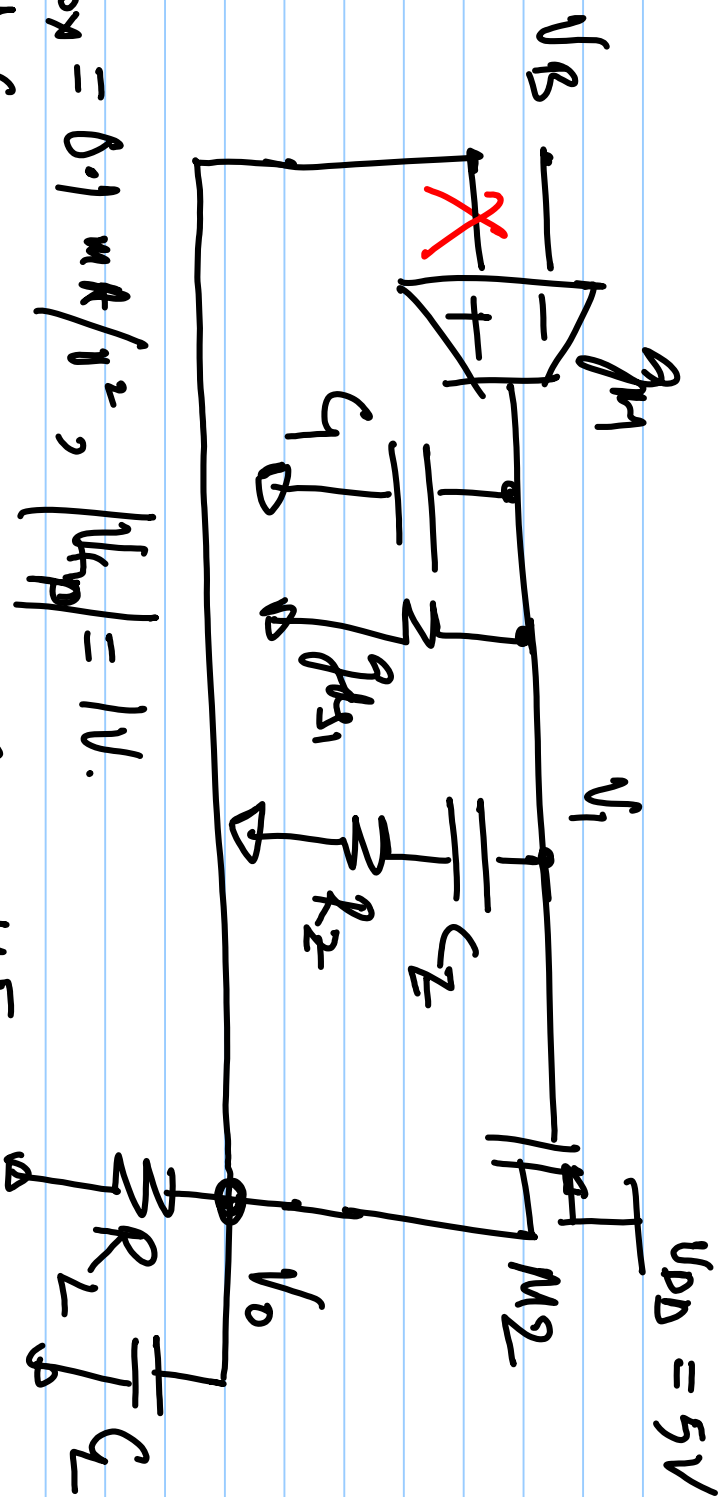
(a) What is the expected V_0 if the loop has $L(\omega) \rightarrow \infty$

(b) Size M2 such that $V_1 = 4.5 \text{ V}$.

c) What is the expression of the loop gain, $L(s)$.
Break the loop @ ~~X~~ for your analysis.

d) What is the constraint on G_2 , such that the $P_2 = 4$ b/wh, when $K_{wh} =$ unity gain frequency of the loop, and P_2 is the pole associated with G_2 . (Note that the loop needs to be broken at X for finding poles of the loop-gain).

Q



$$\mu_n C_{ox} = 0.1 \text{ mA/V}^2, |V_{thp}| = 1 \text{ V.}$$

$$g_m = 1 \text{ mS}$$

$$R_2 = 10 \mu\text{s.}$$

$$C_1 = 1 \text{ pF}, C_2 = 1 \text{ pF},$$

$$R_L = 1 \text{ k}\Omega, V_B = 4 \text{ V.}$$

Find the loop gain symbolically (Assume $g_{m1} = 0$)

b) Size M_2 such that it is in saturation with a margin of 50dB.

c) Size R_2 , C_2 such that the phase margin associated with the loop is 76° .

(Hint: Find all the poles and zeros of $L(s)$ explicitly, find ω_{gb} from the loop gain and then calculate phase margin).